

Lecture 13  
2023/2024

# Microwave Devices and Circuits for Radiocommunications

# 2023/2024

- 2C/1L, **MDCR**
- **Attendance at minimum 7 sessions (course or laboratory)**
- Lectures- **associate professor Radu Damian**
  - Tuesday 16-18, ~~Online~~, P8
  - E – 50% final grade
  - **problems** + (2p atten. lect.) + (3 tests) + (bonus activity)
    - first test L1: 20-27.02.2024 (t2 and t3 not announced, lecture)
    - 3att.=+0.5p
  - **all materials/equipments authorized**

# 2023/2024

- Laboratory – **associate professor Radu Damian**
  - Tuesday 08-12, 11.13 / (08:10)
  - L – 25% final grade
    - ADS, 4 sessions
    - Attendance + **personal results**
  - P – 25% final grade
    - ADS, 3 sessions (-1? 20.02.2024)
    - personal homework

# Materials

■ <http://rf-opto.etti.tuiasi.ro>

The screenshot shows a web browser window with the URL [http://rf-opto.etti.tuiasi.ro/microwave\\_cd.php?chg\\_lang=0](http://rf-opto.etti.tuiasi.ro/microwave_cd.php?chg_lang=0). The page features a dark blue navigation bar with links for Main, Courses, Master, Staff, Research, Students, and Admin. Below this is a secondary navigation bar with links for Microwave CD, Optical Communications, Optoelectronics, Internet, Antennas, Practica, Networks, and Educational software. The main content area is titled "Microwave Devices and Circuits for Radiocommunications (English)" and includes the following information:

- Course: MDCR (2017-2018)**
- Course Coordinator:** Assoc.P. Dr. Radu-Florin Damian
- Code:** EDOS412T
- Discipline Type:** DOS; Alternative, Specialty
- Credits:** 4
- Enrollment Year:** 4, Sem. 7

**Activities**

**Course:** Instructor: Assoc.P. Dr. Radu-Florin Damian, 2 Hours/Week, Specialization Section, Timetable:  
**Laboratory:** Instructor: Assoc.P. Dr. Radu-Florin Damian, 1 Hours/Week, Group, Timetable:

**Evaluation**

Type: Examen

**A:** 50%, (Test/Colloquium)  
**B:** 25%, (Seminary/Laboratory/Project Activity)  
**D:** 25%, (Homework/Specialty papers)

**Grades**

[Aggregate Results](#)

**Attendance**

[Course](#)  
[Laboratory](#)

**Lists**

[Bonus-uri acumulate \(final\)](#)  
[Studenti care nu pot intra in examen](#)

**Materials**

**Course Slides**

- [MDCR Lecture 1](#) (pdf, 5.43 MB, en, [↗](#))
- [MDCR Lecture 2](#) (pdf, 3.67 MB, en, [↗](#))
- [MDCR Lecture 3](#) (pdf, 4.76 MB, en, [↗](#))
- [MDCR Lecture 4](#) (pdf, 5.58 MB, en, [↗](#))

On the right side of the screenshot, there is a banner for "RF-OPTO" with the ETTI logo and the University of Technical Sciences (UTS) logo. The banner includes language selection options: "English" (highlighted with a red circle) and "Romana". Below the banner is a navigation bar with links for Main, Courses, Master, Staff, and Research. A secondary navigation bar below that includes links for Grades, Student List, Exams, and Photos. The main content area on the right is titled "Online Exams" and includes the text: "In order to participate at online exams you must get ready following..."

# Site



## Microwave and Optoelectronics Laboratory

We are enlisted in the Telecommunications Department of the Electronics, Telecommunication and Information Technology Faculty (ETTI) from the "Gh. Asachi" Technical University (TUIASI) in Iasi, Romania

We currently cover inside ETTI the fields related to:

- Microwave Circuits and Devices
- Optoelectronics
- Information Technology

### Courses

| Nr. | Course  | Shortcut | Code       | Type | Semester | Credits | Weekly         | Examination  | Link                    |
|-----|---|----------|------------|------|----------|---------|----------------|--------------|-------------------------|
| 1   | Microwave Devices and Circuits for Radiocommunications                | DCMR     | DOS412T    | DOS  | 7        | 4       | 0P,1L,0S,2C    | Exam         | <a href="#">details</a> |
| 2   | Monolithic Microwave Integrated Circuits                              | CIMM     | RD.IA.207  | DOMS | 11       | 6       | 1.5L,0S,2C,0P  | Exam         | <a href="#">details</a> |
| 3   | Advanced Techniques in the Design of the Radio-communications Systems | TAPSR    | RD.IA.103  | DIMS | 9        | 6       | 1.5P,0L,0S,2C  | Exam         | <a href="#">details</a> |
| 4   | Optical Communications  | CO       | DOS409T    | DOS  | 7        | 5       | 0P,1L,0S,3C    | Colloquium   | <a href="#">details</a> |
| 5   | Optical Communications  | OC       | EDOS409T   | DOS  | 7        | 5       | 0P,1L,0S,3C    | Exam         | <a href="#">details</a> |
| 6   | Satellite Communications  | CS       | RC.IA.104  | DIMS | 9        | 6       | 0L,0S,2C,1.5P  | Exam         | <a href="#">details</a> |
| 7   | Applied Informatics 1   | IA1      | DOF135     | DOF  | 1        | 4       | 0P,1L,0S,2C    | Verification | <a href="#">details</a> |
| 8   | Applied Informatics 1   | AI1      | EDOF135    | DOF  | 1        | 4       | 0P,1L,0S,2C    | Verification | <a href="#">details</a> |
| 9   | Databases, Web Programming and Interfacing                            | DWPI     | ITT.IA.601 | DIS  | 11       | 5       | 1P,1L,0.25S,1C | Verification | <a href="#">details</a> |
| 10  | Web Applications Design   | PAW      | RC.IA.108  | DIMS | 10       | 5       | 1L,0S,1.5C,1P  | Exam         | <a href="#">details</a> |
| 11  | Optoelectronics   | OPTO     | DID405M    | DID  | 8        | 4       | 0P,1L,0S,2C    | Colloquium   | <a href="#">details</a> |
| 12  | Microwave Devices and Circuits for Radiocommunications (English)      | MDCR     | EDOS412T   | DOS  | 8        | 4       | 0P,1L,0S,2C    | Exam         | <a href="#">details</a> |



# Materials

- RF-OPTO
  - <http://rf-opto.etti.tuiasi.ro>
- **David Pozar, “Microwave Engineering”,**  
Wiley; 4th edition , 2011
  - 1 exam problem ← Pozar
- Photos
  - sent by email/**online exam > Week4-Week6**
  - used at lectures/laboratory

# Online – Registration no.

- access to **online exams** requires the **password** received by email

The password is communicated during the lectures. It is necessary to

**Password**



**Registration no.**

**Name of the student**

**Proposed email 1**

**Proposed email 2**

**Write the code below**

 **RF-OPTO** 

English | Romana |

[Main](#) [Courses](#) [Master](#) [Staff](#) [Research](#) [Students](#)

[Login](#) [Tutoring](#)

**Login**

Use the Registration no. and your email or the password received by email

**Registration no.**

**Email/Password**

**Write the code below**

# Password

## ■ received by email

Important message from RF-OPTO Inbox x

 **Radu-Florin Damian**  
to me, POPESCU ▾

 Romanian ▾ > English ▾ [Translate message](#)



Laboratorul de Microunde si Optoelectronica  
Facultatea de Electronica, Telecomunicatii si Tehnologia Informatiei  
Universitatea Tehnica "Gh. Asachi" Iasi


**In atentie: POPESCU GOPO ION**

Parola pentru a accesa examenele pe server-ul **rf-opto** este  
Parola: 

Identificati-va pe [server](#), cu parola, cat mai rapid, pentru confirmare.




**Memorati** acest mesaj intr-un loc sigur, pentru utilizare ulterioara

**Attention: POPESCU GOPO ION**







The password to access the exams on the **rf-opto** server is  
Password: 


Login to the [server](#), with this password, as soon as possible, for confirmation.

**Save** this message in a safe place for later use


 Reply  Reply all  Forward


Subject

|   | Subject   | Correspondents  |
|---|---|---|
|  | <b>Important message from RF-OPTO</b>   | POPESCU GOPO ION  |
|  | Validation of MD/CR exam from 02/05/2020  |  |
|  |  |  |

From Me <rdamian@etti.tuiasi.ro> 

Subject **Important message from RF-OPTO**

To 

Cc Me <rdamian@etti.tuiasi.ro> 



Laboratorul de Microunde si Optoelectronica  
Facultatea de Electronica, Telecomunicatii si Tehnologia Informatiei  
Universitatea Tehnica "Gh. Asachi" Iasi


**In atentie: POPESCU GOPO ION**

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**Memorati** acest mesaj intr-un loc sigur, pentru utilizare ulterioara

**Attention: POPESCU GOPO ION**

The password to access the exams on the **rf-opto** server is  
Password: 

Login to the [server](#), with this password, as soon as possible, for confirmation.

**Save** this message in a safe place for later use



# Online exam manual

- The online exam app used for:
  - ~~lectures (attendance)~~
  - laboratory
  - project
  - ~~examinations~~

## Materials

### Other data

[Manual examen on-line](#) (pdf, 2.65 MB, ro, 🇷🇴)

[Simulare Examen](#) (video) (mp4, 65.12 MB, ro, 🇷🇴)

## Microwave Devices and Circuits (Englis

# Examen online

- always against a **timetable**
  - long period (lecture attendance/laboratory results)
  - ~~short period (tests: 15min, exam: 2h)~~

|   |   |  |                                      |                                  |   |  |
|---|---|--|--------------------------------------|----------------------------------|---|--|
| <b>Announcement</b><br>23:59 (10/05/2020) | <b>Support material</b><br>00:05 (11/05/2020) | <b>Exam Topics</b><br>00:07 (11/05/2020) | <b>Results</b><br>00:10 (11/05/2020) | <b>End</b><br>00:20 (15/05/2020) | <b>Confirmation</b><br>00:20 (16/05/2020) | Next timeframe in:<br>05 m 43 s<br><a href="#">Refresh now</a> |
|---|---|--|--------------------------------------|----------------------------------|---|--|

**Announcement**

This is a "fake" exam, introduced to familiarize you with the server interface and to perform the necessary actions during an exam: thesis scan, selfie, use email for co

**Server Time**

All exams are based on the server's time zone (it may be different from local time). For reference time on the server is now:

10/05/2020 23:59:16

# Online results submission

- many numerical values/files

| Schema finala             | Rezultate - castig        | Rezultate - zgomot        | Fisier justificare calcul (factor andrei) | Fisier zap (optional)     | T1, fisier parametri S    | T2, fisier parametri S    | Z1      | Z2      | Z3      | Z4      | Z5     | Z6      | Z7      | Ze1    | Zo1    | Ze2   | Zo2   | Ze3   | Zo3   | Ze4   | Zo4   | Ze5   | Zo5   | Ze6  |   |
|---------------------------|---------------------------|---------------------------|---|---------------------------|---------------------------|---------------------------|---------|---------|---------|---------|--------|---------|---------|--------|--------|-------|-------|-------|-------|-------|-------|-------|-------|------|---|
| 86 -<br>5428 -<br>259 ... | 86 -<br>5428 -<br>260 ... | 86 -<br>5428 -<br>261 ... | 86 -<br>5428 -<br>316 ...                 | -                         | 86 -<br>5428 -<br>314 ... | 86 -<br>5428 -<br>315 ... | 148.33  | 155.88  | 202.12  | 164.35  | 180.91 | 30.29   | 185.19  | 79.9   | 37     | 68.89 | 45.14 | 61.83 | 45.05 | 57.97 | 46.02 | 61.85 | 45.05 | 68.8 |   |
| 86 -<br>5622 -<br>259 ... | 86 -<br>5622 -<br>260 ... | 86 -<br>5622 -<br>261 ... | 86 -<br>5622 -<br>316 ...                 | 86 -<br>5622 -<br>262 ... | 86 -<br>5622 -<br>314 ... | 86 -<br>5622 -<br>315 ... | 26.97   | 153.5   | 34.64   | 35.79   | 55.56  | 26.212  | 10.693  | 0      | 0      | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0    | 0 |
| 86 -<br>5488 -<br>259 ... | 86 -<br>5488 -<br>260 ... | 86 -<br>5488 -<br>261 ... | 86 -<br>5488 -<br>316 ...                 | 86 -<br>5488 -<br>262 ... | 86 -<br>5488 -<br>314 ... | 86 -<br>5488 -<br>315 ... | 0       | 0       | 0       | 0       | 0      | 0       | 0       | 0      | 0      | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0    | 0 |
| 86 -<br>5391 -<br>259 ... | 86 -<br>5391 -<br>260 ... | 86 -<br>5391 -<br>261 ... | 86 -<br>5391 -<br>316 ...                 | -                         | -                         | -                         | 50      | 50      | 50      | 50      | 50     | 50      | 50      | 70.14  | 40.39  | 61.85 | 44.59 | 55.7  | 45.2  | 54.89 | 45.38 | 58.65 | 45.8  | 70.0 |   |
| 86 -<br>5664 -<br>259 ... | 86 -<br>5664 -<br>260 ... | 86 -<br>5664 -<br>261 ... | 86 -<br>5664 -<br>316 ...                 | -                         | 86 -<br>5664 -<br>314 ... | 86 -<br>5664 -<br>315 ... | 168.02  | 150.5   | 178.28  | 133.75  | 92.12  | 121.67  | 144.48  | 94.36  | 36.19  | 70.77 | 42.56 | 65.69 | 42.05 | 55.17 | 42.29 | 65.59 | 42.05 | 70.7 |   |
| 86 -<br>5665 -<br>259 ... | 86 -<br>5665 -<br>260 ... | 86 -<br>5665 -<br>261 ... | 86 -<br>5665 -<br>316 ...                 | -                         | 86 -<br>5665 -<br>314 ... | 86 -<br>5665 -<br>315 ... | 162.2   | 80.8    | 209.2   | 140.85  | 135.1  | 183.7   | 167.6   | 94.58  | 36.15  | 78.16 | 39.77 | 65.57 | 45.05 | 65.57 | 45.05 | 78.16 | 39.77 | 94.5 |   |
| 86 -<br>5433 -<br>259 ... | 86 -<br>5433 -<br>260 ... | 86 -<br>5433 -<br>261 ... | 86 -<br>5433 -<br>316 ...                 | -                         | 86 -<br>5433 -<br>314 ... | 86 -<br>5433 -<br>315 ... | 165.138 | 106.228 | 226.157 | 130.134 | 72.71  | 180.177 | 164.616 | 101.36 | 36.11  | 77.22 | 42.49 | 68.02 | 45.62 | 60    | 45.42 | 68.02 | 45.62 | 77.2 |   |
| 86 -<br>5608 -<br>259 ... | 86 -<br>5608 -<br>260 ... | 86 -<br>5608 -<br>261 ... | 86 -<br>5608 -<br>316 ...                 | -                         | 86 -<br>5608 -<br>314 ... | 86 -<br>5608 -<br>315 ... | 150.84  | 152.5   | 30.94   | 32.37   | 54.36  | 19.837  | 29.85   | 64.14  | 40.145 | 54.32 | 46.32 | 53.8  | 46.7  | 53.8  | 46.7  | 54.32 | 46.32 | 54.9 |   |
| 86 -<br>5555 -<br>259 ... | 86 -<br>5555 -<br>260 ... | 86 -<br>5555 -<br>261 ... | 86 -<br>5555 -<br>316 ...                 | -                         | 86 -<br>5555 -<br>314 ... | 86 -<br>5555 -<br>315 ... | 168.001 | 150.288 | 178.399 | 133.115 | 92.491 | 121.257 | 144.126 | 97.05  | 36.16  | 71.13 | 43.09 | 65.45 | 42.12 | 55.66 | 42.18 | 65.45 | 42.12 | 71.1 |   |

# Online results submission

- many numerical values

|  | Z1     | Z2     | Z3     | Z4     | Z5     | Z6     | Z7     |
|--|--------|--------|--------|--------|--------|--------|--------|
|  | 148.33 | 155.88 | 202.12 | 164.35 | 180.91 | 30.29  | 185.19 |
|  | 25.97  | 153.5  | 34.64  | 35.79  | 55.56  | 26.212 | 10.692 |
|  | 0      | 0      | 0      | 0      | 0      | 0      | 0      |
|  | 50     | 50     | 50     | 50     | 50     | 50     | 50     |



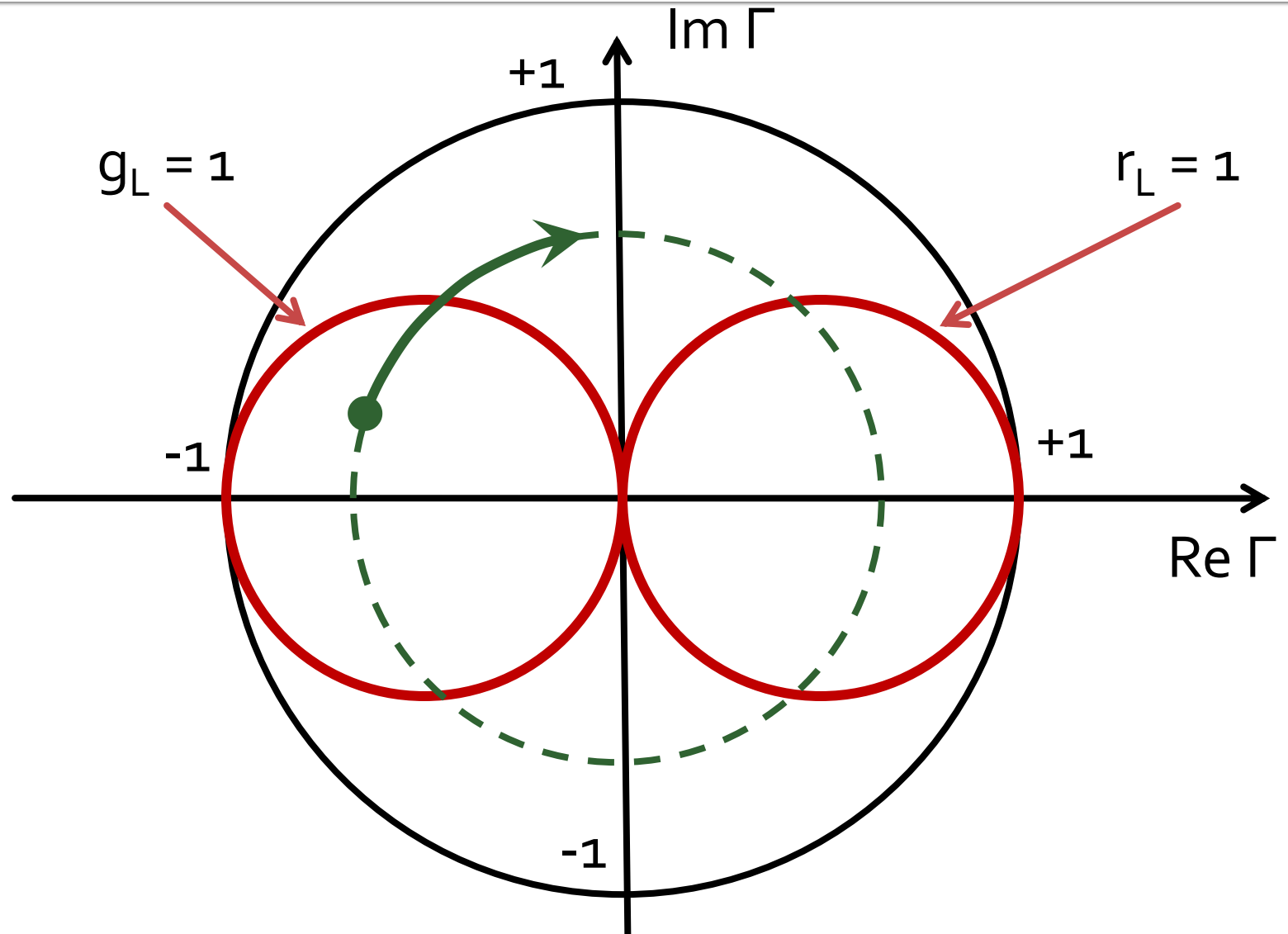
# Online results submission

**Grade = Quality of the work +  
+ Quality of the submission**

Impedance Matching

# Impedance Matching with Stubs

# Smith chart, $r=1$ and $g=1$



# Analytical solutions

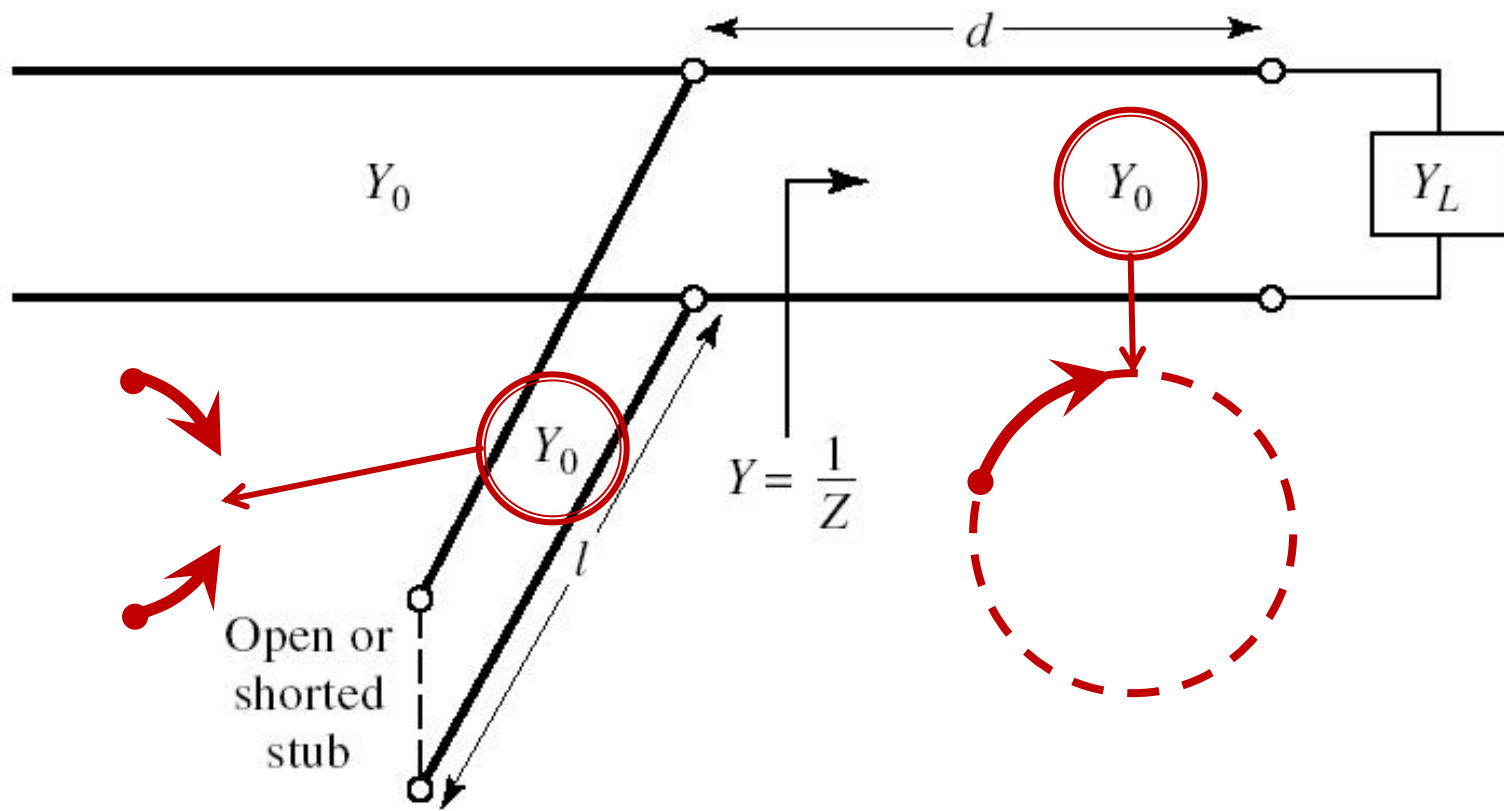
Exam / Project

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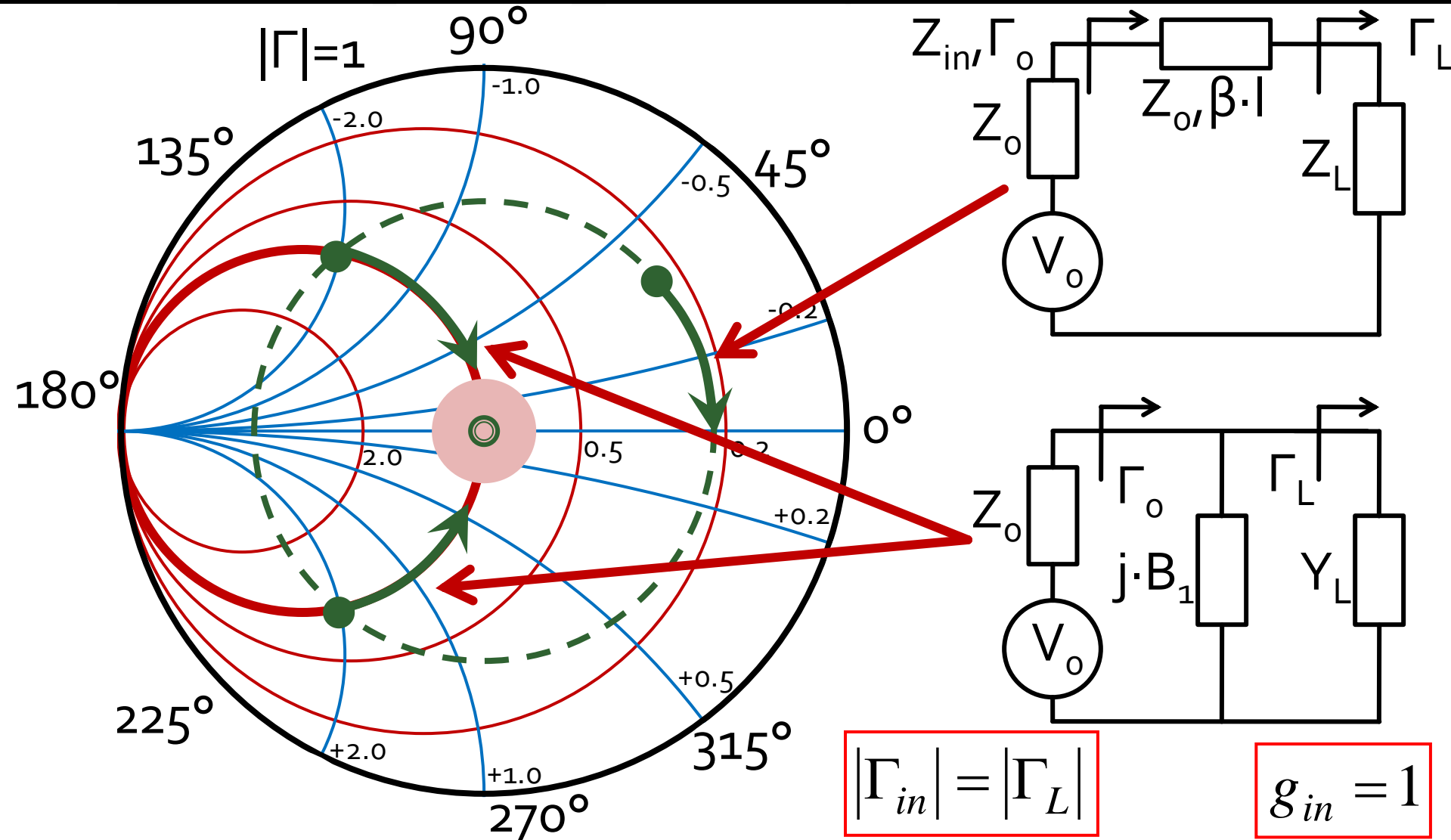


# Case 1, Shunt Stub

- Shunt Stub



# Matching, series line + shunt susceptance



# Analytical solution, usage

$$\cos(\varphi + 2\theta) = -|\Gamma_S|$$

$$\Gamma_S = 0.593 \angle 46.85^\circ$$

$$\theta_{sp} = \beta \cdot l = \tan^{-1} \frac{\mp 2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}}$$

$$|\Gamma_S| = 0.593; \quad \varphi = 46.85^\circ \quad \cos(\varphi + 2\theta) = -0.593 \Rightarrow (\varphi + 2\theta) = \pm 126.35^\circ$$

- The **sign** (+/-) chosen for the **series line** equation imposes the **sign** used for the **shunt stub** equation

- **“+” solution** ↓

$$(46.85^\circ + 2\theta) = +126.35^\circ \quad \theta = +39.7^\circ \quad \text{Im } y_S = \frac{-2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}} = -1.472$$

$$\theta_{sp} = \tan^{-1}(\text{Im } y_S) = -55.8^\circ (+180^\circ) \rightarrow \theta_{sp} = 124.2^\circ$$

- **“-” solution** ↓

$$(46.85^\circ + 2\theta) = -126.35^\circ \quad \theta = -86.6^\circ (+180^\circ) \rightarrow \theta = 93.4^\circ$$

$$\text{Im } y_S = \frac{+2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}} = +1.472 \quad \theta_{sp} = \tan^{-1}(\text{Im } y_S) = 55.8^\circ$$

# Analytical solution, usage

$$(\varphi + 2\theta) = \begin{cases} +126.35^\circ \\ -126.35^\circ \end{cases} \quad \theta = \begin{cases} 39.7^\circ \\ 93.4^\circ \end{cases} \quad \text{Im}[y_s(\theta)] = \begin{cases} -1.472 \\ +1.472 \end{cases} \quad \theta_{sp} = \begin{cases} -55.8^\circ + 180^\circ = 124.2^\circ \\ +55.8^\circ \end{cases}$$

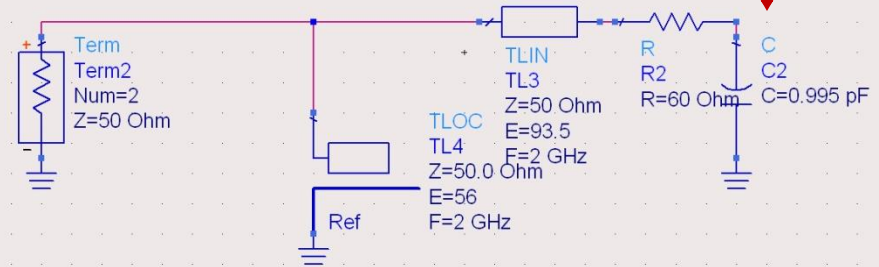
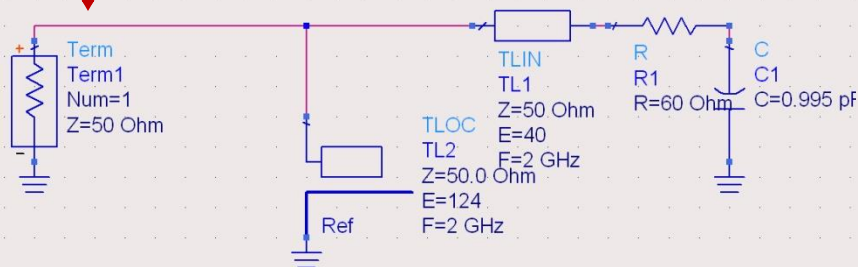
- We choose **one** of the two possible solutions
- The **sign** (+/-) chosen for the **series line** equation imposes the **sign** used for the **shunt stub** equation

$$l_1 = \frac{39.7^\circ}{360^\circ} \cdot \lambda = 0.110 \cdot \lambda$$

$$l_2 = \frac{124.2^\circ}{360^\circ} \cdot \lambda = 0.345 \cdot \lambda$$

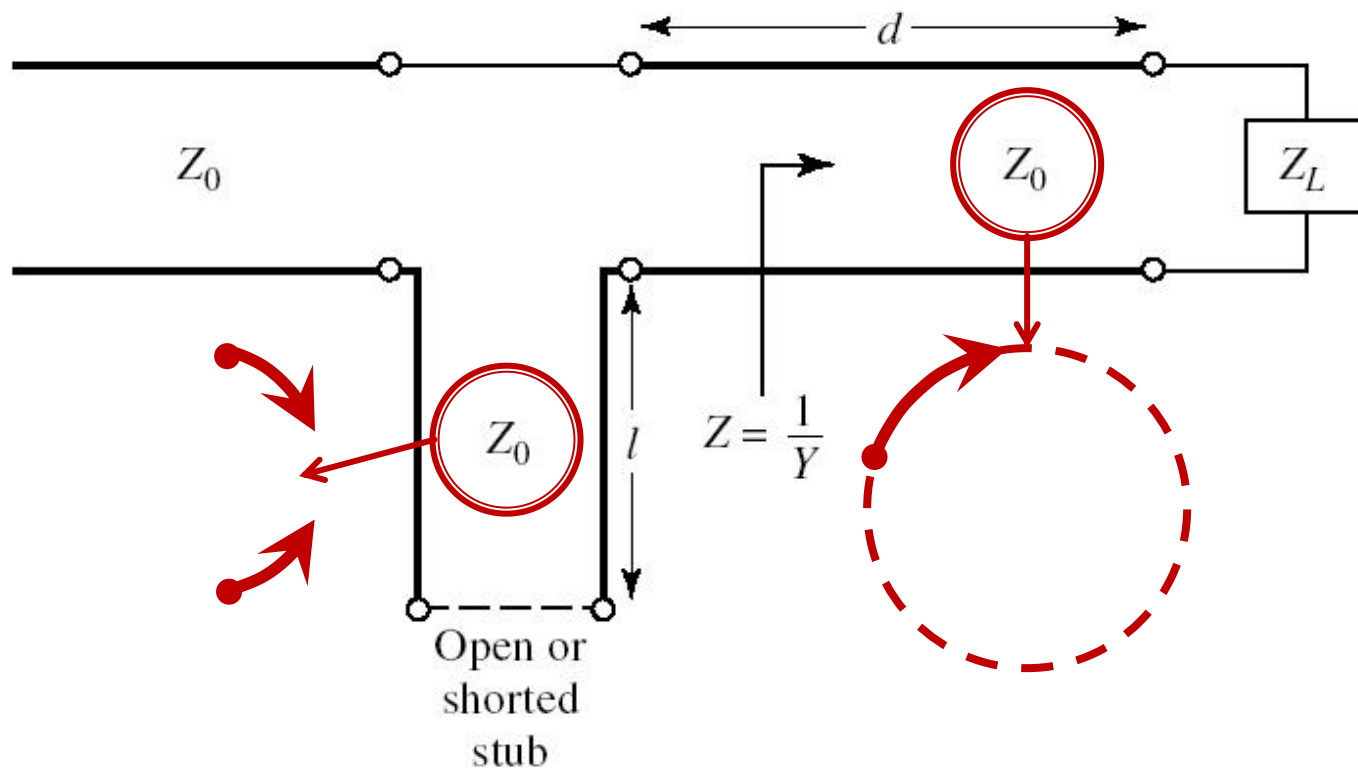
$$l_1 = \frac{93.4^\circ}{360^\circ} \cdot \lambda = 0.259 \cdot \lambda$$

$$l_2 = \frac{55.8^\circ}{360^\circ} \cdot \lambda = 0.155 \cdot \lambda$$

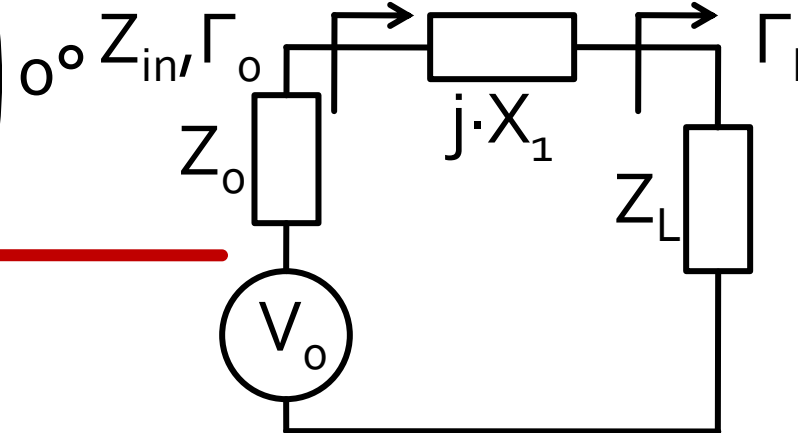
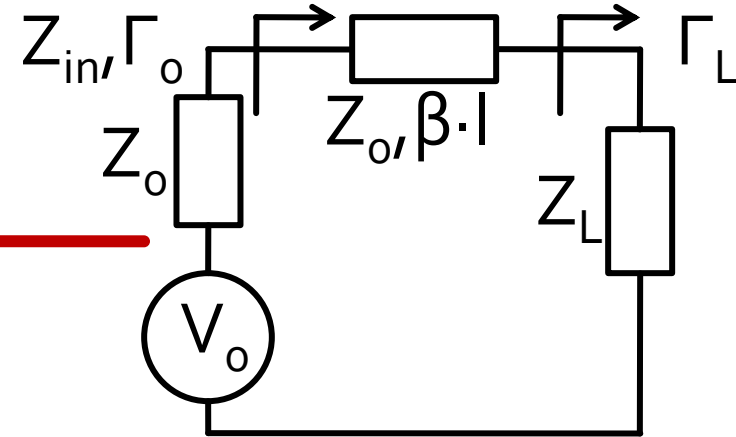
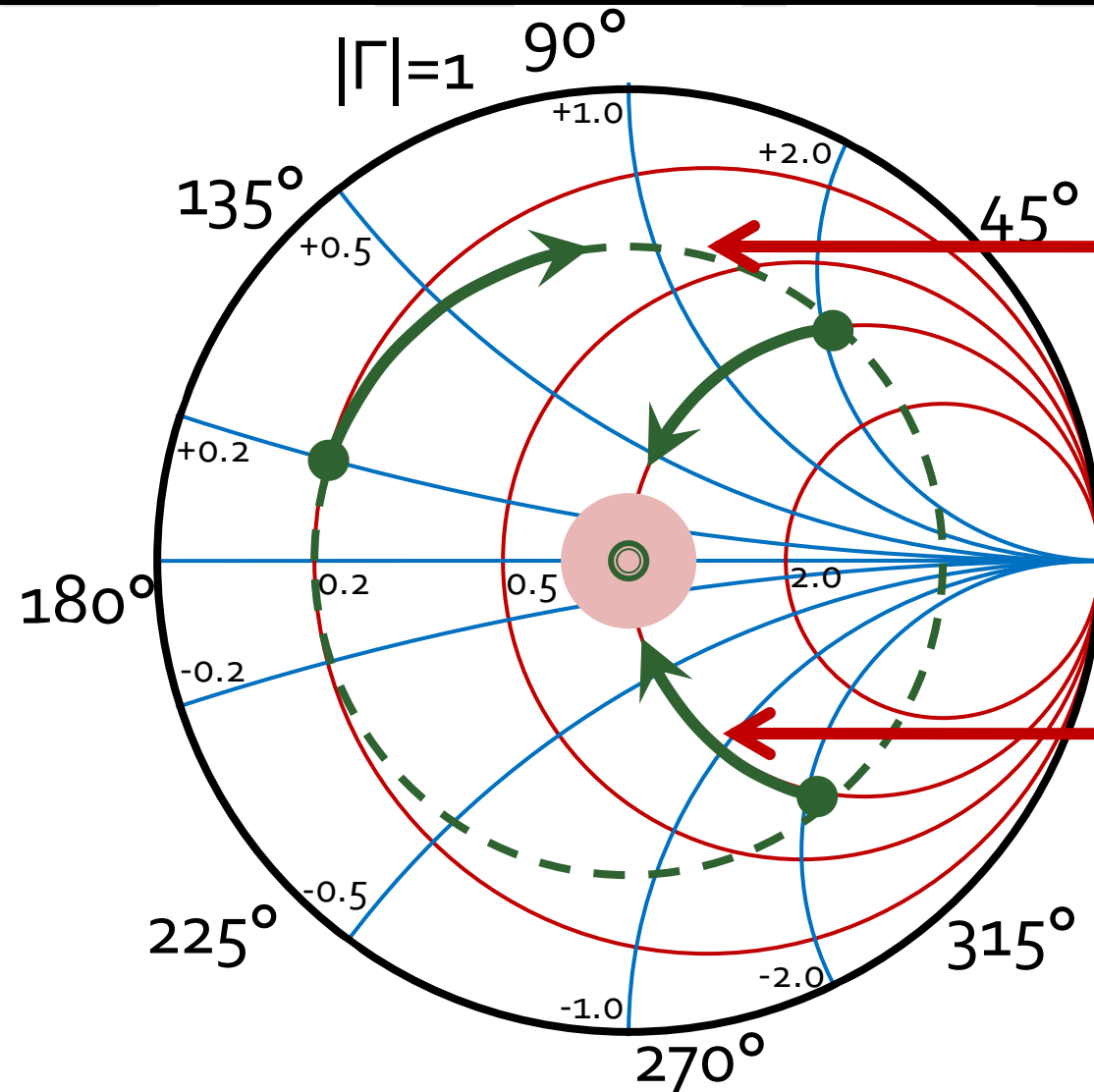


# Case 2, Series Stub

- Series Stub
- difficult to realize in single conductor line technologies (microstrip)



# Matching, series line + series reactance



$$|\Gamma_{in}| = |\Gamma_L|$$

$$r_{in} = 1$$

# Analytical solution, usage

$$\cos(\varphi + 2\theta) = |\Gamma_s|$$

$$\theta_{ss} = \beta \cdot l = \cot^{-1} \frac{\mp 2 \cdot |\Gamma_s|}{\sqrt{1 - |\Gamma_s|^2}}$$

$$\Gamma_s = 0.555 \angle -29.92^\circ$$

$$|\Gamma_s| = 0.555; \quad \varphi = -29.92^\circ \quad \cos(\varphi + 2\theta) = 0.555 \Rightarrow (\varphi + 2\theta) = \pm 56.28^\circ$$

- The **sign** (+/-) chosen for the **series line** equation imposes the **sign** used for the **series stub** equation

- **"+" solution** ↓

$$(-29.92^\circ + 2\theta) = +56.28^\circ \quad \theta = 43.1^\circ \quad \text{Im } z_s = \frac{+2 \cdot |\Gamma_s|}{\sqrt{1 - |\Gamma_s|^2}} = +1.335$$

$$\theta_{ss} = -\cot^{-1}(\text{Im } z_s) = -36.8^\circ (+180^\circ) \rightarrow \theta_{ss} = 143.2^\circ$$

- **"-" solution** ↓

$$(-29.92^\circ + 2\theta) = -56.28^\circ \quad \theta = -13.2^\circ (+180^\circ) \rightarrow \theta = 166.8^\circ$$

$$\text{Im } z_s = \frac{-2 \cdot |\Gamma_s|}{\sqrt{1 - |\Gamma_s|^2}} = -1.335 \quad \theta_{ss} = -\cot^{-1}(\text{Im } z_s) = 36.8^\circ$$

# Analytical solution, usage

$$(\varphi + 2\theta) = \begin{cases} +56.28^\circ \\ -56.28^\circ \end{cases} \quad \theta = \begin{cases} 43.1^\circ \\ 166.8^\circ \end{cases} \quad \text{Im}[z_s(\theta)] = \begin{cases} +1.335 \\ -1.335 \end{cases} \quad \theta_{ss} = \begin{cases} -36.8^\circ + 180^\circ = 143.2^\circ \\ +36.8^\circ \end{cases}$$

- We choose **one** of the two possible solutions
- The **sign** (+/-) chosen for the **series line** equation imposes the **sign** used for the **series stub** equation

$$l_1 = \frac{43.1^\circ}{360^\circ} \cdot \lambda = 0.120 \cdot \lambda$$

$$l_2 = \frac{143.2^\circ}{360^\circ} \cdot \lambda = 0.398 \cdot \lambda$$

$$l_1 = \frac{166.8^\circ}{360^\circ} \cdot \lambda = 0.463 \cdot \lambda$$

$$l_2 = \frac{36.8^\circ}{360^\circ} \cdot \lambda = 0.102 \cdot \lambda$$





# Stub, observations

- adding or subtracting **180°** ( $\lambda/2$ ) doesn't change the result (full rotation around the Smith Chart)

$$E = \beta \cdot l = \pi = 180^\circ \quad l = k \cdot \frac{\lambda}{2}, \forall k \in \mathbf{N}$$

- if the lines/stubs result with **negative** "length"/ "electrical length" we add  $\lambda/2$  /  $180^\circ$  to obtain physically realizable lines
- adding or subtracting **90°** ( $\lambda/4$ ) change the stub impedance:

$$Z_{in,sc} = j \cdot Z_0 \cdot \tan \beta \cdot l \quad \Leftrightarrow \quad Z_{in,g} = -j \cdot Z_0 \cdot \cot \beta \cdot l$$

- for the stub we can add or subtract  $90^\circ$  ( $\lambda/4$ ) while in the same time changing **open-circuit**  $\Leftrightarrow$  **short-circuit**

# Microwave Filters

---

# Filter synthesis

- Filter is designed with lumped elements (L/C) followed by implementation with distributed elements (transmission lines)
  - general
  - analytical relationships easy to implement on the computer
  - efficient
- The preferred procedure is **insertion loss method**

# Insertion loss method

$$P_{LR} = \frac{P_S}{P_L} = \frac{1}{1 - |\Gamma(\omega)|^2}$$

- $|\Gamma(\omega)|^2$  is an even function of  $\omega$

$$|\Gamma(\omega)|^2 = \frac{M(\omega^2)}{M(\omega^2) + N(\omega^2)}$$

$$P_{LR} = 1 + \frac{M(\omega^2)}{N(\omega^2)}$$

- Choosing M and N polynomials appropriately leads to a filter with a completely specified frequency response

# Insertion loss method

- We control the power loss ratio/attenuation introduced by the filter:
  - in the passband (pass all frequencies)
  - in the stopband (reject all frequencies)

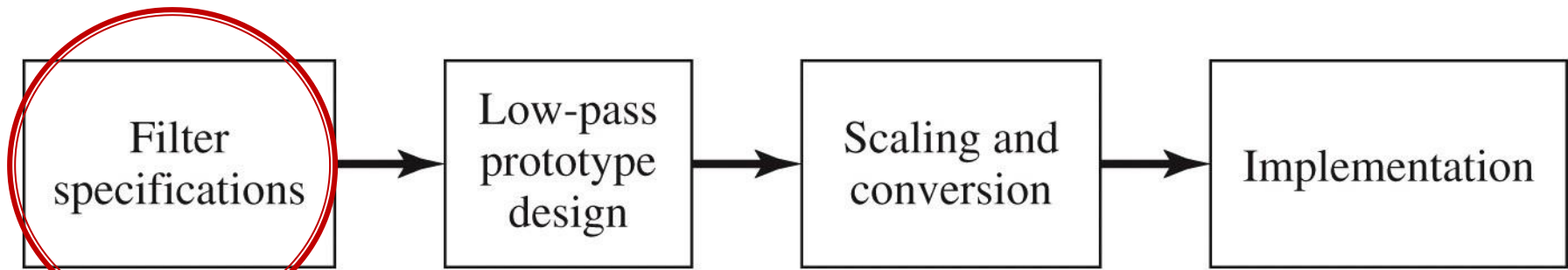
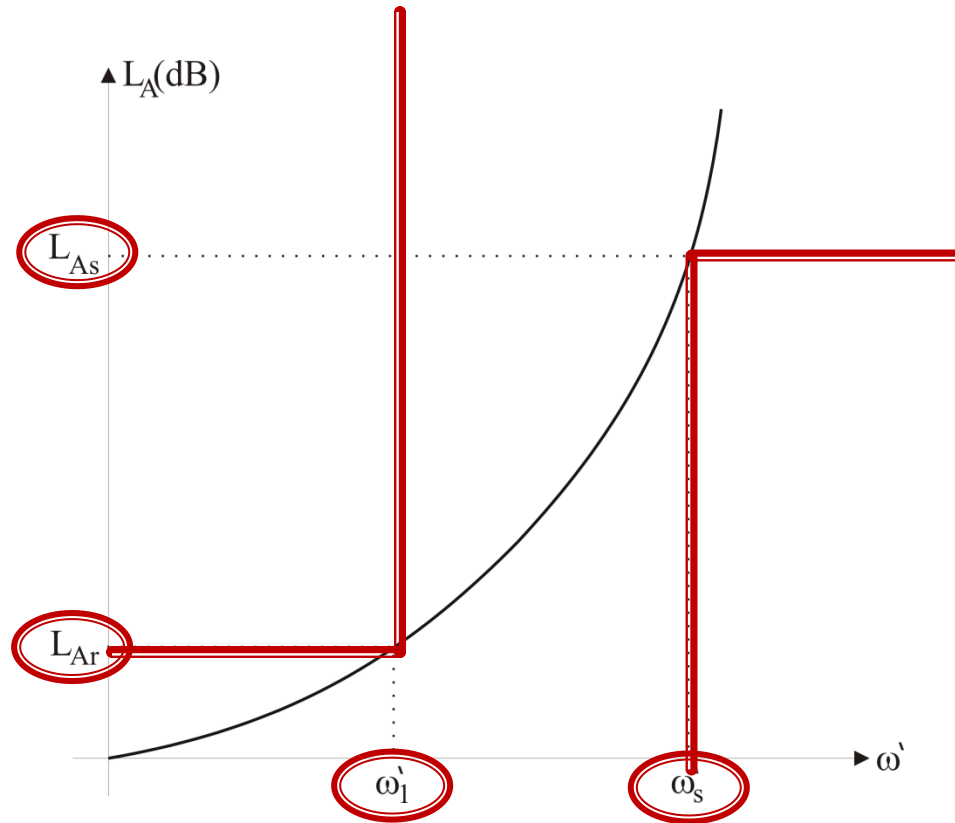


Figure 8.23

# Filter specifications

- Attenuation
  - in passband
  - in stopband
  - most often in **dB**
- Frequency range
  - passband
  - stopband
  - cutoff frequency  $\omega_1'$   
usually normalized  
(= **1**)



# Insertion loss method

- We choose the right polynomials to design an **low-pass** filter (prototype)
- The low-pass prototype are then converted to the desired other types of filters
  - low-pass, high-pass, bandpass, or bandstop

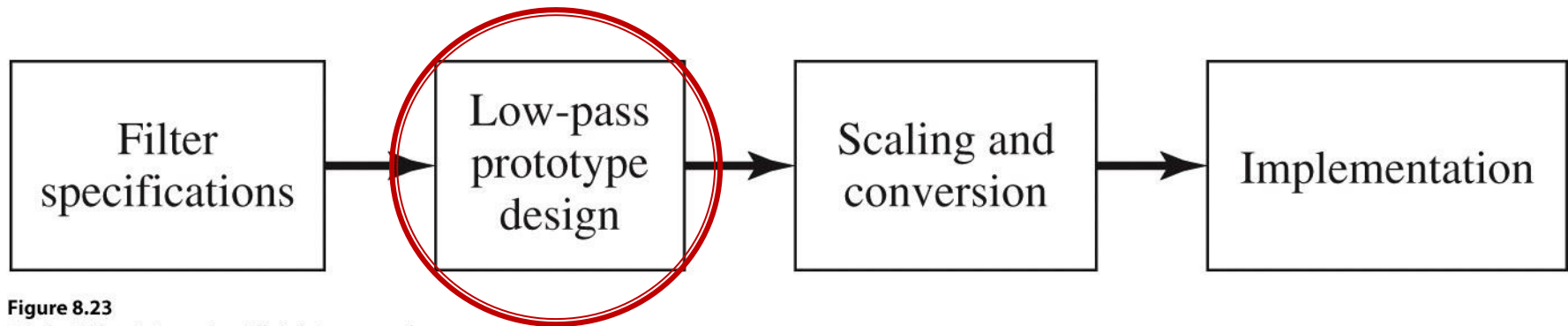


Figure 8.23

# Maximally Flat/Equal ripple LPF Prototype

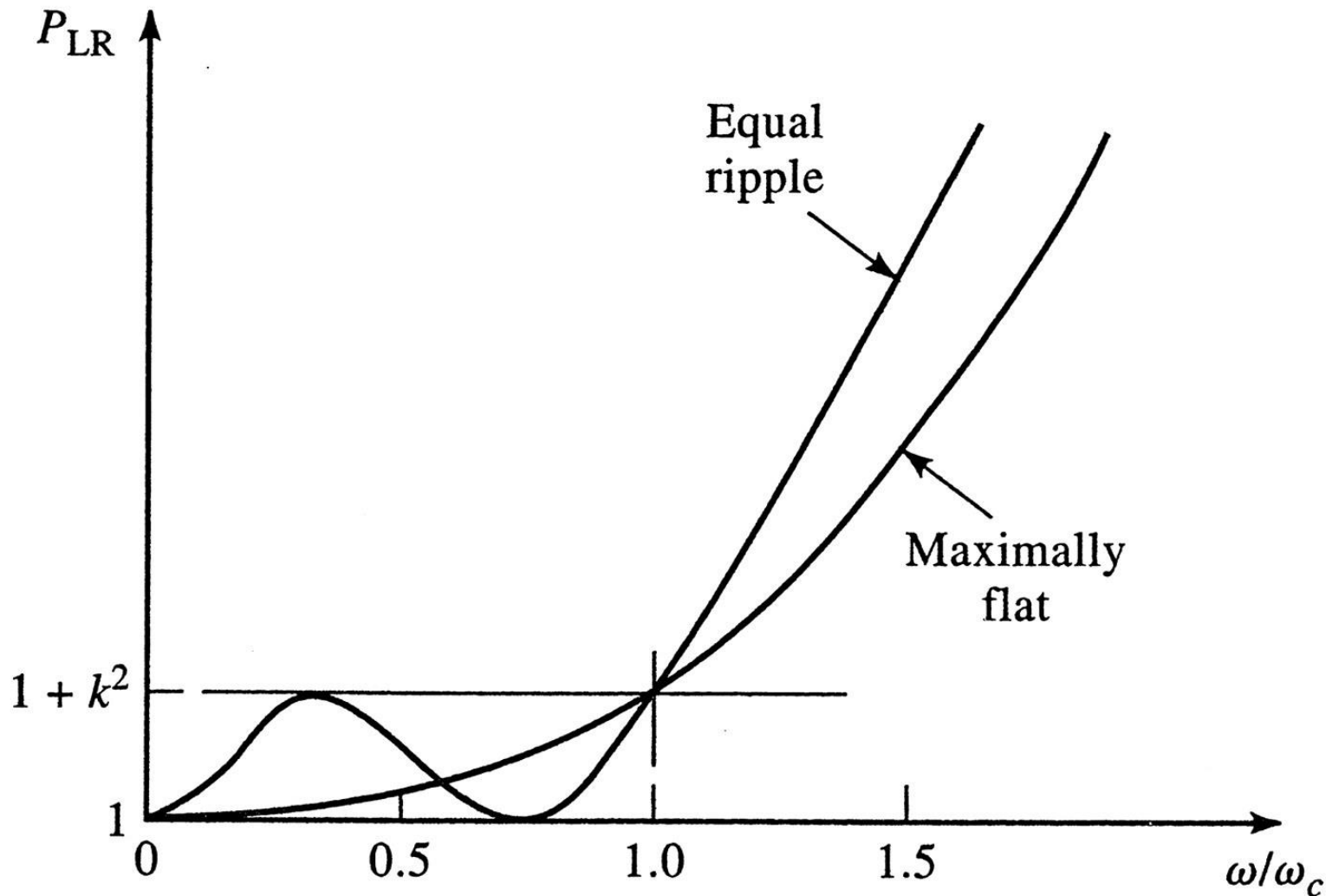
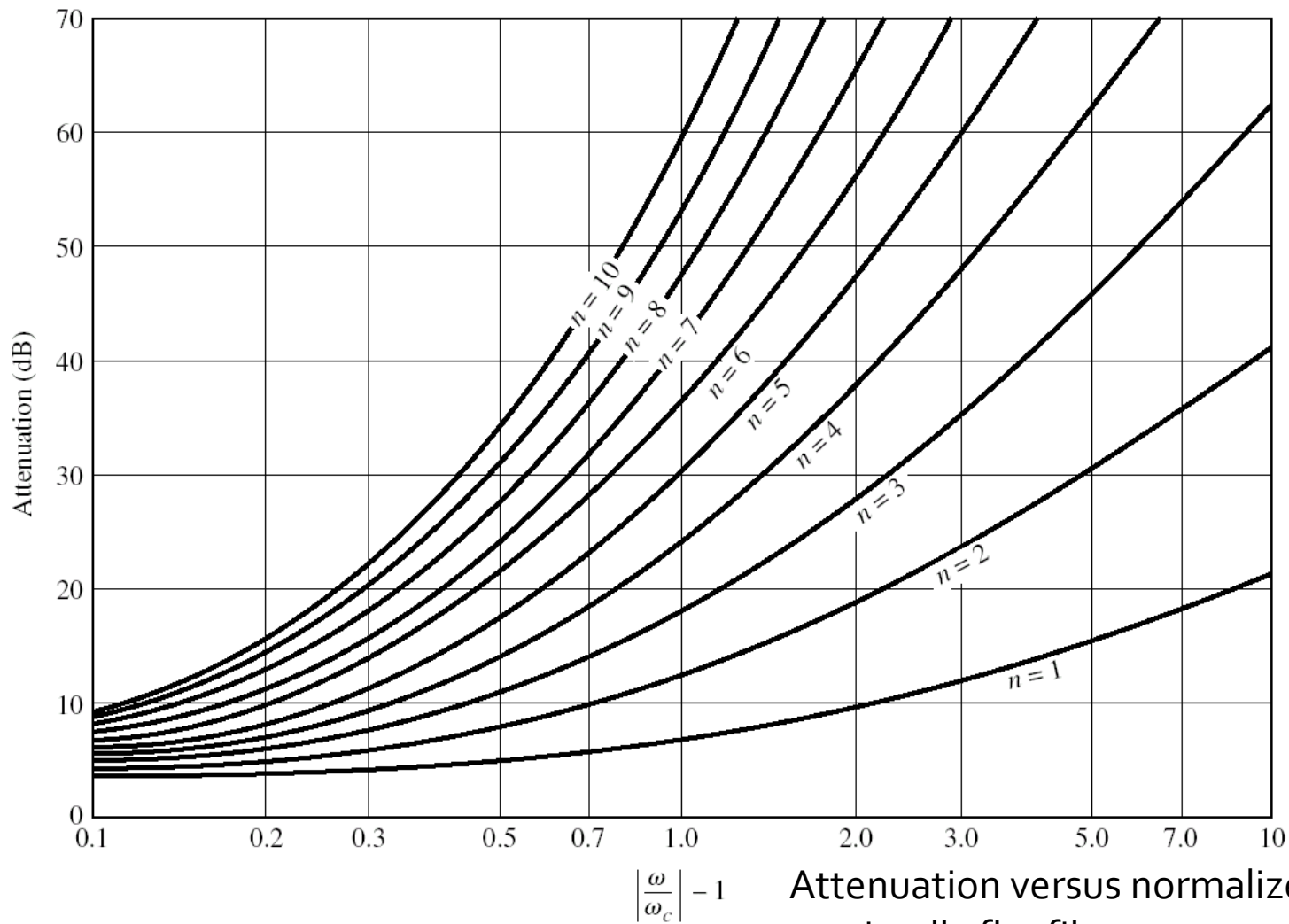


Figure 8.21  
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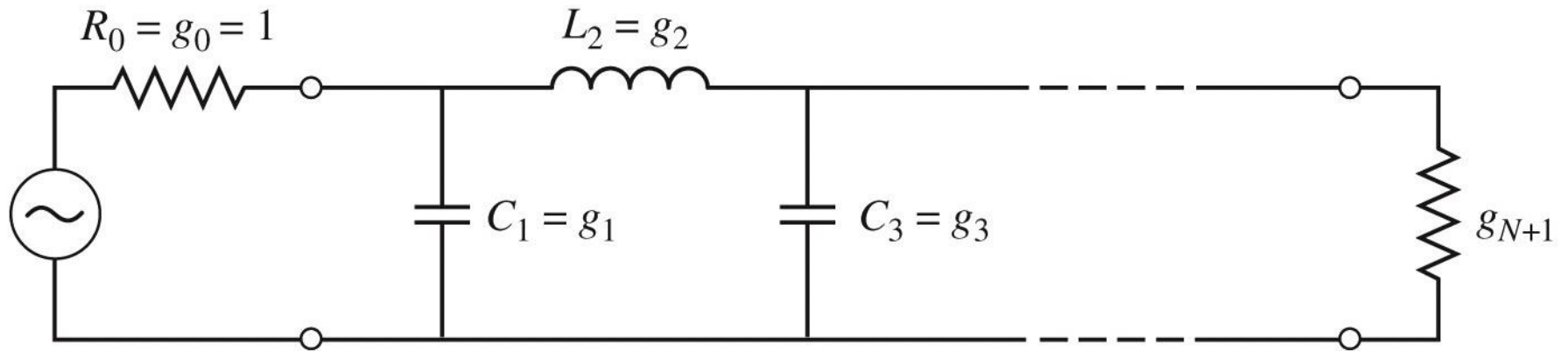


# Maximally flat filter prototypes

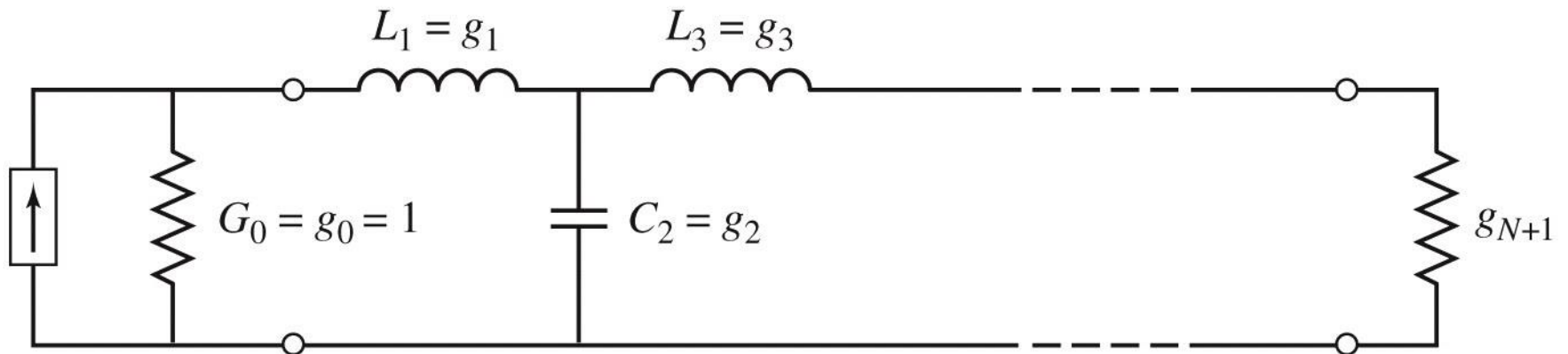


Attenuation versus normalized frequency for maximally flat filter prototypes

# Prototype Filters



(a)



(b)

# Maximally Flat LPF Prototype

- Formulas for filter parameters

$$g_0 = 1$$

$$g_k = 2 \cdot \sin \left[ \frac{(2 \cdot k - 1) \cdot \pi}{2 \cdot N} \right], \quad k = 1, N$$

$$g_{N+1} = 1$$

# Maximally Flat LPF Prototype

**TABLE 8.3** Element Values for Maximally Flat Low-Pass Filter Prototypes ( $g_0 = 1$ ,  $\omega_c = 1$ ,  $N = 1$  to 10)

| $N$ | $g_1$  | $g_2$  | $g_3$  | $g_4$  | $g_5$  | $g_6$  | $g_7$  | $g_8$  | $g_9$  | $g_{10}$ | $g_{11}$ |
|-----|--------|--------|--------|--------|--------|--------|--------|--------|--------|----------|----------|
| 1   | 2.0000 | 1.0000 |        |        |        |        |        |        |        |          |          |
| 2   | 1.4142 | 1.4142 | 1.0000 |        |        |        |        |        |        |          |          |
| 3   | 1.0000 | 2.0000 | 1.0000 | 1.0000 |        |        |        |        |        |          |          |
| 4   | 0.7654 | 1.8478 | 1.8478 | 0.7654 | 1.0000 |        |        |        |        |          |          |
| 5   | 0.6180 | 1.6180 | 2.0000 | 1.6180 | 0.6180 | 1.0000 |        |        |        |          |          |
| 6   | 0.5176 | 1.4142 | 1.9318 | 1.9318 | 1.4142 | 0.5176 | 1.0000 |        |        |          |          |
| 7   | 0.4450 | 1.2470 | 1.8019 | 2.0000 | 1.8019 | 1.2470 | 0.4450 | 1.0000 |        |          |          |
| 8   | 0.3902 | 1.1111 | 1.6629 | 1.9615 | 1.9615 | 1.6629 | 1.1111 | 0.3902 | 1.0000 |          |          |
| 9   | 0.3473 | 1.0000 | 1.5321 | 1.8794 | 2.0000 | 1.8794 | 1.5321 | 1.0000 | 0.3473 | 1.0000   |          |
| 10  | 0.3129 | 0.9080 | 1.4142 | 1.7820 | 1.9754 | 1.9754 | 1.7820 | 1.4142 | 0.9080 | 0.3129   | 1.0000   |

*Source:* Reprinted from G. L. Matthaei, L. Young, and E. M. T. Jones, *Microwave Filters, Impedance-Matching Networks, and Coupling Structures*, Artech House, Dedham, Mass., 1980, with permission.

# Impedance and Frequency Scaling

- After computing prototype filter's elements:
  - Low-Pass Filters (**LPF**)
  - cutoff frequency  **$\omega_o = 1 \text{ rad/s}$**  ( $f_o = 0.159 \text{ Hz}$ )
  - connected to a source with  **$R = 1\Omega$**
- component values can be scaled in terms of impedance and frequency

# Impedance and Frequency Scaling

- LPF Prototype is only used as an intermediate step
  - Low-Pass Filter (LPF)
  - cutoff frequency  $\omega_o = 1 \text{ rad/s}$  ( $f_o = 0.159 \text{ Hz}$ )
  - connected to a source with  $R = 1\Omega$

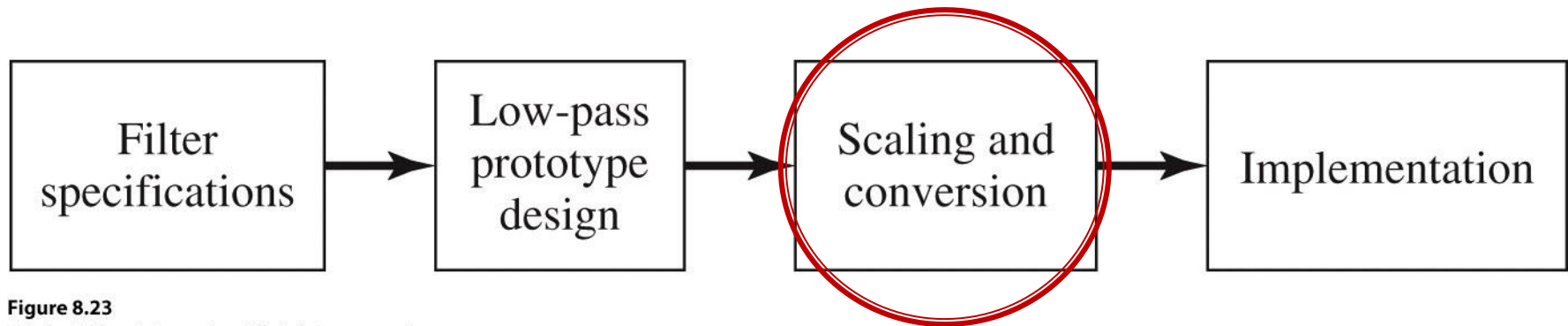


Figure 8.23

# Impedance Scaling

- To design a filter which will work with a source resistance of  $R_0$  we multiply all the impedances of the prototype design by  $R_0$  (" $'$ " denotes scaled values)

$$R'_s = R_0 \cdot (R_s = 1)$$

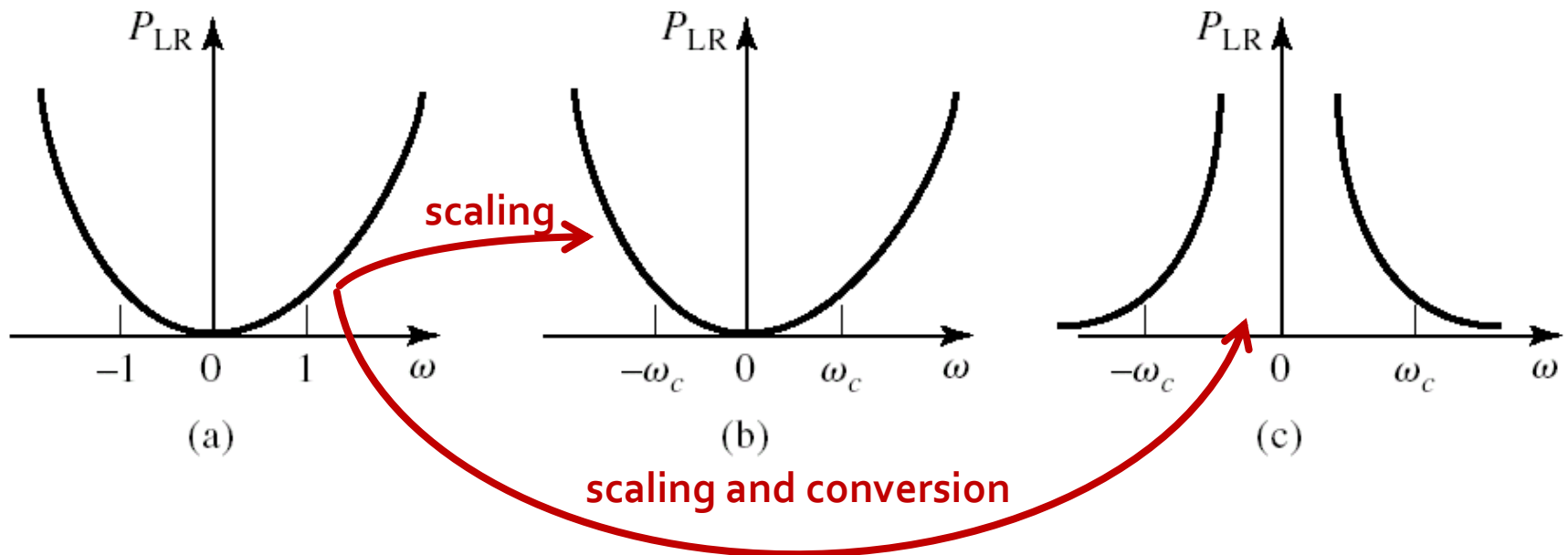
$$R'_L = R_0 \cdot R_L$$

$$L' = R_0 \cdot L$$

$$C' = \frac{C}{R_0}$$

# Frequency Scaling

- changing the cutoff frequency – (fig. b)
- changing the type (for example LPF  $\rightarrow$  HPF – fig. c) requires also conversion

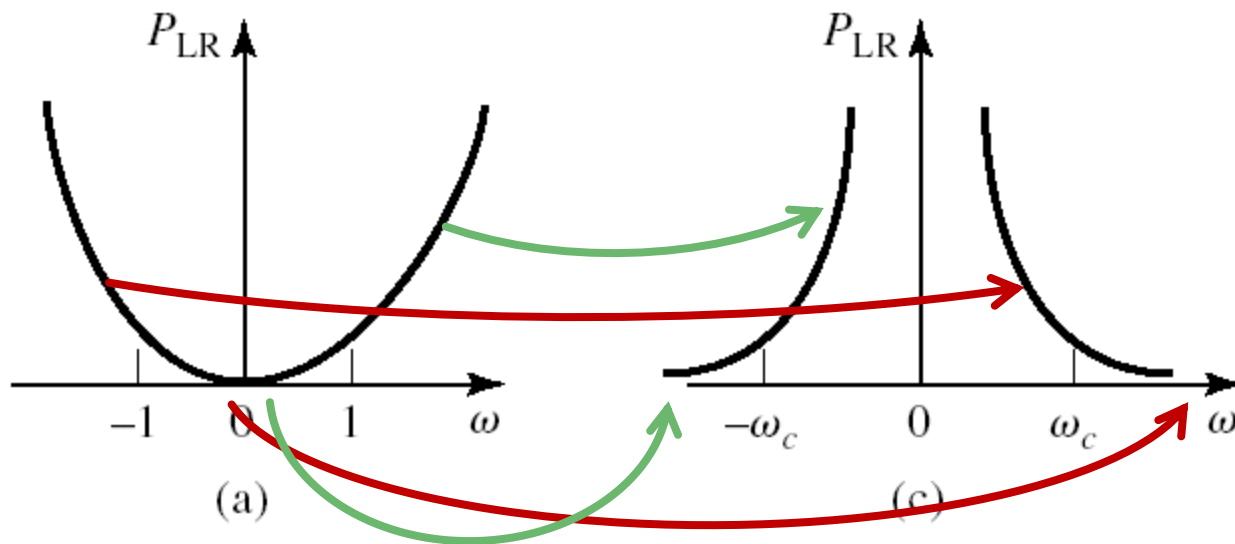




# Low-pass to high-pass transformation LPF $\rightarrow$ HPF

- Variable substitution for LPF  $\rightarrow$  HPF:

$$\omega \leftarrow -\frac{\omega_c}{\omega}$$



# High-pass transformation LPF $\rightarrow$ HPF

- Variable substitution for LPF  $\rightarrow$  HPF :

$$\omega \leftarrow -\frac{\omega_c}{\omega}$$
$$j \cdot X_k = -j \cdot \frac{\omega_c}{\omega} \cdot L_k = \frac{1}{j \cdot \omega \cdot C'_k} \quad j \cdot B_k = -j \cdot \frac{\omega_c}{\omega} \cdot C_k = \frac{1}{j \cdot \omega \cdot L'_k}$$

- Impedance scaling can be included

$$C'_k = \frac{1}{R_0 \cdot \omega_c \cdot L_k} \quad L'_k = \frac{R_0}{\omega_c \cdot C_k}$$

- In the schematic series **inductors** must be replaced with series **capacitors**, and shunt **capacitors** must be replaced with shunt **inductors**

# Summary of Prototype Filter Transformations


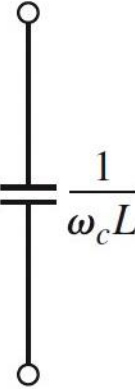
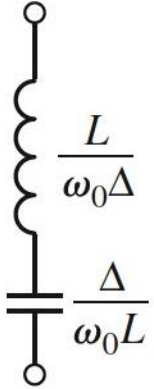
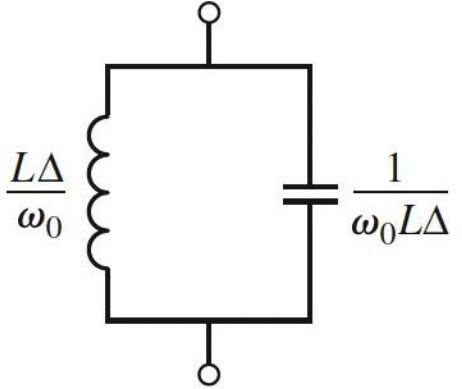
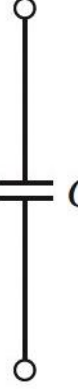
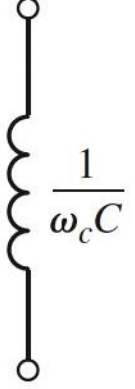
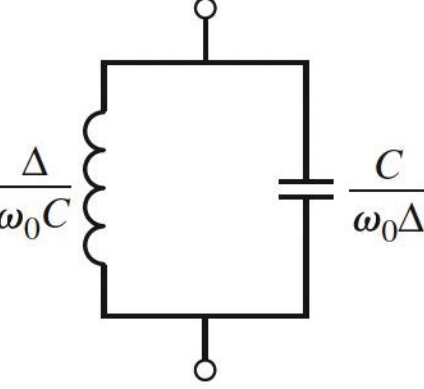
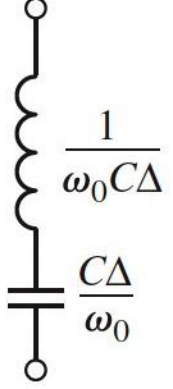
| Low-pass   | High-pass   | Bandpass  | Bandstop  |
|--|---|---|---|
|  <p style="text-align: center;"><math>L</math></p>  |  <p style="text-align: center;"><math>\frac{1}{\omega_c L}</math></p>  |  <p style="text-align: center;"><math>\frac{L}{\omega_0 \Delta}</math><br/><math>\frac{\Delta}{\omega_0 L}</math></p>   |  <p style="text-align: center;"><math>\frac{L\Delta}{\omega_0}</math>      <math>\frac{1}{\omega_0 L\Delta}</math></p> |
|  <p style="text-align: center;"><math>C</math></p> |  <p style="text-align: center;"><math>\frac{1}{\omega_c C}</math></p> |  <p style="text-align: center;"><math>\frac{\Delta}{\omega_0 C}</math>      <math>\frac{C}{\omega_0 \Delta}</math></p> |  <p style="text-align: center;"><math>\frac{1}{\omega_0 C\Delta}</math><br/><math>\frac{C\Delta}{\omega_0}</math></p> |

Table 8.6

# Example

- Design a 3rd order **bandpass** filter with 0.5 dB ripples in passband. The **center frequency** of the filter should be 1 GHz. The **fractional bandwidth** of the passband should be 10%, and the **impedance** 50Ω.

$$\omega_0 = 2 \cdot \pi \cdot 1 \text{ GHz} = 6.283 \cdot 10^9 \text{ rad / s}$$

$$\Delta = 0.1$$

# Bandpass Transformation / BPF

$$\omega_0 = 2 \cdot \pi \cdot 1 \text{GHz} = 6.283 \cdot 10^9 \text{ rad/s} \quad \Delta = \frac{\Delta\omega}{\omega_0} = \frac{\Delta f}{f_0} = 0.1 \quad R_0 = 50 \Omega$$

$$g_1 = 1.5963 = L_1,$$

$$g_3 = 1.5963 = L_3,$$

$$g_2 = 1.0967 = C_2,$$

$$g_4 = 1.000 = R_L$$

$$L'_1 = \frac{L_1 \cdot R_0}{\Delta \cdot \omega_0} = 127.0 \text{ nH}$$

$$C'_1 = \frac{\Delta}{\omega_0 \cdot L_1 \cdot R_0} = 0.199 \text{ pF}$$

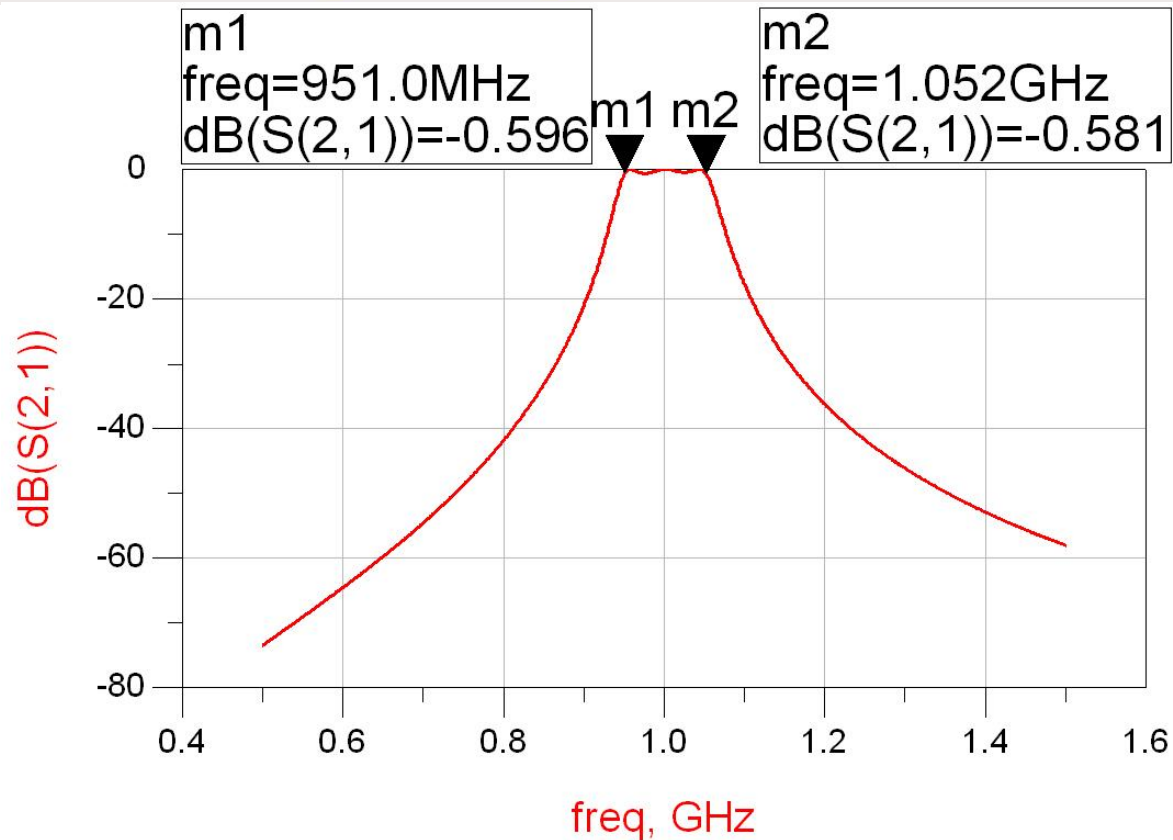
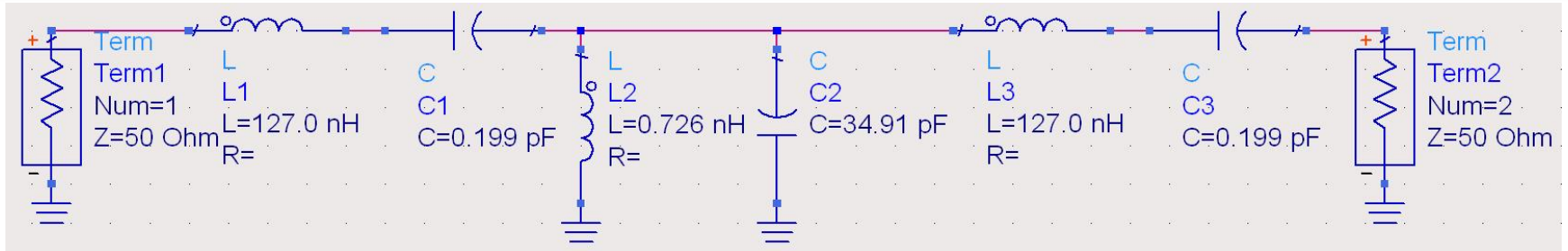
$$L'_2 = \frac{\Delta \cdot R_0}{\omega_0 \cdot C_2} = 0.726 \text{ nH}$$

$$C'_2 = \frac{C_2}{\Delta \cdot \omega_0 \cdot R_0} = 34.91 \text{ pF}$$

$$L'_3 = \frac{L_3 \cdot R_0}{\Delta \cdot \omega_0} = 127.0 \text{ nH}$$

$$C'_3 = \frac{\Delta}{\omega_0 \cdot L_3 \cdot R_0} = 0.199 \text{ pF}$$

# ADS



# Microwave Filters Implementation

# Microwave Filters Implementation

- The lumped-element (L, C) filter design generally works well **only** at low frequencies (RF):
  - lumped-element inductors and capacitors are generally available only for a limited range of values, and can be difficult to implement at microwave frequencies
  - difficulty to obtain the (very low) required tolerance for elements

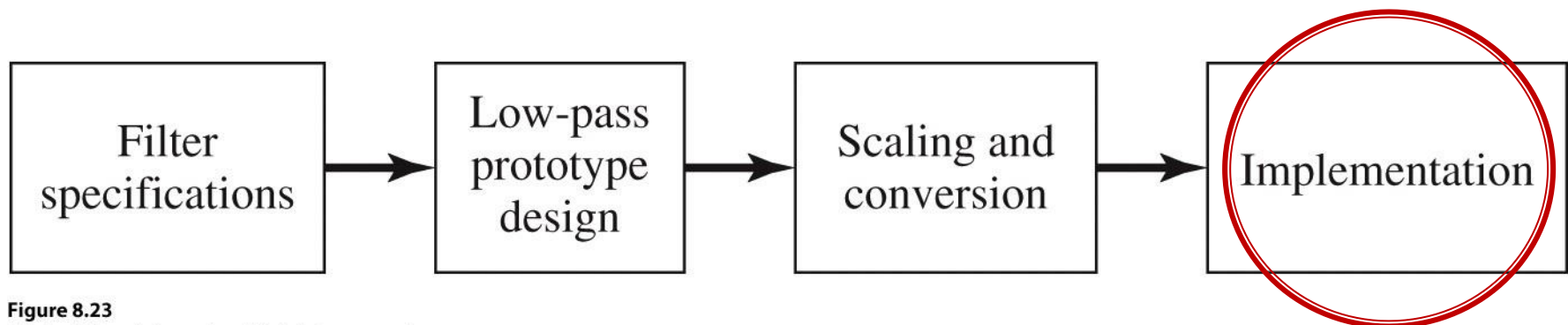


Figure 8.23



# Richards' Transformation

- Impedance seen at the input of a line loaded with  $Z_L$

$$Z_{in} = Z_0 \cdot \frac{Z_L + j \cdot Z_0 \cdot \tan \beta \cdot l}{Z_0 + j \cdot Z_L \cdot \tan \beta \cdot l}$$

- We prefer the load impedance to be:

- open circuit ( $Z_L = \infty$ )  $Z_{in,oc} = -j \cdot Z_0 \cdot \cot \beta \cdot l$

- short circuit ( $Z_L = 0$ )  $Z_{in,sc} = j \cdot Z_0 \cdot \tan \beta \cdot l$

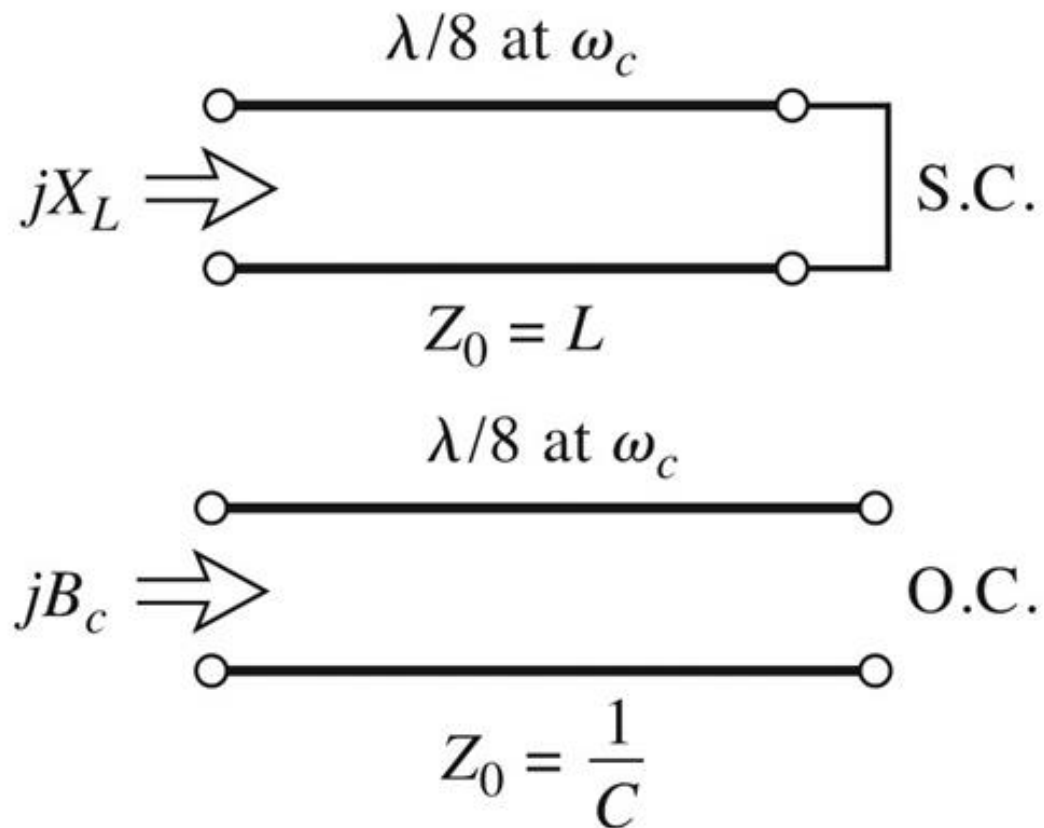
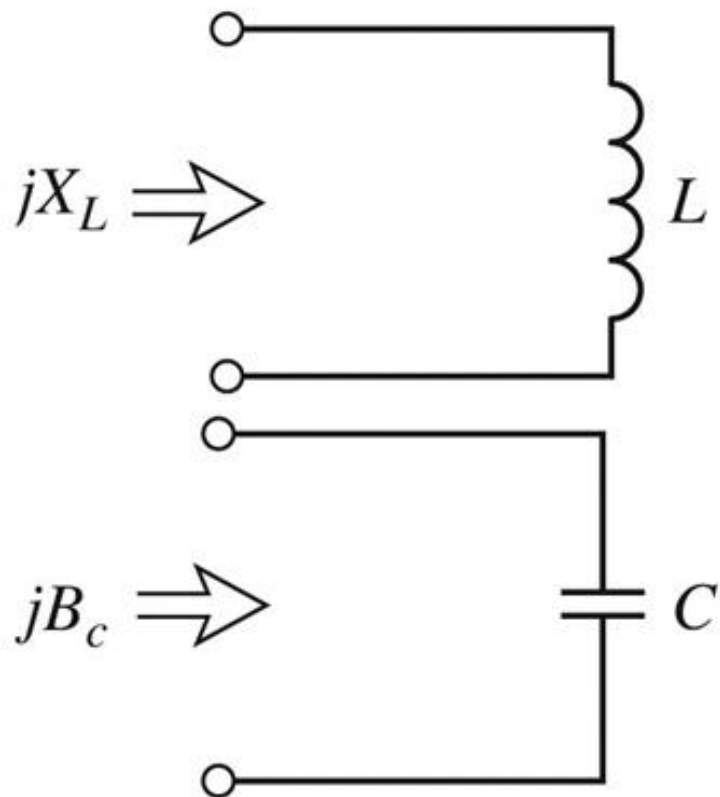
- Input impedance is:

- capacitive  $Z_{in,oc} = j \cdot X_C = \frac{1}{j \cdot B_C}$   $Z_0 \leftrightarrow \frac{1}{C}$   $\tan \beta \cdot l \leftrightarrow \omega$

- inductive  $Z_{in,sc} = j \cdot X_L$   $Z_0 \leftrightarrow L$   $\tan \beta \cdot l \leftrightarrow \omega$

# Richards' Transformation

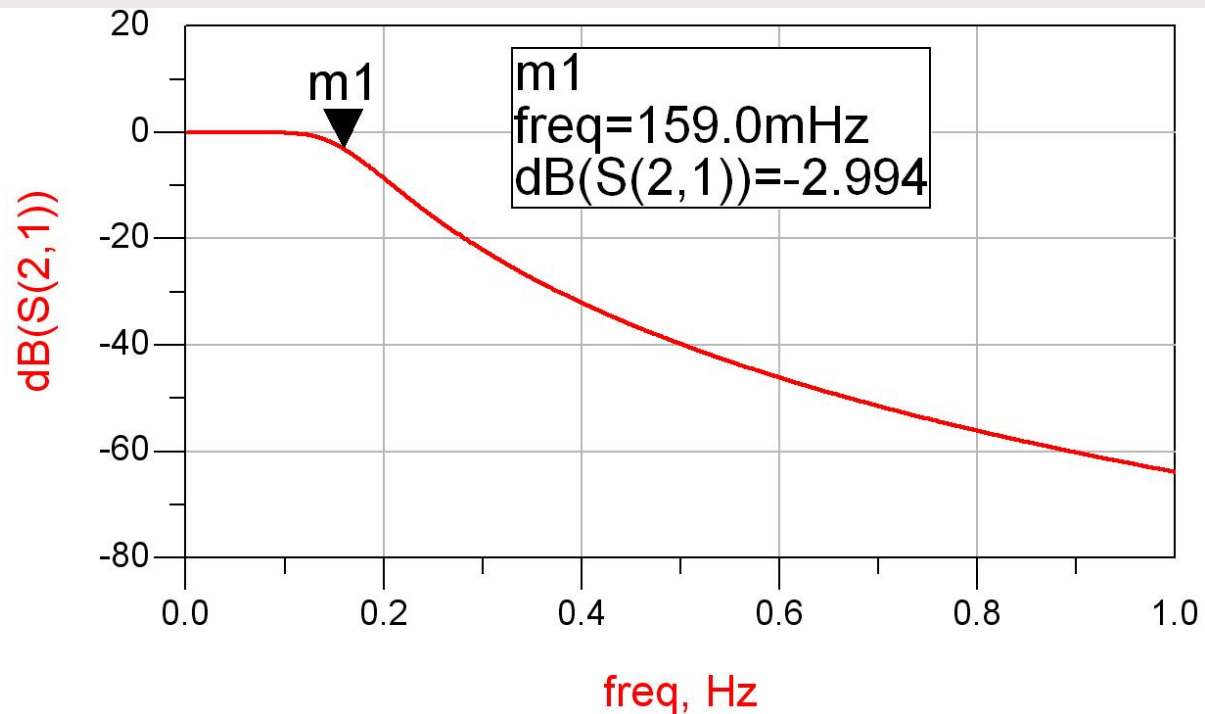
- allows implementation of the inductors and capacitors with lines **after** the transformation of the LPF prototype to the required type (LPF/HPF/BPF/BSF)



# Example

- Low-pass filter 4<sup>th</sup> order, 4 GHz cutoff frequency, maximally flat design (working with 50Ω source and load)
- maximally flat table or formulas:
  - $g_1 = 0.7654 = L_1$
  - $g_2 = 1.8478 = C_2$
  - $g_3 = 1.8478 = L_3$
  - $g_4 = 0.7654 = C_4$
  - $g_5 = 1$  (**does not** need supplemental impedance matching – required only for even order equal-ripple filters)

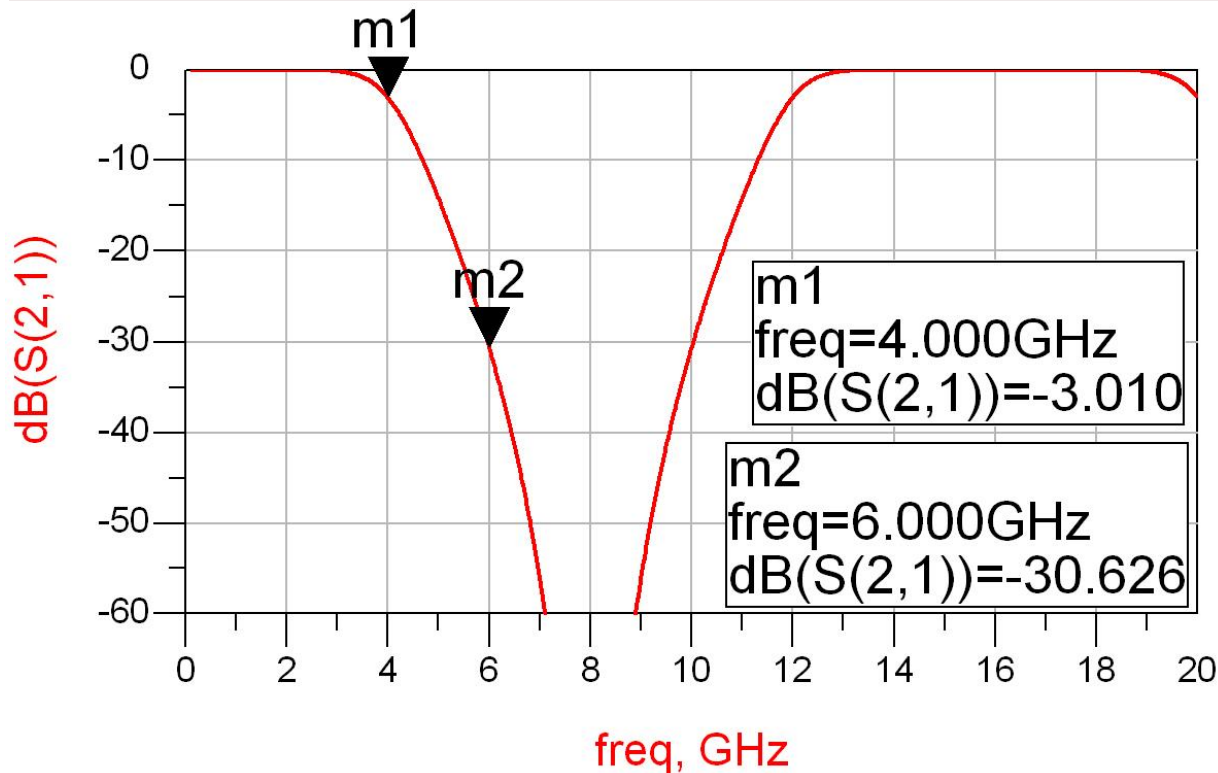
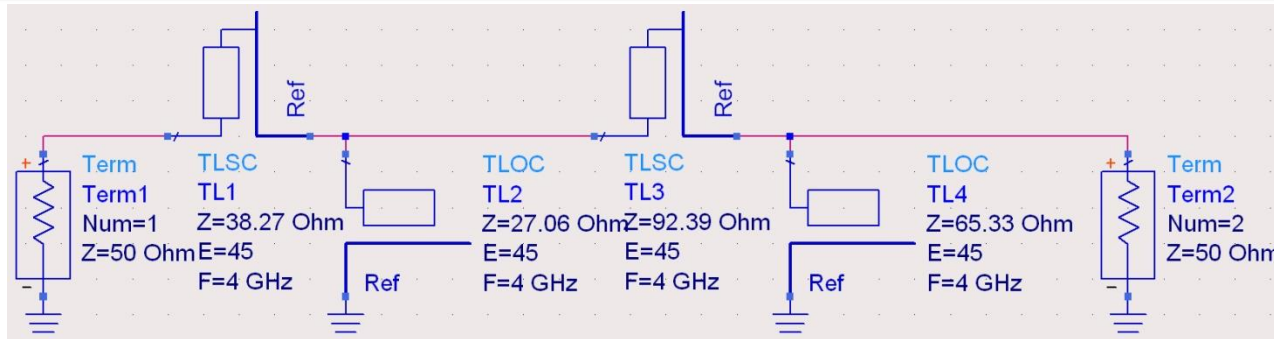
# LPF Prototype



# Richards' Transformation

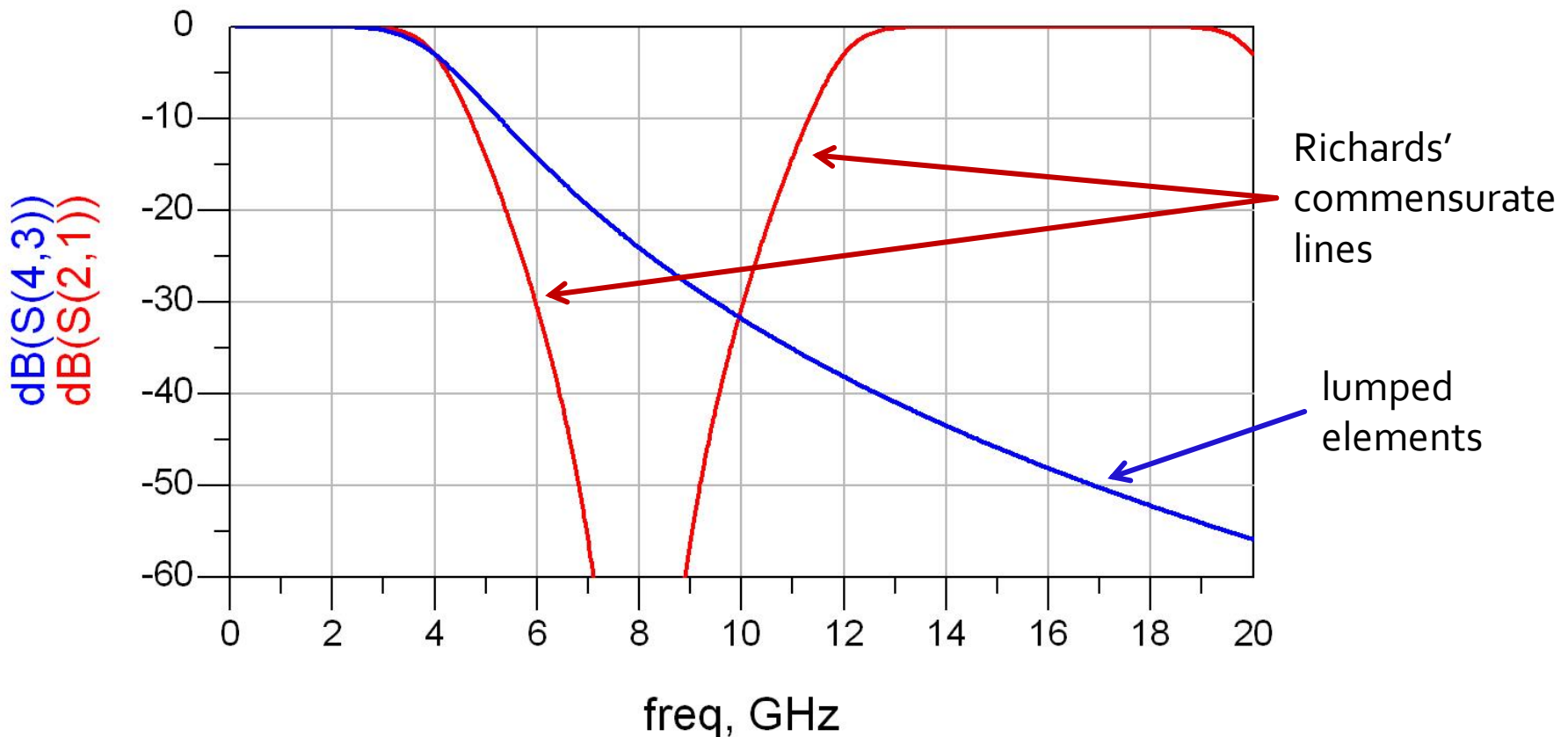
- LPF Prototype parameters:
  - $g_1 = 0.7654 = L_1$
  - $g_2 = 1.8478 = C_2$
  - $g_3 = 1.8478 = L_3$
  - $g_4 = 0.7654 = C_4$
- Normalized line impedances
  - $z_1 = 0.7654 = \text{series / short circuit}$   $Z_0 \leftrightarrow \frac{1}{C}$
  - $z_2 = 1 / 1.8478 = 0.5412 = \text{shunt / open circuit}$
  - $z_3 = 1.8478 = \text{series / short circuit}$   $Z_0 \leftrightarrow L$
  - $z_4 = 1 / 0.7654 = 1.3065 = \text{shunt / open circuit}$
- Impedance scaling by multiplying with  $Z_0 = 50\Omega$
- All lines must have the length equal to  $\lambda/8$  (electrical length  $E = 45^\circ$ ) at 4GHz

# Richards' Transformation – ADS



# Richards' Transformation

- Filters implemented with Richards' Transformation
  - beneficiate from the supplemental pole at  $2 \cdot \omega_c$
  - have the major disadvantage of frequency periodicity, a supplemental non-periodic LPF must be inserted if needed



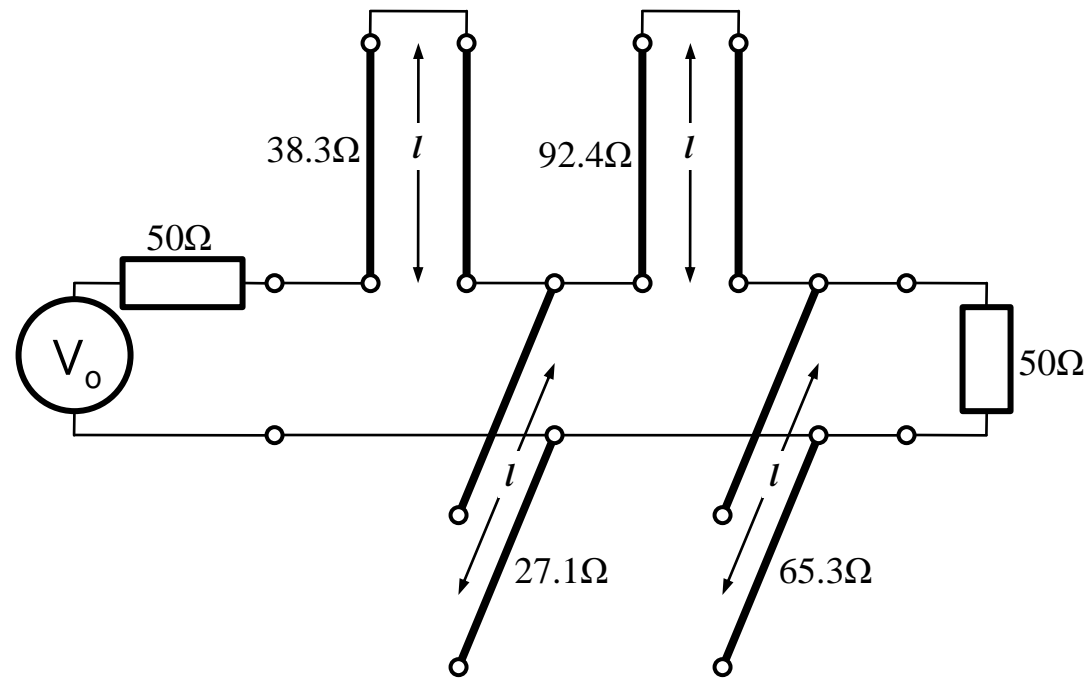
**Continue**

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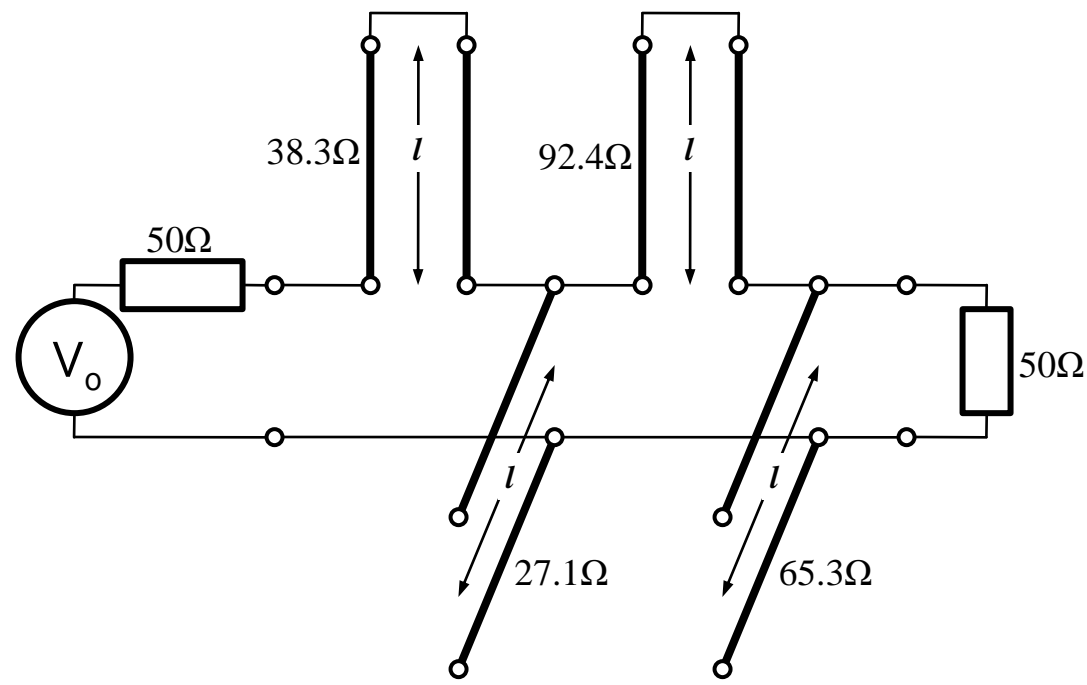
# Kuroda's Identities

- Filters implemented with the Richards' transformation have certain disadvantages in terms of practical use
- Kuroda's Identities/Transformations can eliminate some of these disadvantages
- We use additional line sections to obtain systems that are easier to implement in practice
- The additional line sections are called unit elements and have lengths of  $\lambda / 8$  at the desired cutoff frequency ( $\omega_c$ ) thus being commensurate with the stubs implementing the inductors and capacitors.



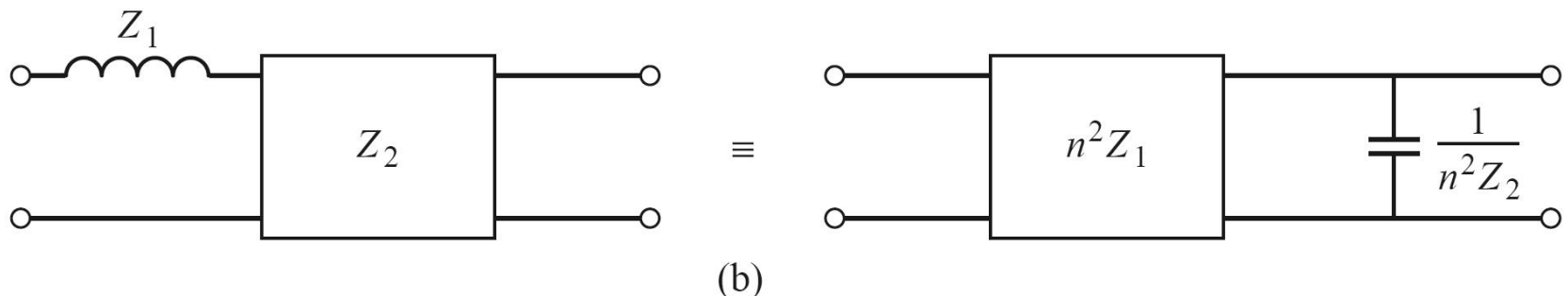
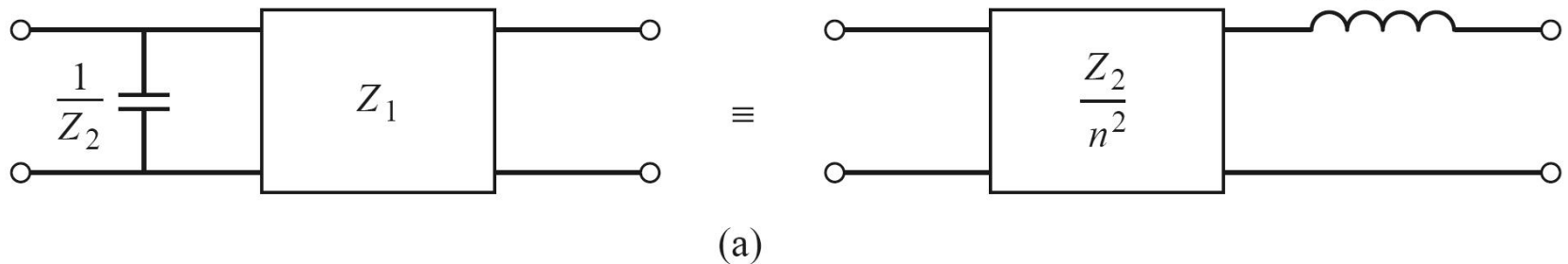
# Kuroda's Identities

- Kuroda's Identities perform any of the following operations:
  - Physically separate transmission line stubs
  - Transform series stubs into shunt stubs, or vice versa
  - Change impractical characteristic impedances into more realizable values ( $\sim 50\Omega$ )



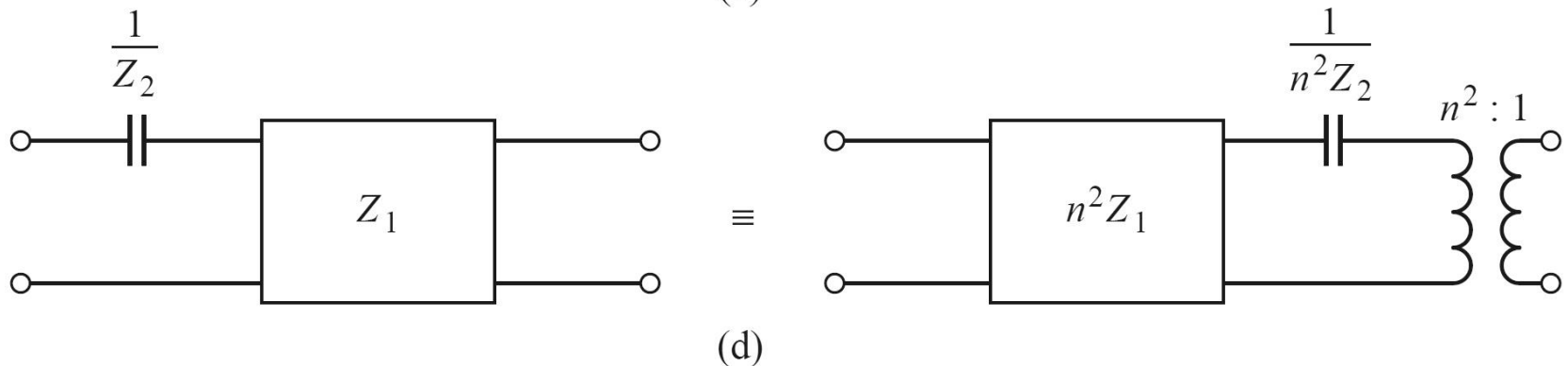
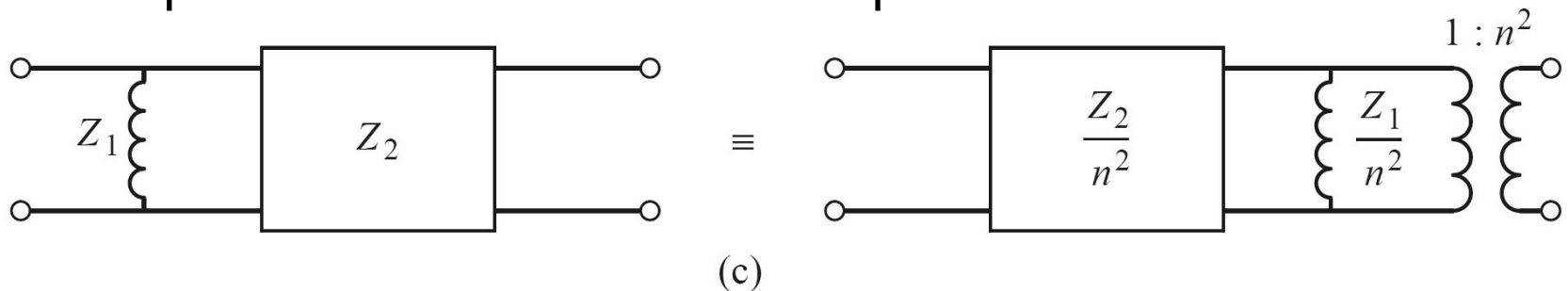
# Kuroda's Identities

- 4 circuit equivalents (a,b)
  - each box represents a unit element, or transmission line, of the indicated characteristic impedance and length ( $\lambda/8$  at  $\omega_c$ ). The inductors and capacitors represent short-circuit and open-circuit stubs  $\frac{Z_1}{n^2}$



# Kuroda's Identities

- 4 circuit equivalents (c,d)
  - each box represents a unit element, or transmission line, of the indicated characteristic impedance and length ( $\lambda/8$  at  $\omega_c$ ). The inductors and capacitors represent short-circuit and open-circuit stubs



# Kuroda's Identities

- In all Kuroda's Identities:

- n:

$$n^2 = 1 + \frac{Z_2}{Z_1}$$

- The inductors and capacitors represent short-circuit and open-circuit stubs resulted from Richards' transformation ( $\lambda/8$  at  $\omega_c$ ).
    - Each box represents a unit element, or transmission line, of the indicated characteristic impedance and length ( $\lambda/8$  at  $\omega_c$ ).

# First Kuroda's Identity

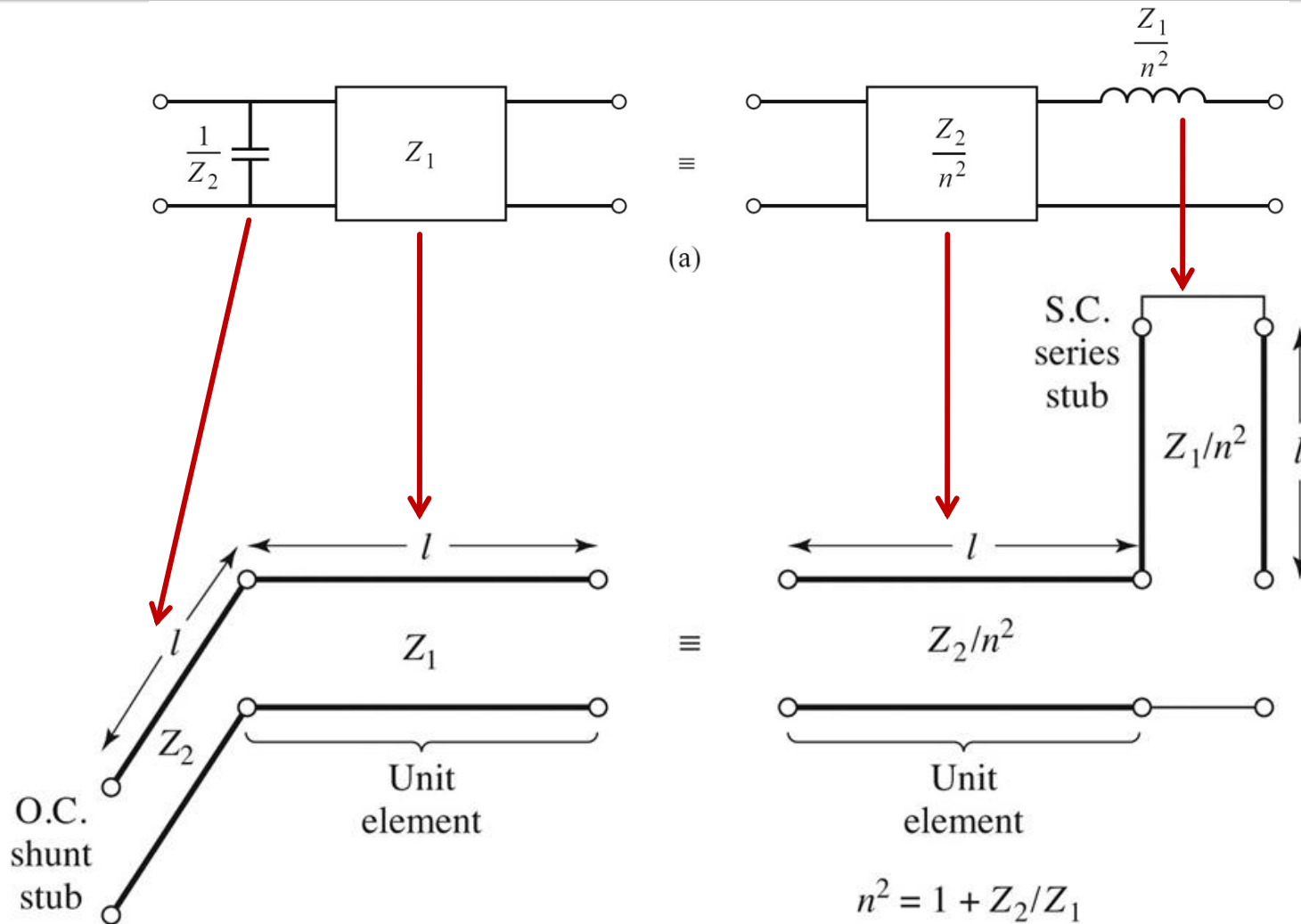
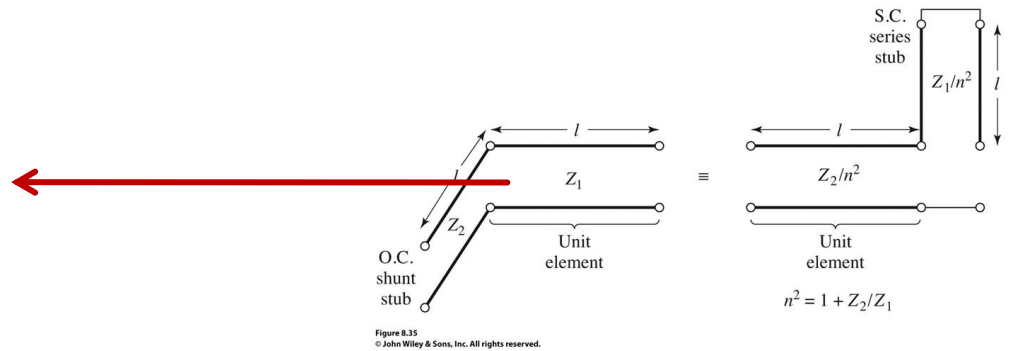
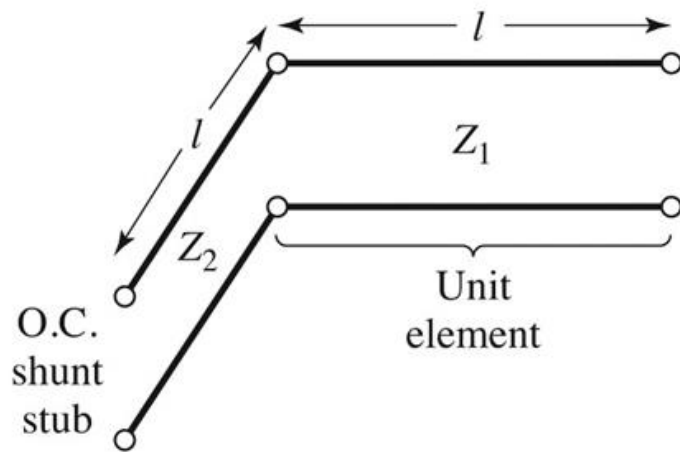
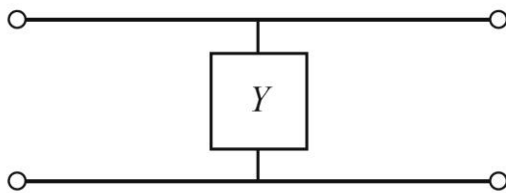


Figure 8.35  
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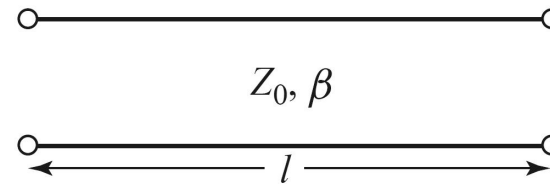
# First Kuroda's Identity – Proof



## ■ ABCD matrices, $L_4$



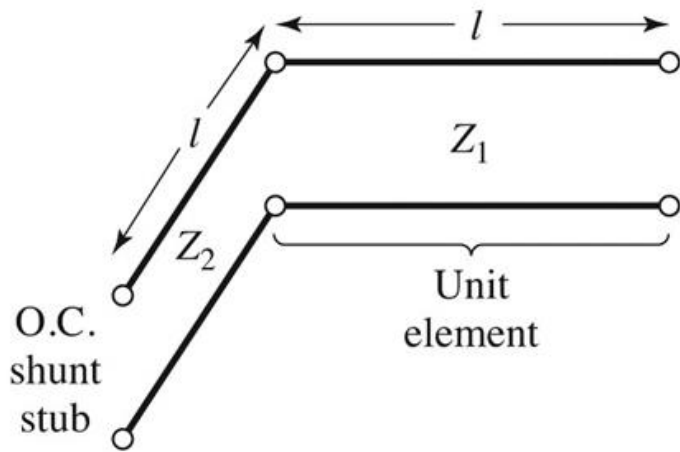
+



$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ Y & 1 \end{bmatrix}$$

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} \cos \beta \cdot l & j \cdot Z_0 \cdot \sin \beta \cdot l \\ j \cdot Y_0 \cdot \sin \beta \cdot l & \cos \beta \cdot l \end{bmatrix}$$

# First Kuroda's Identity – Proof



$$\Omega = \tan \beta \cdot l$$

$$\cos \beta \cdot l = \frac{1}{\sqrt{1 + \Omega^2}} \quad \sin \beta \cdot l = \frac{\Omega}{\sqrt{1 + \Omega^2}}$$

$$Z_{in,oc} = -j \cdot Z_2 \cdot \cot \beta \cdot l = -j \cdot \frac{Z_2}{\Omega}$$

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ j \cdot \Omega & 1 \\ Z_2 & 1 \end{bmatrix} \cdot \begin{bmatrix} \frac{1}{\sqrt{1 + \Omega^2}} & j \cdot Z_1 \cdot \frac{\Omega}{\sqrt{1 + \Omega^2}} \\ j \cdot \frac{1}{Z_1} \cdot \frac{\Omega}{\sqrt{1 + \Omega^2}} & \frac{1}{\sqrt{1 + \Omega^2}} \end{bmatrix}$$

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \frac{1}{\sqrt{1 + \Omega^2}} \cdot \begin{bmatrix} 1 & 0 \\ j \cdot \Omega & 1 \\ Z_2 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & j \cdot \Omega \cdot Z_1 \\ j \cdot \Omega & 1 \\ Z_1 & 1 \end{bmatrix} = \frac{1}{\sqrt{1 + \Omega^2}} \cdot \begin{bmatrix} 1 & j \cdot \Omega \cdot Z_1 \\ j \cdot \Omega \cdot \left( \frac{1}{Z_1} + \frac{1}{Z_2} \right) & 1 - \Omega^2 \cdot \frac{Z_1}{Z_2} \end{bmatrix}$$



# First Kuroda's Identity – Proof

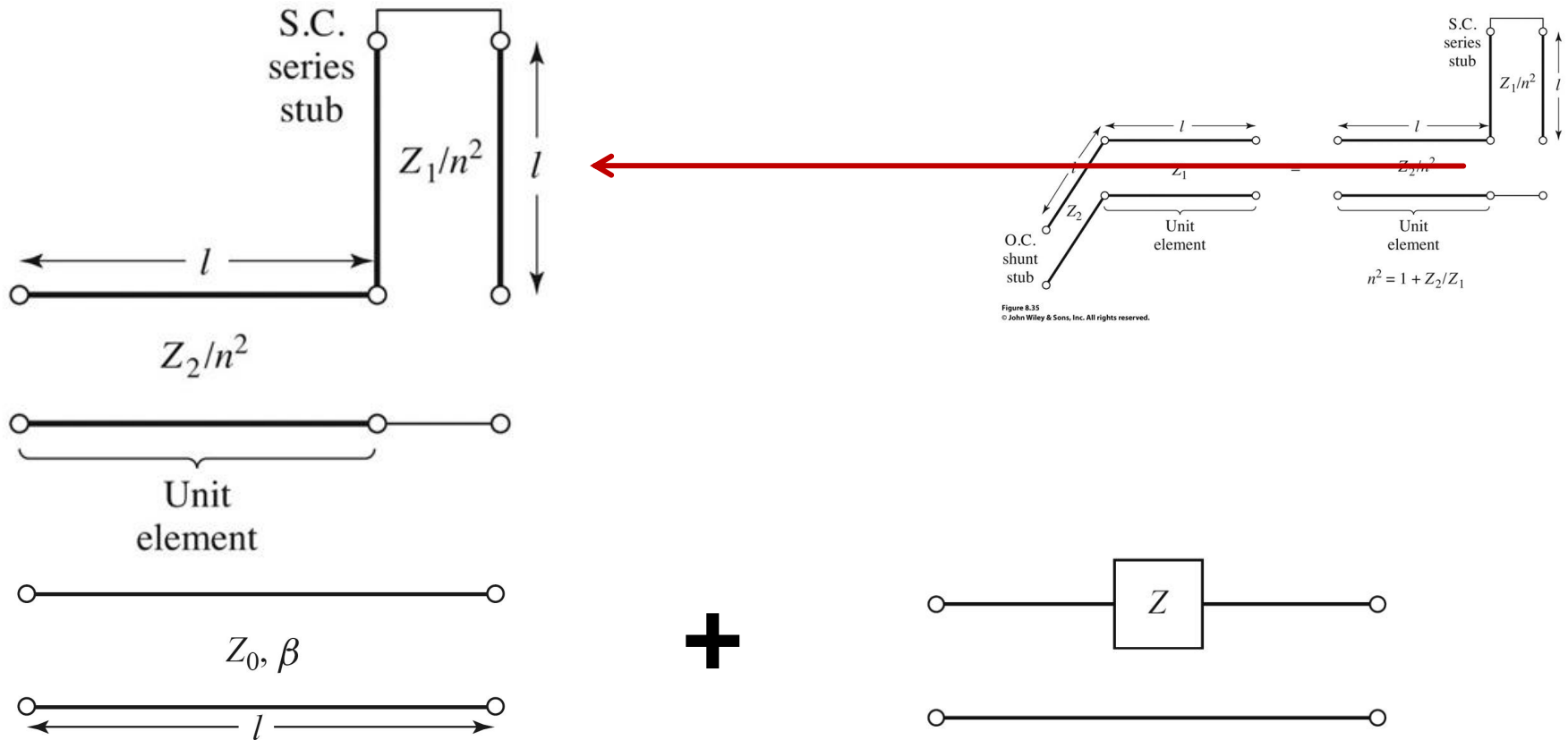
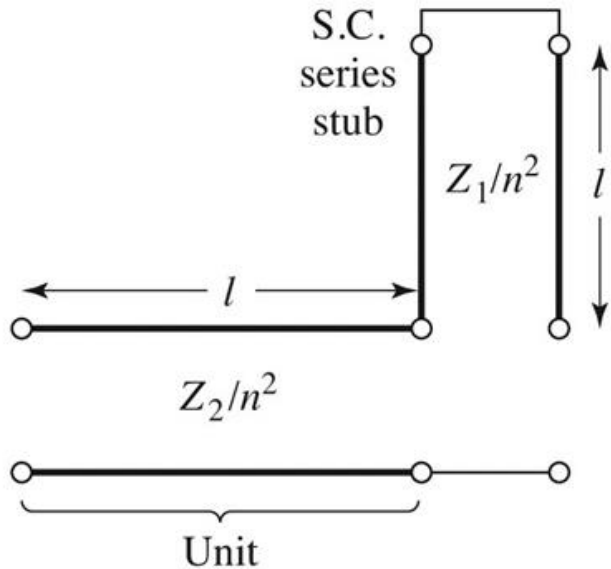


Figure 8.35  
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$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} \cos \beta \cdot l & j \cdot Z_0 \cdot \sin \beta \cdot l \\ j \cdot Y_0 \cdot \sin \beta \cdot l & \cos \beta \cdot l \end{bmatrix}$$

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} 1 & Z \\ 0 & 1 \end{bmatrix}$$

# First Kuroda's Identity – Proof



$$\Omega = \tan \beta \cdot l$$

$$\cos \beta \cdot l = \frac{1}{\sqrt{1 + \Omega^2}} \quad \sin \beta \cdot l = \frac{\Omega}{\sqrt{1 + \Omega^2}}$$

$$Z_{in,sc} = j \cdot \left( \frac{Z_1}{n^2} \right) \cdot \tan \beta \cdot l = \frac{j \cdot \Omega \cdot Z_1}{n^2}$$

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} \frac{1}{\sqrt{1 + \Omega^2}} & j \cdot \frac{Z_2}{n^2} \cdot \frac{\Omega}{\sqrt{1 + \Omega^2}} \\ j \cdot \frac{n^2}{Z_2} \cdot \frac{\Omega}{\sqrt{1 + \Omega^2}} & \frac{1}{\sqrt{1 + \Omega^2}} \end{bmatrix} \cdot \begin{bmatrix} 1 & \frac{j \cdot \Omega \cdot Z_1}{n^2} \\ 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \frac{1}{\sqrt{1 + \Omega^2}} \cdot \begin{bmatrix} 1 & j \cdot \Omega \cdot \frac{Z_2}{n^2} \\ \frac{j \cdot \Omega \cdot n^2}{Z_2} & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & j \cdot \Omega \cdot \frac{Z_1}{n^2} \\ 0 & 1 \end{bmatrix} = \frac{1}{\sqrt{1 + \Omega^2}} \cdot \begin{bmatrix} 1 & j \cdot \frac{\Omega}{n^2} \cdot (Z_1 + Z_2) \\ \frac{j \cdot \Omega \cdot n^2}{Z_2} & 1 - \Omega^2 \cdot \frac{Z_1}{Z_2} \end{bmatrix}$$

# First Kuroda's Identity – Proof

- First circuit

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \frac{1}{\sqrt{1 + \Omega^2}} \cdot \begin{bmatrix} 1 & j \cdot \Omega \cdot Z_1 \\ j \cdot \Omega \cdot \left( \frac{1}{Z_1} + \frac{1}{Z_2} \right) & 1 - \Omega^2 \cdot \frac{Z_1}{Z_2} \end{bmatrix}$$

- Second circuit

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \frac{1}{\sqrt{1 + \Omega^2}} \cdot \begin{bmatrix} 1 & j \cdot \frac{\Omega}{n^2} \cdot (Z_1 + Z_2) \\ \frac{j \cdot \Omega \cdot n^2}{Z_2} & 1 - \Omega^2 \cdot \frac{Z_1}{Z_2} \end{bmatrix}$$

- Results are identical if we choose

$$n^2 = 1 + \frac{Z_2}{Z_1}$$

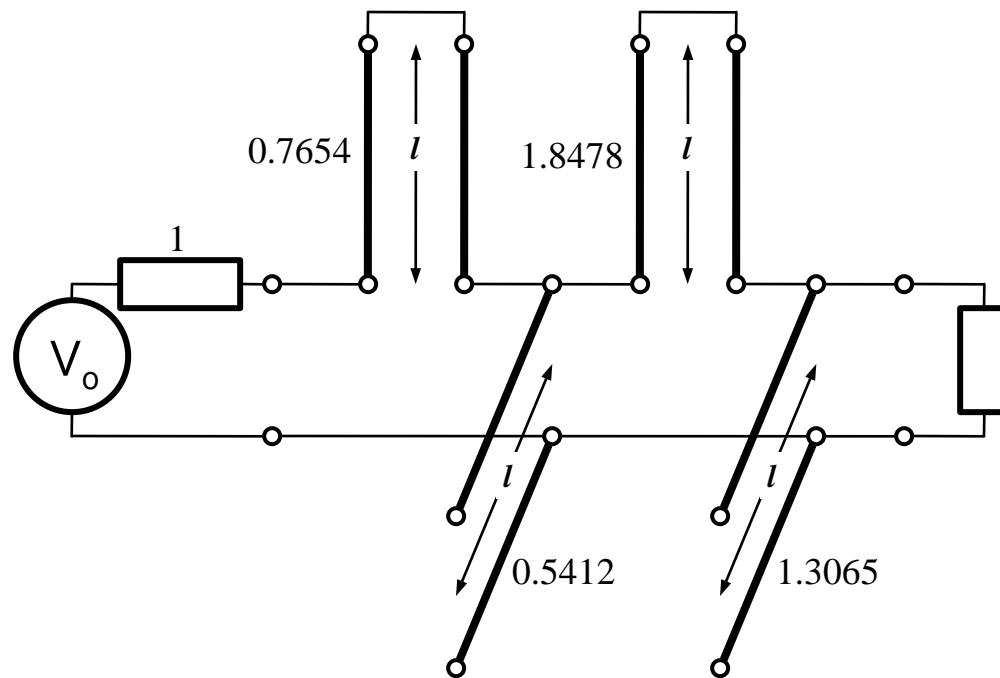
- The other 3 identities can be proved in the same way

# (Same) Example

- Low-pass filter 4<sup>th</sup> order, 4 GHz cutoff frequency, maximally flat design (working with 50Ω source and load)
- maximally flat table or formulas:
  - $g_1 = 0.7654 = L_1$
  - $g_2 = 1.8478 = C_2$
  - $g_3 = 1.8478 = L_3$
  - $g_4 = 0.7654 = C_4$
  - $g_5 = 1$  (**does not** need supplemental impedance matching – required only for even order equal-ripple filters)

# Example

- Apply Richards's transformation

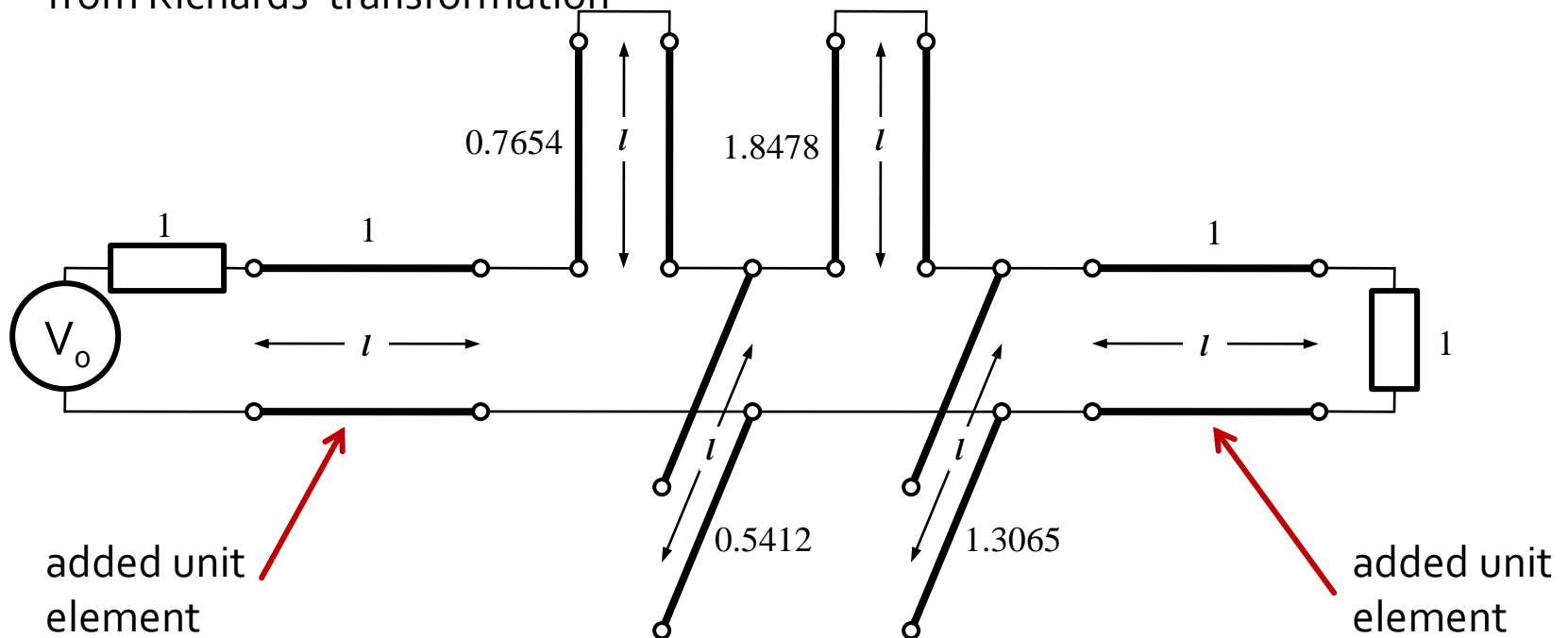


- Problems:

- the series stubs would be **very difficult** to implement in microstrip line form
- in microstrip technology it is preferable to have open-circuit stubs (short-circuit requires a **via-hole** to the ground plane)
- the 4 stubs are physically connected at the same point, an implementation that eliminates/reduces the **coupling** between these lines is impossible
- not the case here, but sometimes the normalized impedances are much different from 1. Most circuit technologies are designed for 50 $\Omega$  lines

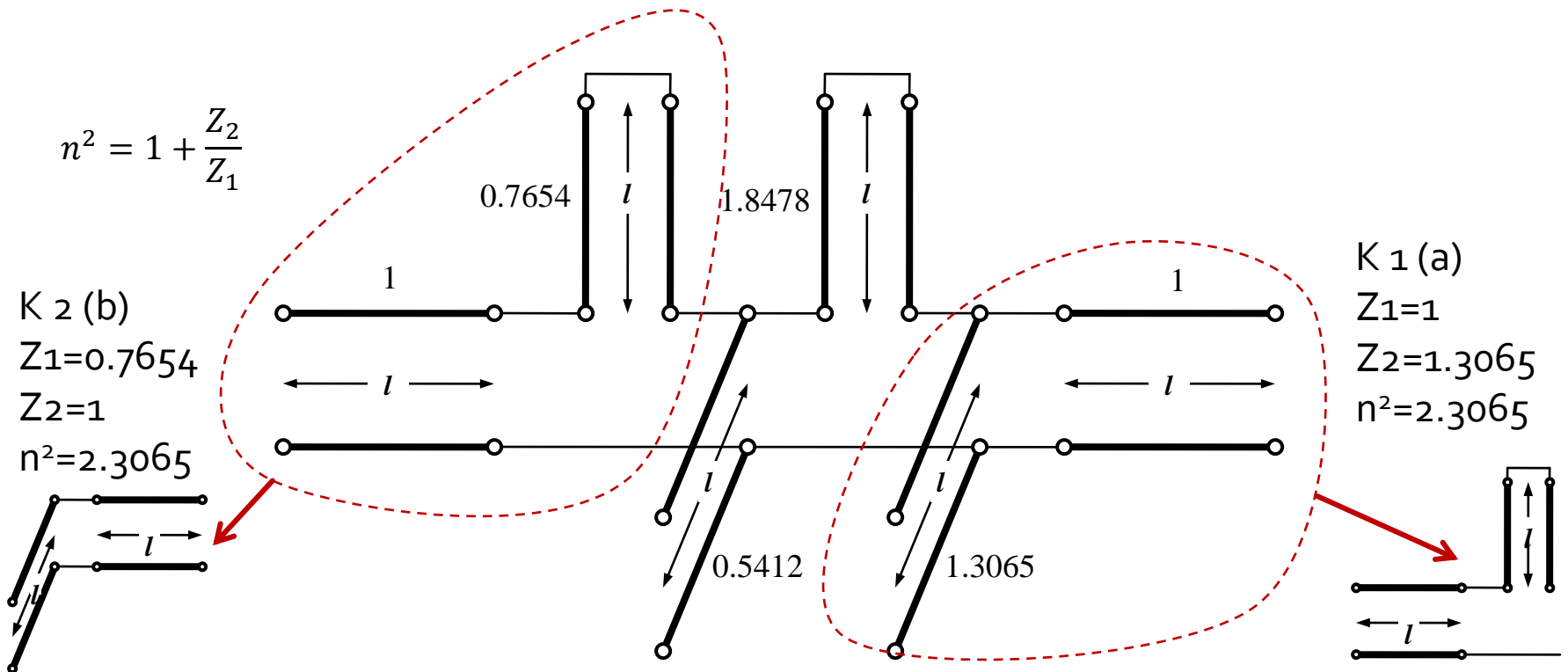
# Example

- In all 4 Kuroda's Identities we **always** have a circuit with a series line section (not present in initial circuit):
  - we **add** unit elements ( $z = 1, l = \lambda/8$ ) at the ends of the filter (these redundant elements do not affect filter performance since they are matched to  $z = 1$ , both source and load)
  - we **apply** one of the Kuroda's Identities at both ends and **continue** (add unit ...)
  - we can **stop** the procedure when we have a series line section between all the stubs from Richards' transformation



# Example

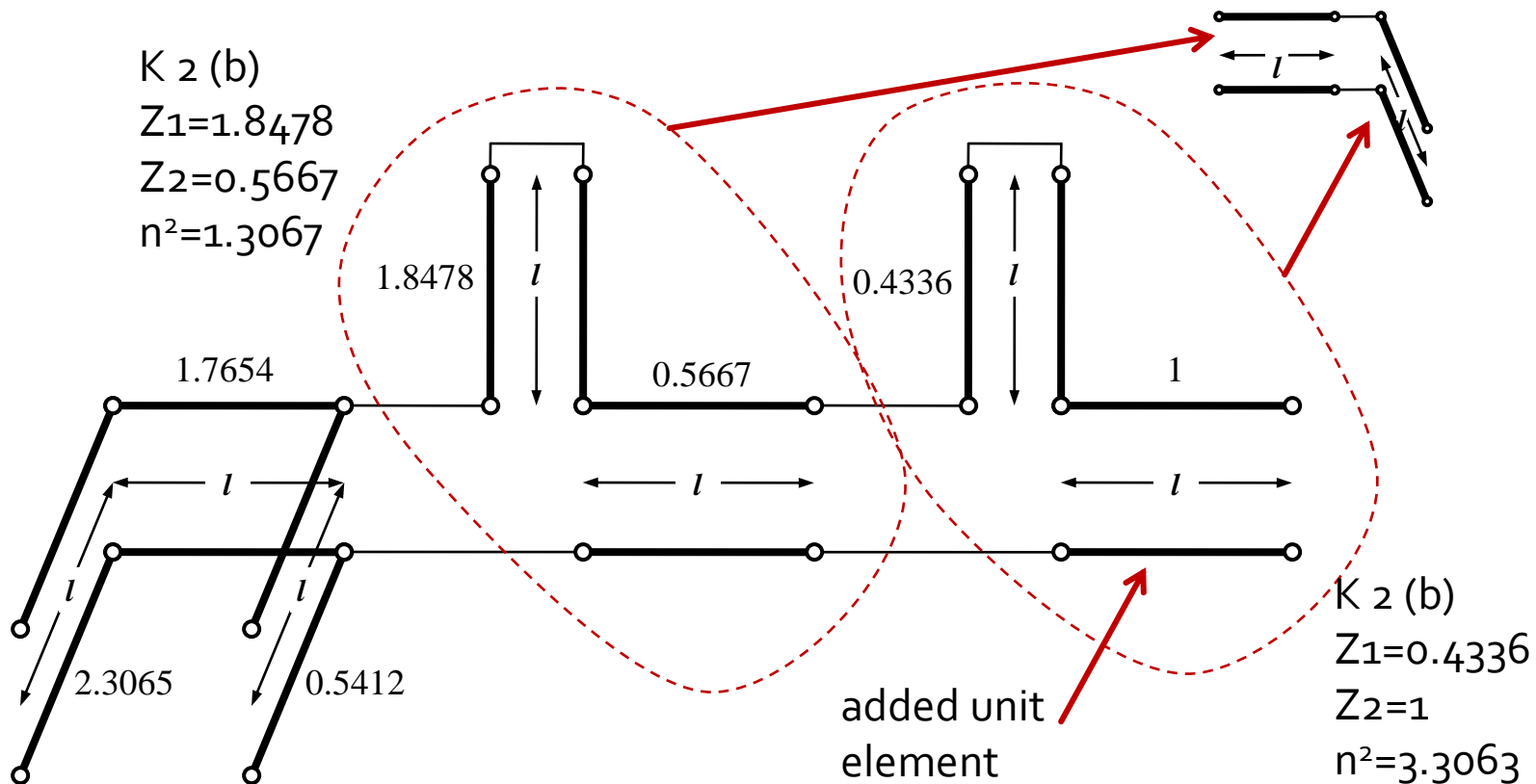
- Apply:
  - Kuroda 2 ( $L, Z$  known  $\rightarrow C, Z$ ) on the left side
  - Kuroda 1 ( $C, Z$  known  $\rightarrow L, Z$ ) on the right side



# Example

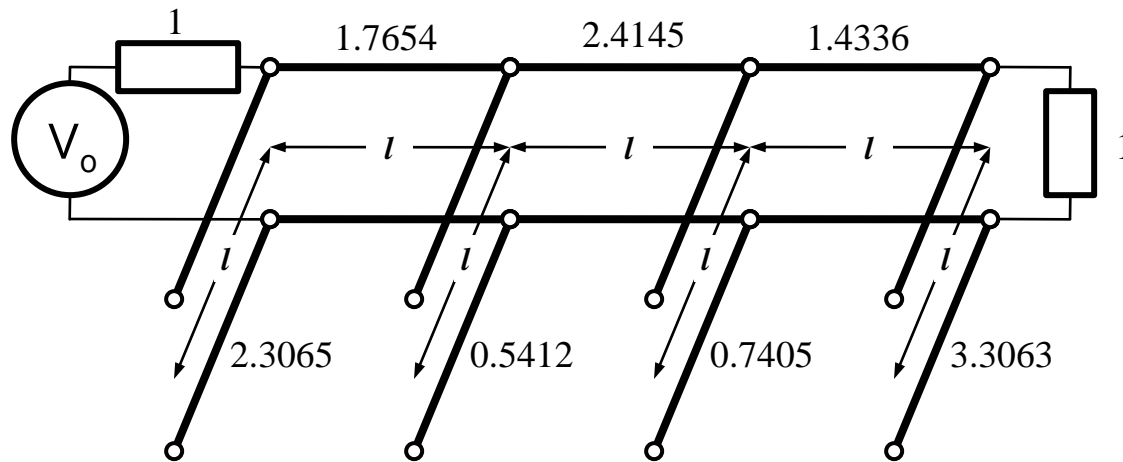
- We add another unit element on the right side and apply Kuroda 2 twice

$$n^2 = 1 + \frac{Z_2}{Z_1}$$

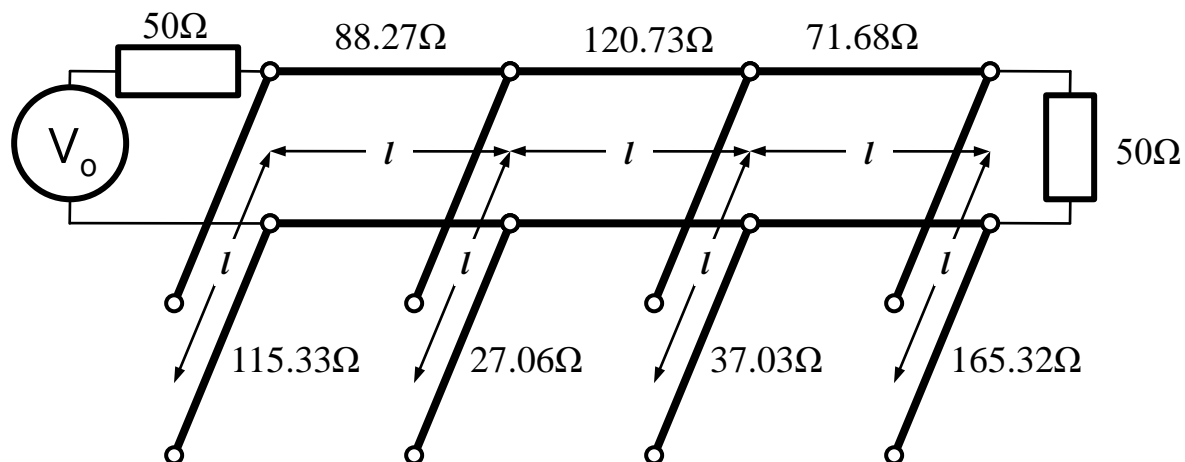




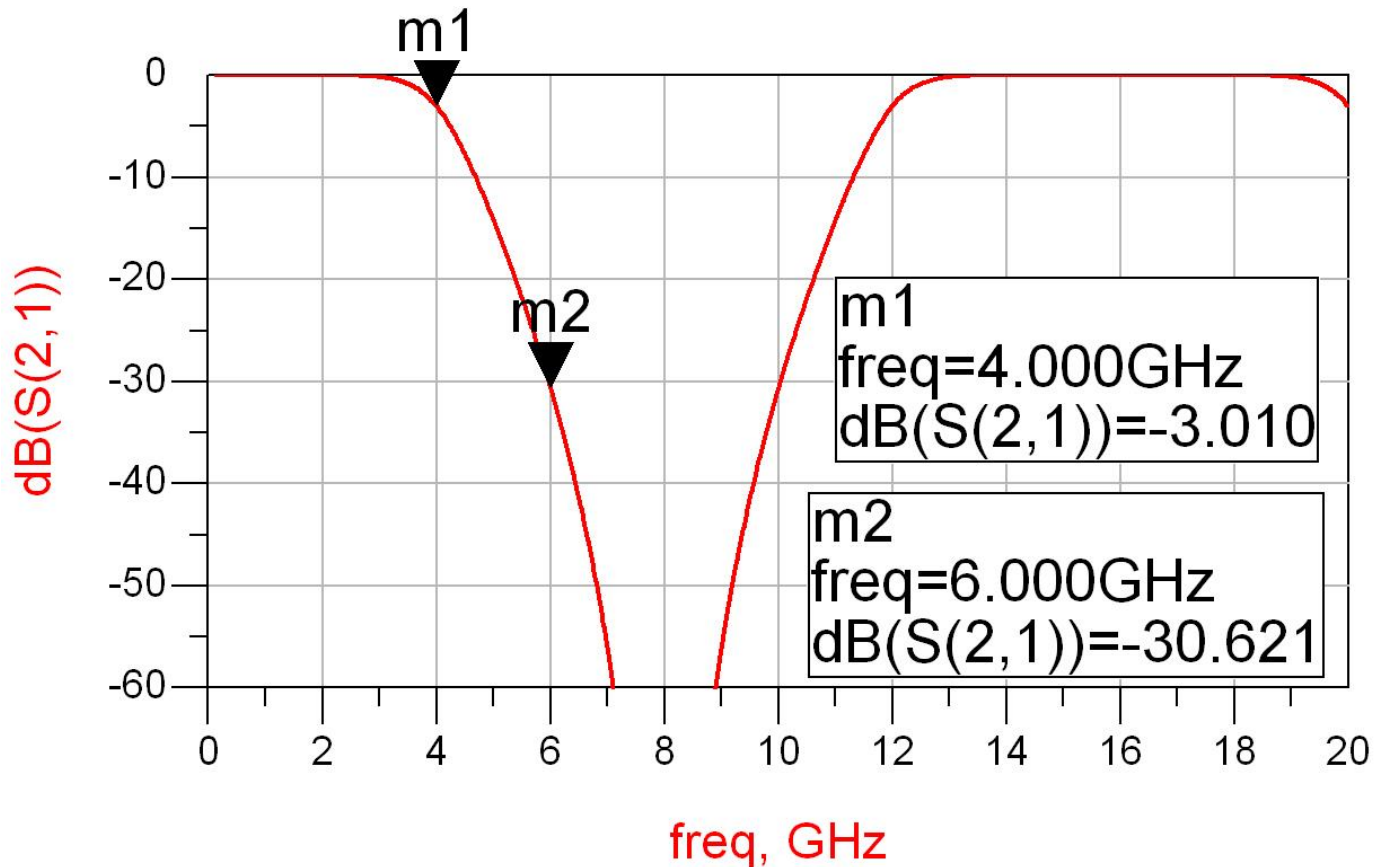
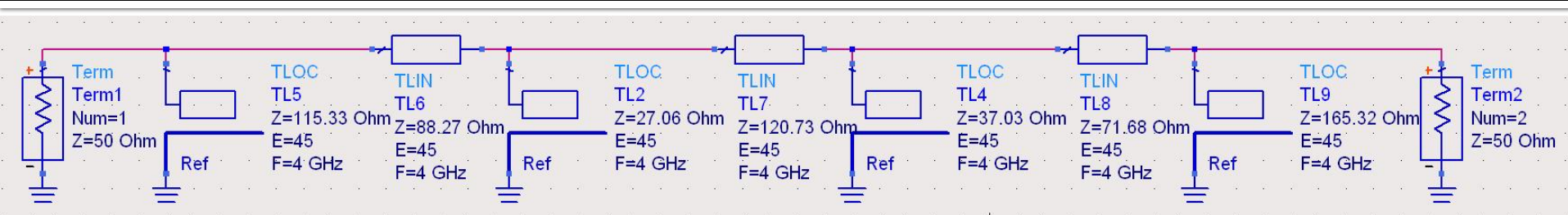
# Example



- Impedance scaling (multiply by  $50\Omega$ )



# Kuroda's Identities – ADS



# Examples

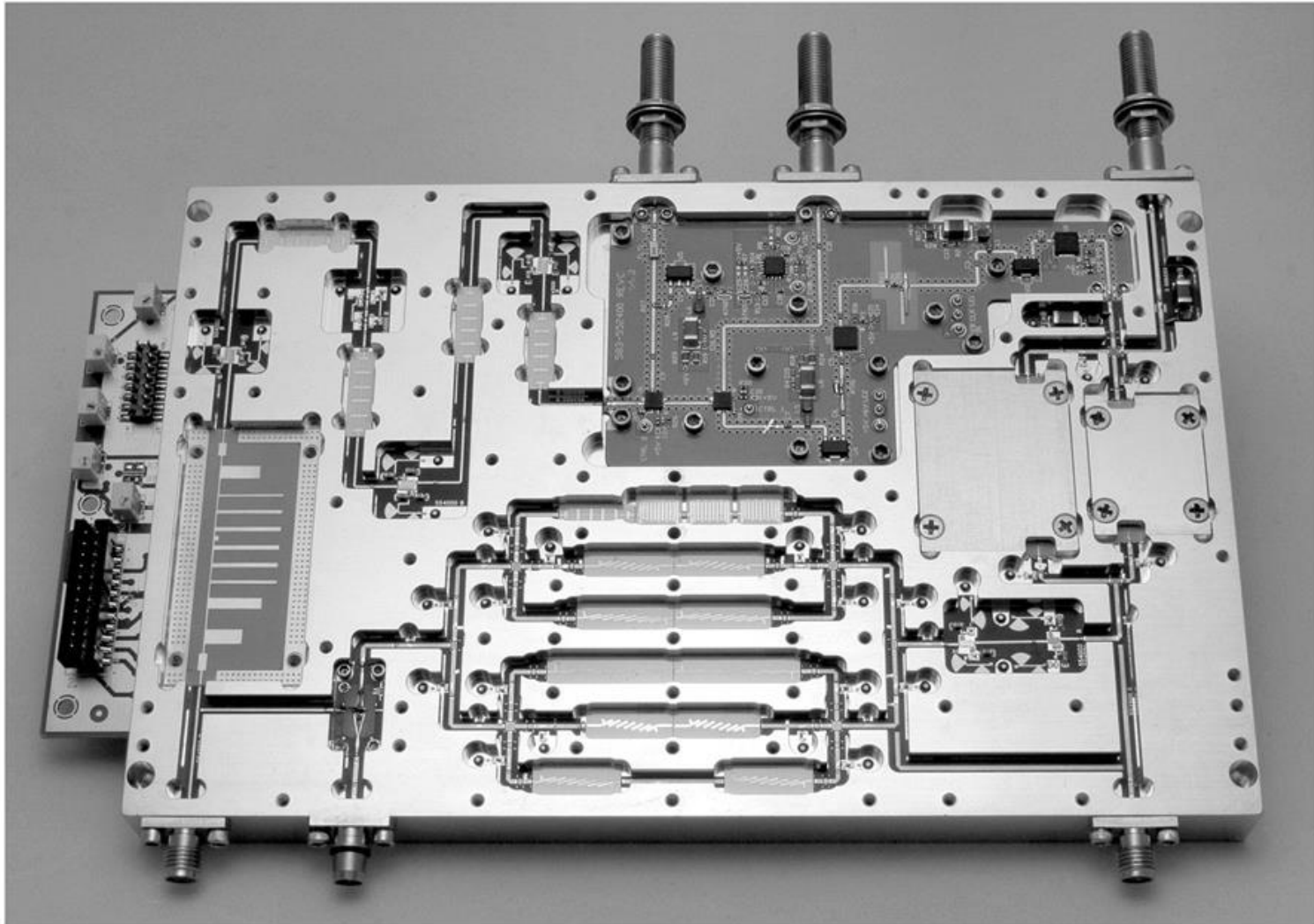


Figure 8.55  
Courtesy of LNX Corporation, Salem, N.H.

# Examples

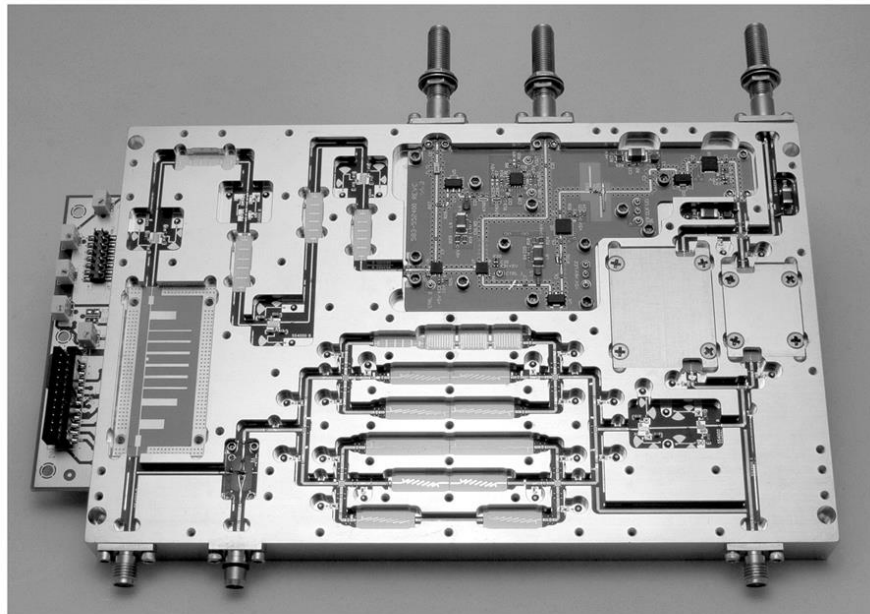
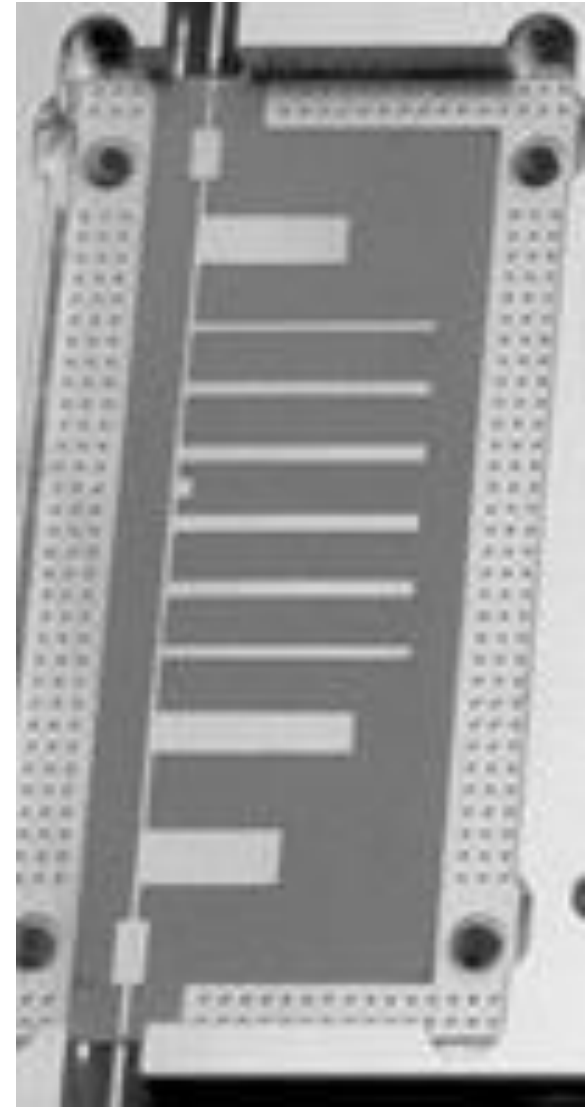
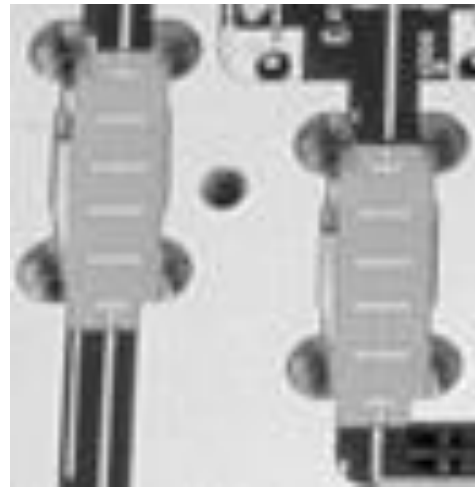
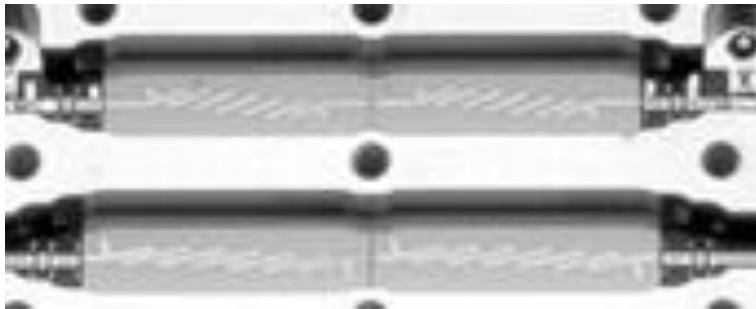


Figure 8.55  
Courtesy of LNX Corporation, Salem, N.H.



# Impedance and Admittance Inverters

- Richards' transformation and Kuroda's identities are useful especially for low-pass filters in technologies where the series stubs would be very difficult/impossible to implement (microstrip)
- In the case of other filters (example 3<sup>rd</sup> order BPF):
  - series inductance can be implemented using K1-K2
  - series capacitance cannot be implemented using shunt stubs

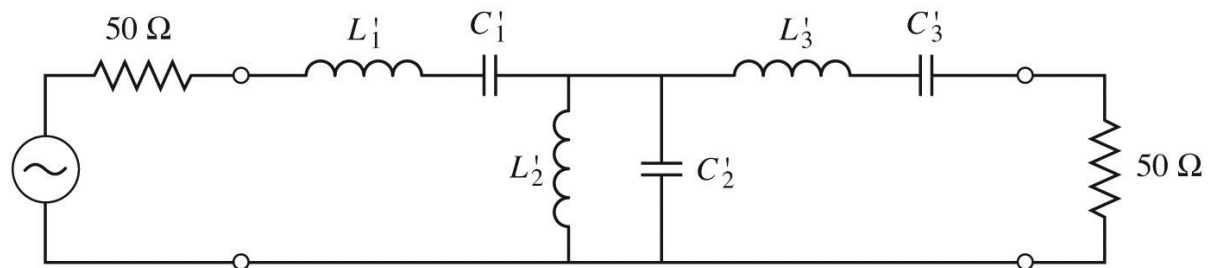


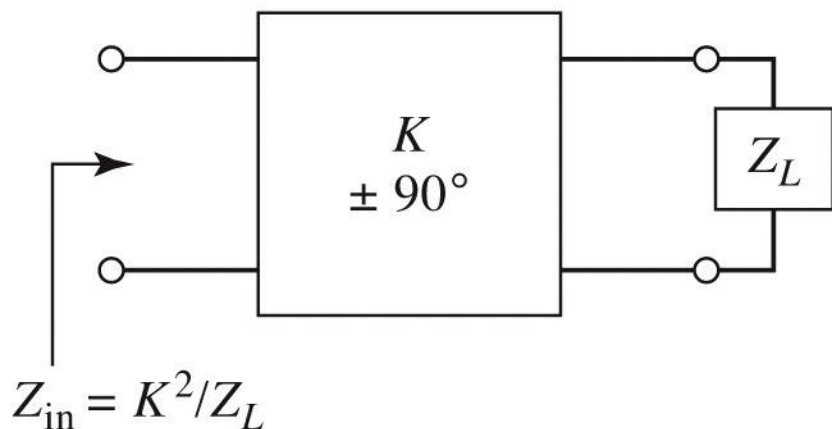
Figure 8.32  
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# Impedance and Admittance Inverters

- For cases where Richards + Kuroda do not offer practical solutions we use circuits called **impedance and admittance inverters**

$$Z_{in} = \frac{K^2}{Z_L}$$

Impedance inverters



$$Y_{in} = \frac{J^2}{Y_L}$$

Admittance inverters

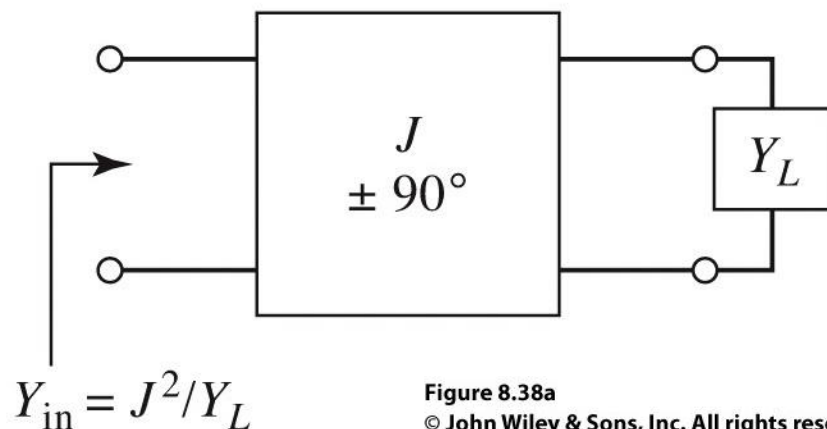


Figure 8.38a

# Impedance and Admittance Inverters

- The simplest example of impedance and admittance inverter is the **quarter-wave transformer** (L3)

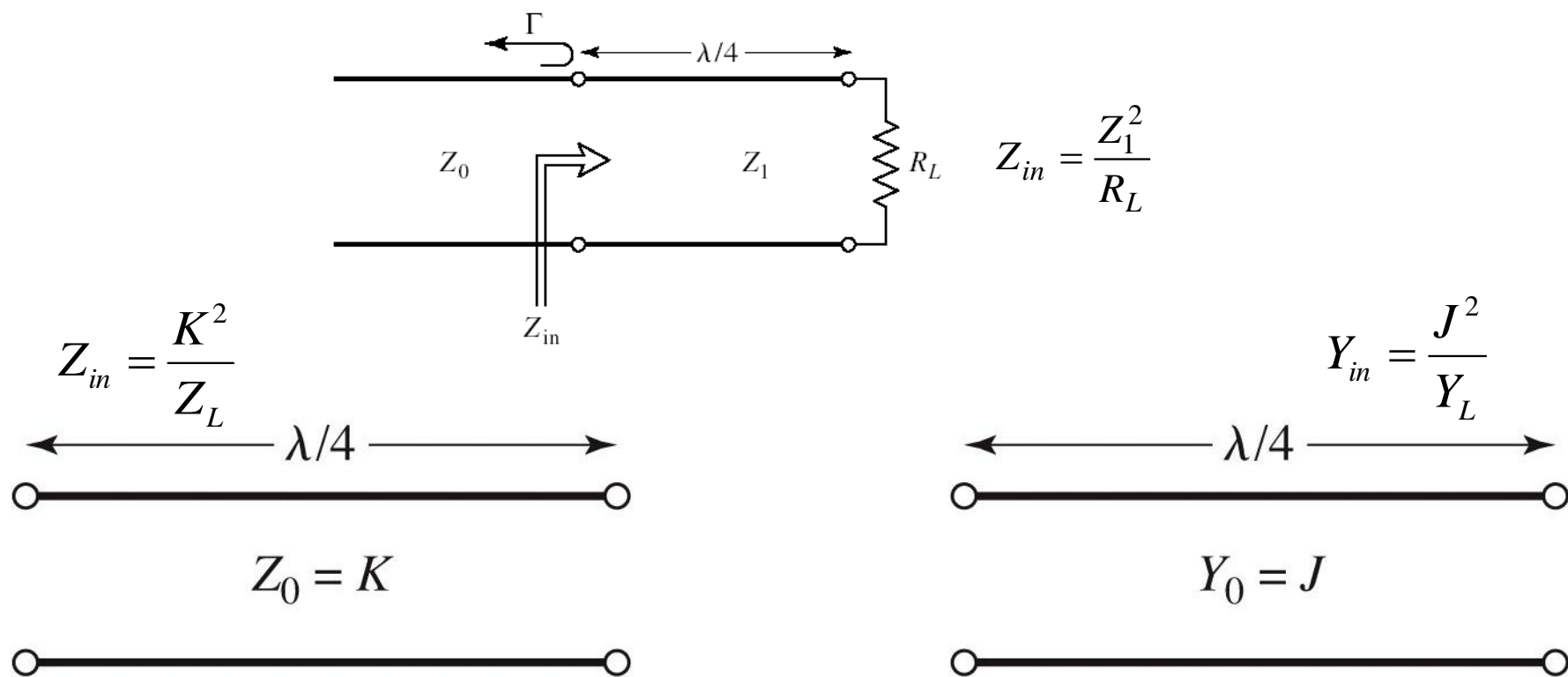
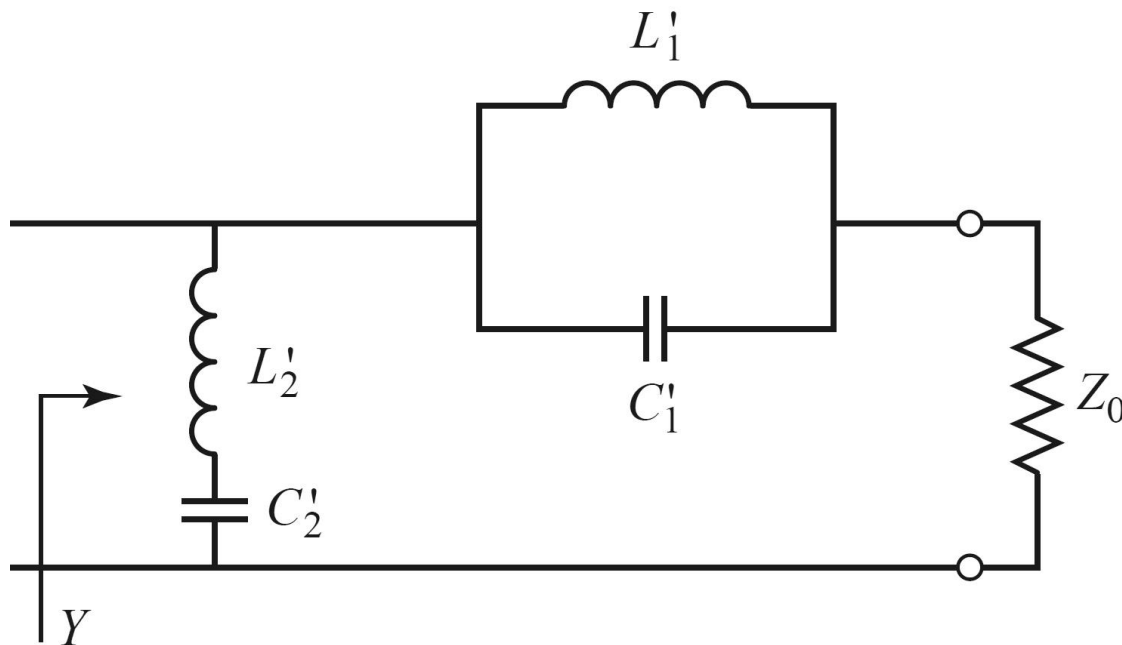


Figure 8.38b  
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# Impedance and Admittance Inverters

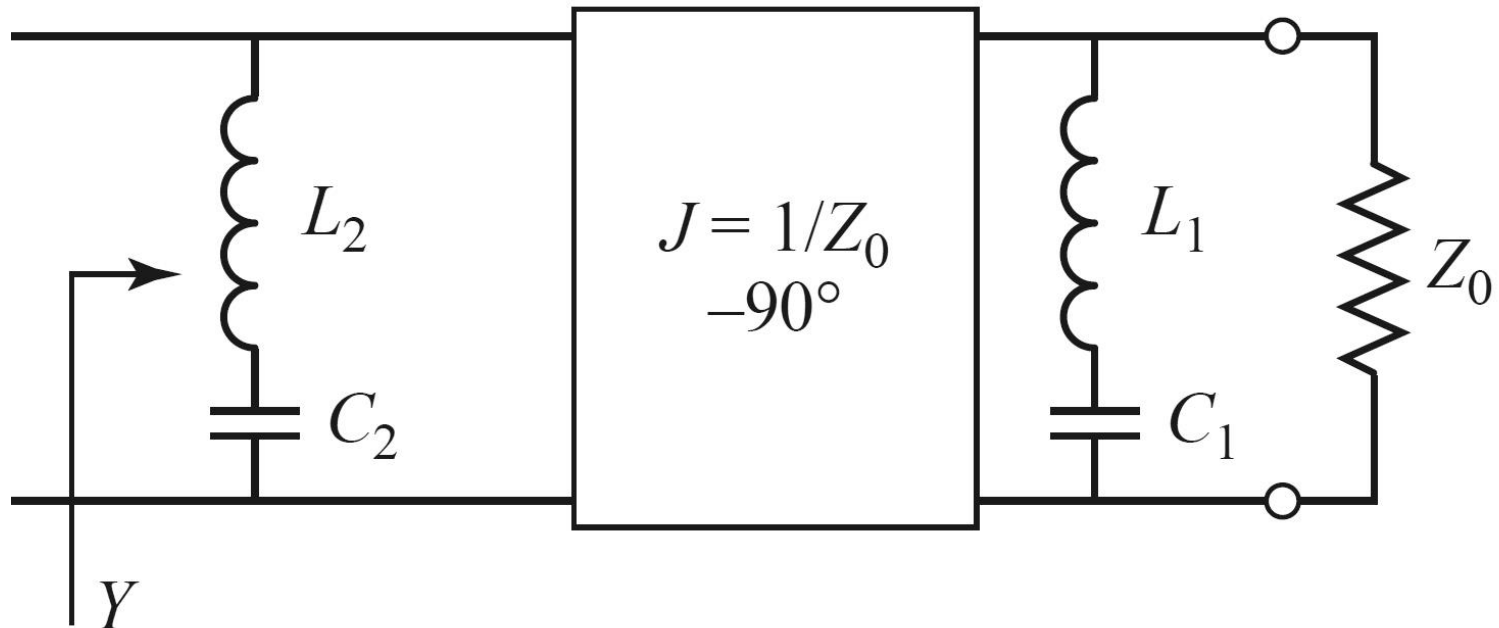
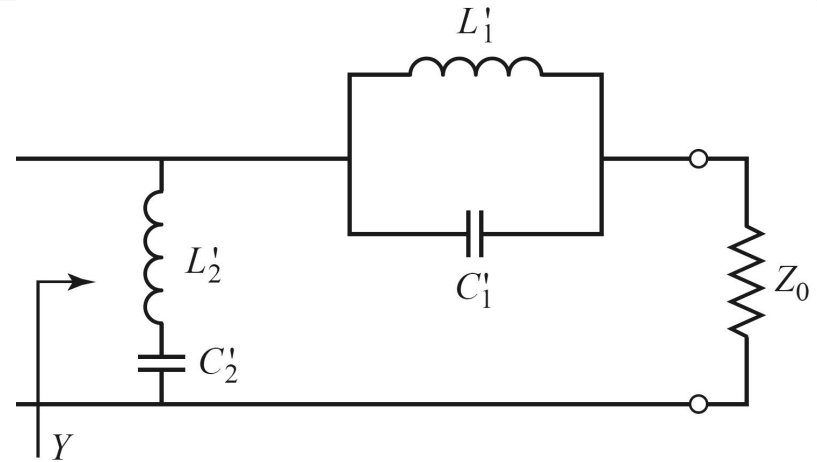
- Impedance/admittance inverters can be used to change the structure of a designed filter to a realizable form
- For example a 2<sup>nd</sup> order BSF





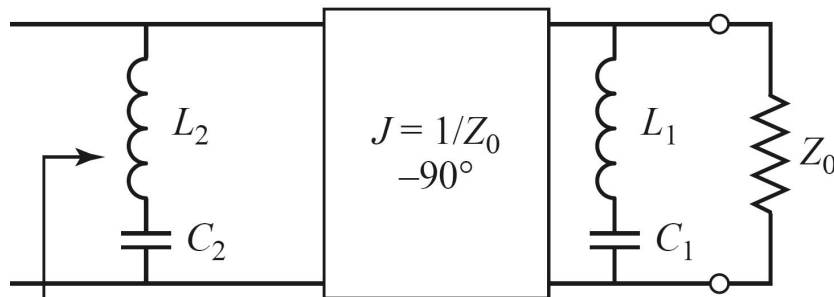
# Impedance and Admittance Inverters

- The series elements can be eliminated/replaced using an admittance inverter

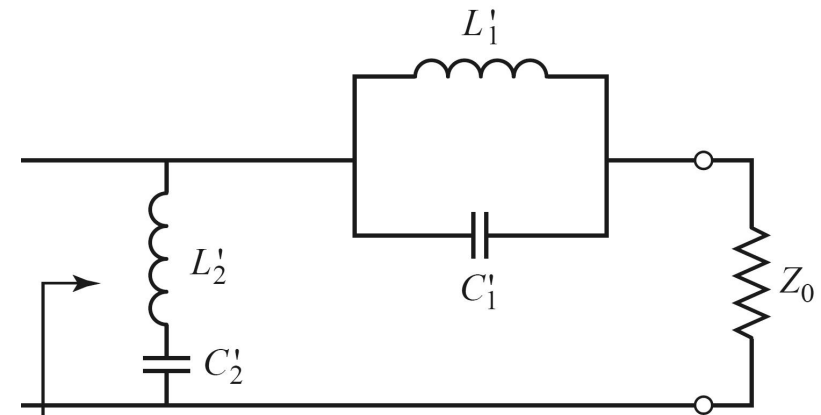


# Impedance and Admittance Inverters

- The equivalence of the two schematics (when looking from the left) is proofed by obtaining the same input admittance



$$Y = \frac{1}{j \cdot \omega \cdot L_2 + \frac{1}{j \cdot \omega \cdot C_2}} + \frac{1}{Z_0} \cdot \left( \frac{1}{j \cdot \omega \cdot L_1 + \frac{1}{j \cdot \omega \cdot C_1}} + \frac{1}{Z_0} \right)^{-1}$$



$$Y' = \frac{1}{j \cdot \omega \cdot L'_2 + \frac{1}{j \cdot \omega \cdot C'_2}} + \left( \frac{1}{j \cdot \omega \cdot C'_1 + \frac{1}{j \cdot \omega \cdot L'_1}} + Z_0 \right)^{-1}$$

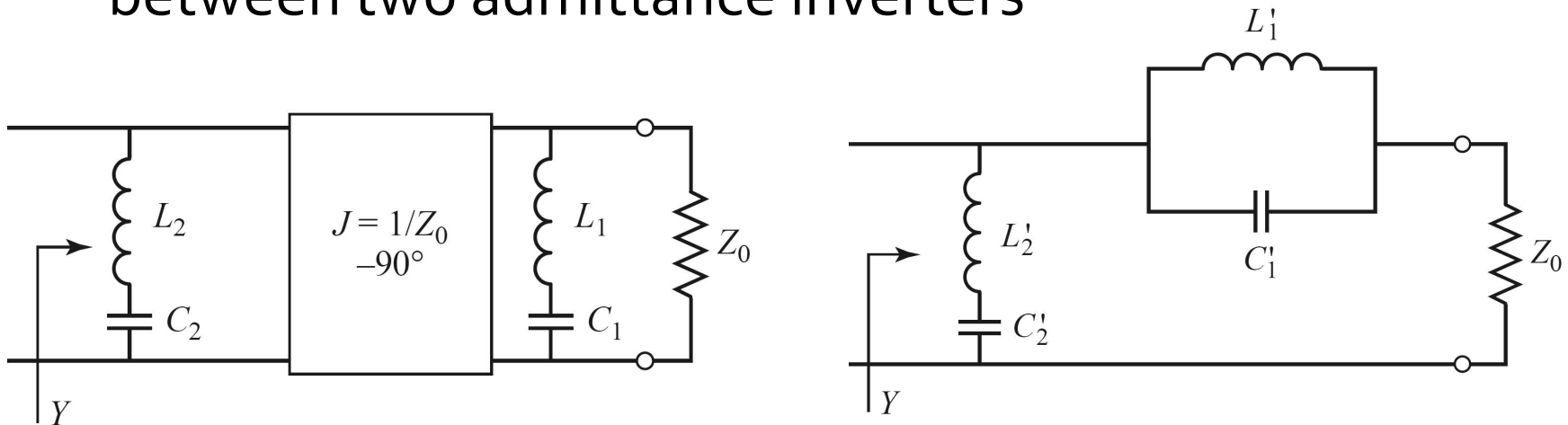
$$L_n \cdot C_n = L'_n \cdot C'_n = \frac{1}{\omega_0^2} \Rightarrow \frac{1}{Z_0^2} \cdot \sqrt{\frac{L_1}{C_1}} = \sqrt{\frac{C'_1}{L'_1}} \Rightarrow Y = Y'$$

$$\sqrt{\frac{L_2}{C_2}} = \sqrt{\frac{L'_2}{C'_2}}$$

- A similar result can be obtained for a bandpass filter

# Impedance and Admittance Inverters

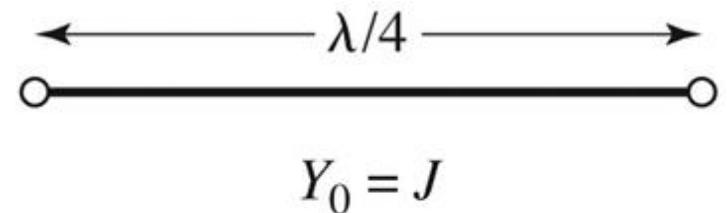
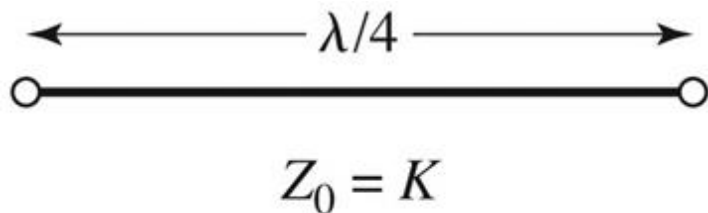
- The complete equivalence (when looking from both sides) is obtained by enclosing the series LC circuit between two admittance inverters



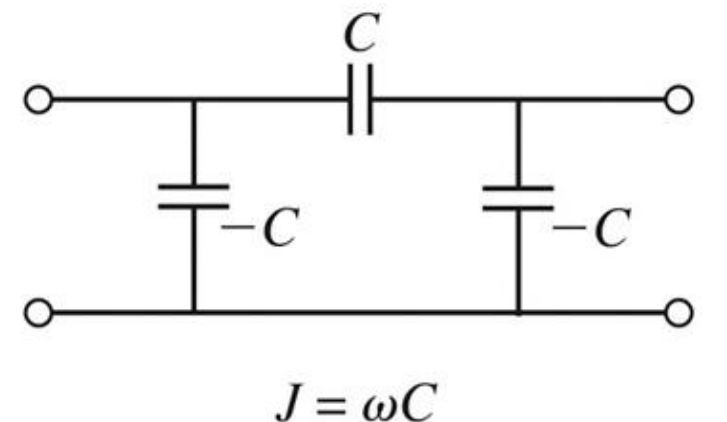
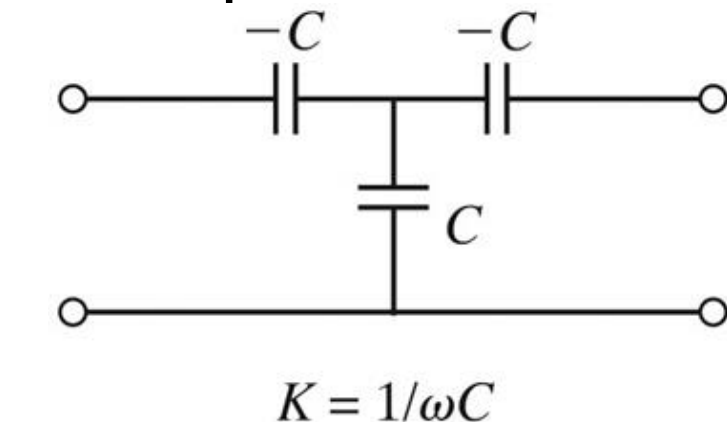
- A **series LC** circuit inserted in series in the circuit can be replaced by a **shunt LC** circuit inserted in parallel enclosed between 2 admittance inverters
- A **shunt LC** circuit inserted in series in the circuit can be replaced by a **series LC** circuit inserted in parallel enclosed between 2 admittance inverters

# Practical implementations of impedance/admittance inverters

- Most often the quarter-wave transformer is used

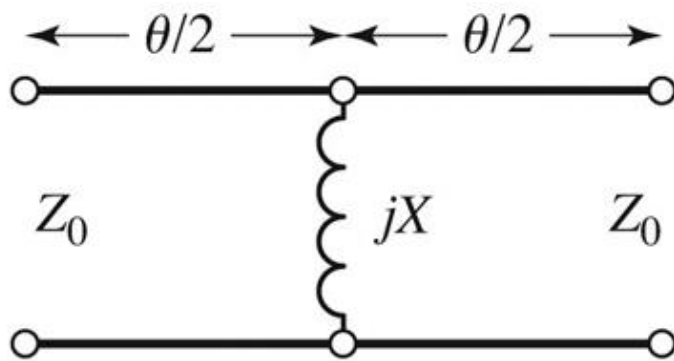


- Implementation with capacitor networks



# Practical implementations of impedance/admittance inverters

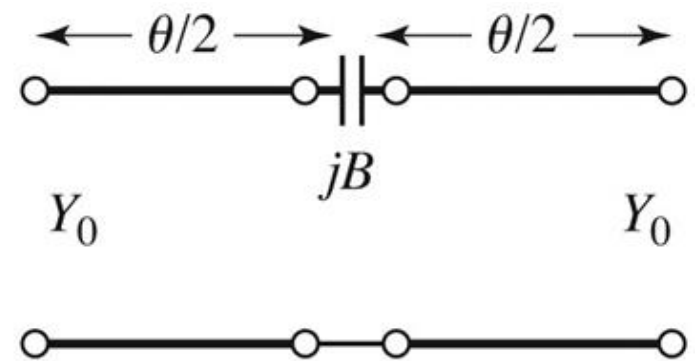
- Implementation with transmission lines and reactive elements



$$K = Z_0 \cdot \tan \left| \frac{\theta}{2} \right|$$

$$X = \frac{K}{1 - \left( \frac{K}{Z_0} \right)^2}$$

$$\theta = -\tan^{-1} \frac{2 \cdot X}{Z_0}$$



$$J = Y_0 \cdot \tan \left| \frac{\theta}{2} \right|$$

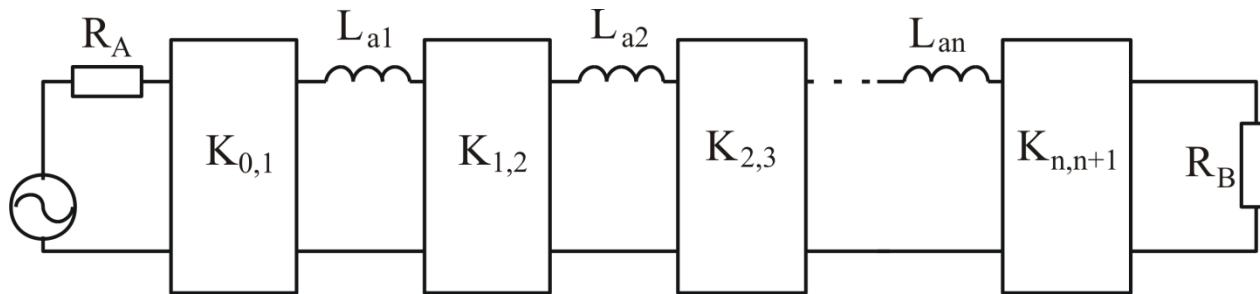
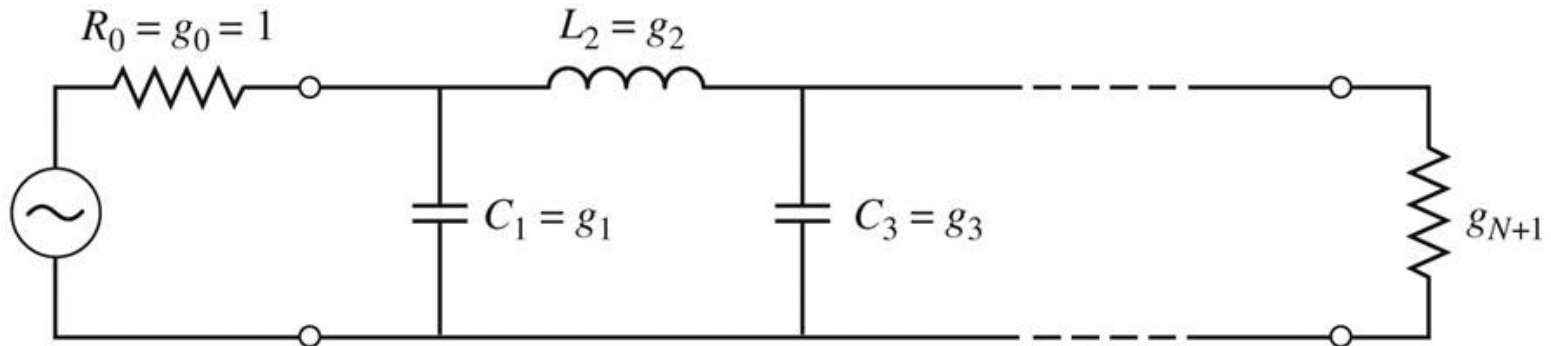
$$B = \frac{J}{1 - \left( \frac{J}{Y_0} \right)^2}$$

$$\theta = -\tan^{-1} \frac{2 \cdot B}{Y_0}$$

$$\theta < 0$$

# Prototype filters using inverters

- Using impedance/admittance inverters we can implement prototype filters using a single type of reactive elements
  - Shunt C replaced by series L enclosed between 2 inverters



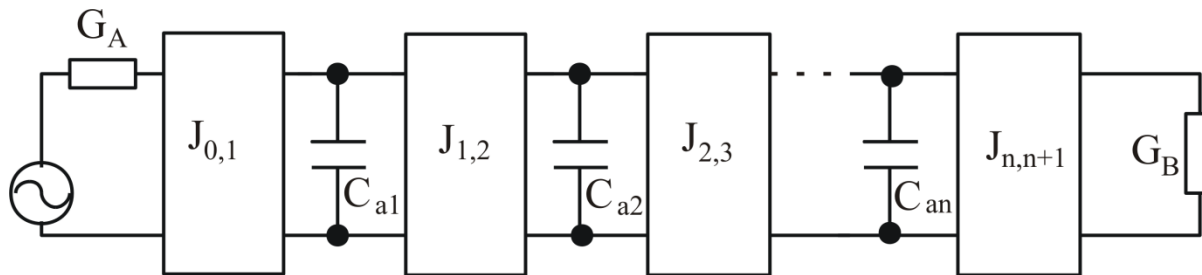
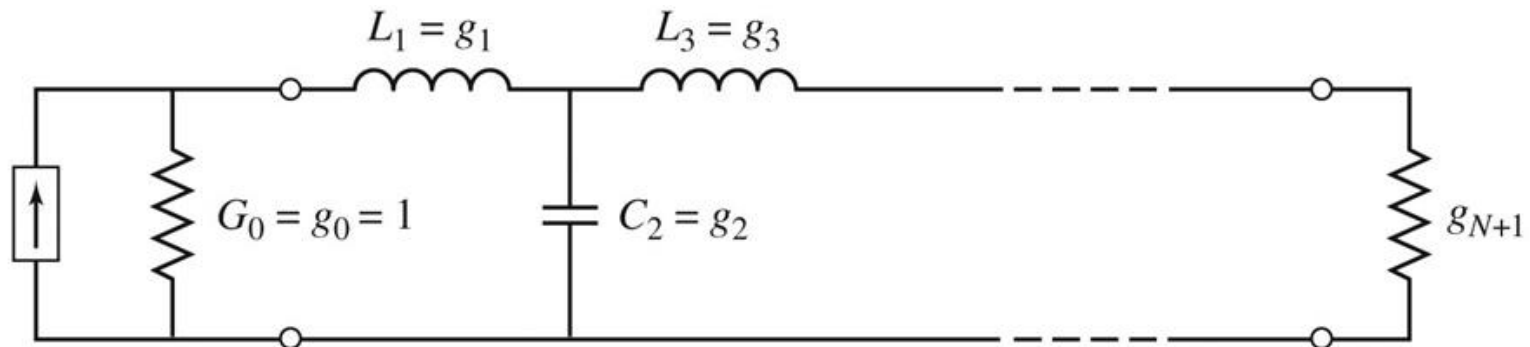
$$K_{0,1} = \sqrt{\frac{R_A \cdot L_{a,1}}{g_0 \cdot g_1}}$$

$$K_{k,k+1} \Big|_{k=1, n-1} = \sqrt{\frac{L_{a,k} \cdot L_{a,k+1}}{g_k \cdot g_{k+1}}}$$

$$K_{n,n+1} = \sqrt{\frac{L_{a,n} \cdot R_B}{g_n \cdot g_{n+1}}}$$

# Prototype filters using inverters

- Using impedance/admittance inverters we can implement prototype filters using a single type of reactive elements
  - Series L replaced by shunt C enclosed between 2 inverters



$$J_{0,1} = \sqrt{\frac{G_A \cdot C_{a,1}}{g_0 \cdot g_1}}$$

$$J_{k,k+1} \Big|_{k=1, n-1} = \sqrt{\frac{C_{a,k} \cdot C_{a,k+1}}{g_k \cdot g_{k+1}}}$$

$$J_{n,n+1} = \sqrt{\frac{C_{a,n} \cdot g_B}{g_n \cdot g_{n+1}}}$$

# Prototype filters using inverters

- For prototype filters using inverters formulas we have  $2 \cdot N + 1$  parameters and  $N + 1$  equations (to ensure the equivalence of the 2 schematics) so  $N$  parameters can be chosen freely
  - convenient values for the reactance can be chosen, and the required inverters will be computed from the equivalence equations or,
  - convenient inverters can be chosen, and the required reactance values will be computed from the equivalence equations



# BPF and BSF using inverters

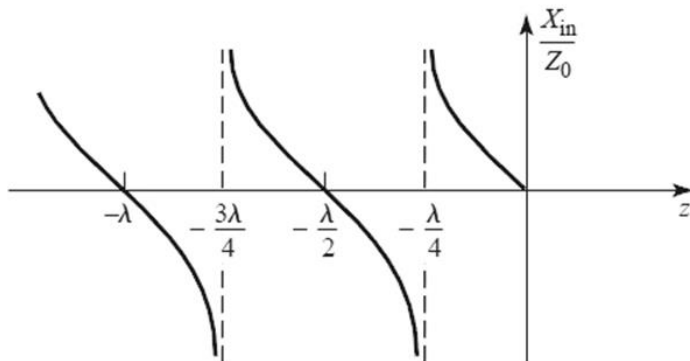
- The same principle can be applied to the BPF and BSF filters, those can be implemented using  $N+1$  inverters and  $N$  resonators (**series or shunt LC circuits** with resonant frequency  $\omega_0$ ) connected either in series or in parallel enclosed between 2 inverters
  - BPF are implemented with
    - series LC circuits connected in series between inverters
    - shunt LC circuits connected in parallel between inverters
  - BSF are implemented with
    - shunt LC circuits connected in series between inverters
    - series LC circuits connected in parallel between inverters

# Lines as resonators

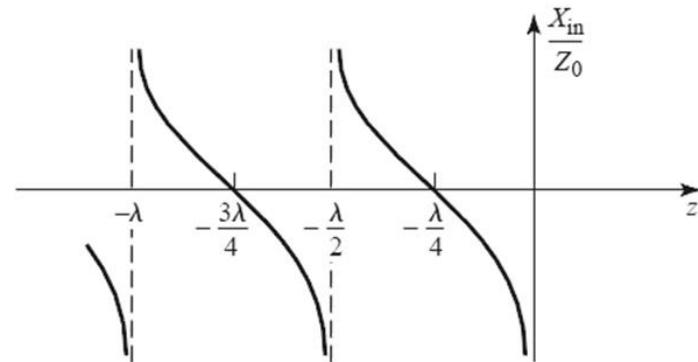
- The impedance of short-circuited or open-circuited line (stub) shows a resonant behavior that can be used to implement required resonators

$$Z_{in} = Z_0 \cdot \frac{Z_L + j \cdot Z_0 \cdot \tan \beta \cdot l}{Z_0 + j \cdot Z_L \cdot \tan \beta \cdot l}$$

$$Z_{in,sc} = j \cdot Z_0 \cdot \tan \beta \cdot l$$

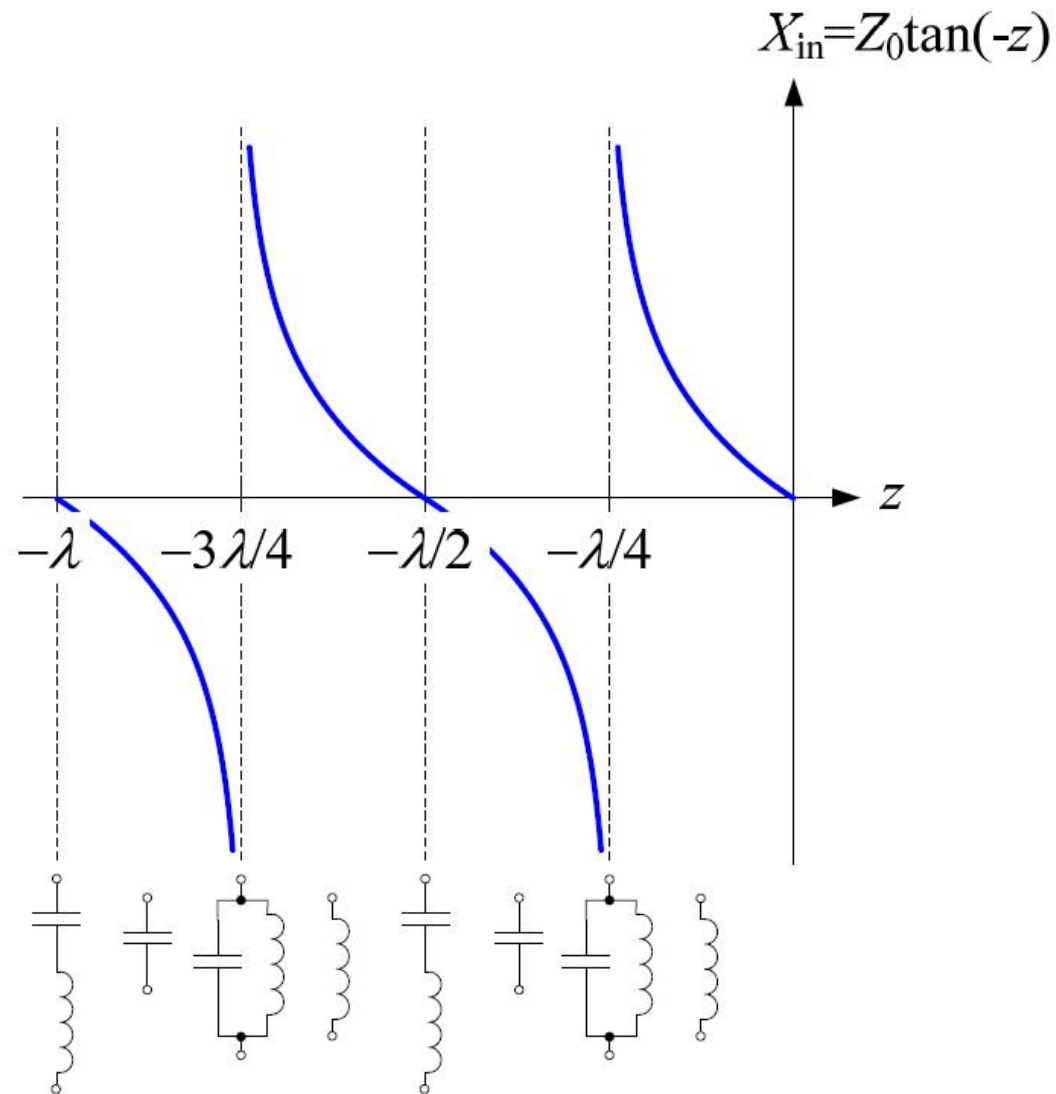


$$Z_{in,oc} = -j \cdot Z_0 \cdot \cot \beta \cdot l$$



# Lines as resonators

- Short-circuited line
- For the frequency at which  $l = \lambda/4$  ( $\omega_0$ ) the line behaves as a shunt LC resonator circuit
  - the line shows capacitive behavior for lower frequencies ( $l > \lambda/4$ )
  - the line shows inductive behavior for higher frequencies ( $l < \lambda/4$ )
- Similar discussion for the open circuited line (equivalent to a series LC resonator around the frequency at which  $l = \lambda/4$ )



# BPF/BSP design formulas

- When the admittance inverters are implemented with quarter-wave transformers with  $Z_0$  characteristic impedance
  - BPF – short-circuited shunt stubs with  $l = \lambda/4$

$$Z_{0n} \approx \frac{\pi \cdot Z_0 \cdot \Delta}{4 \cdot g_n}$$

- BSF – open-circuited shunt stubs with  $l = \lambda/4$

$$Z_{0n} \approx \frac{4 \cdot Z_0}{\pi \cdot g_n \cdot \Delta}$$

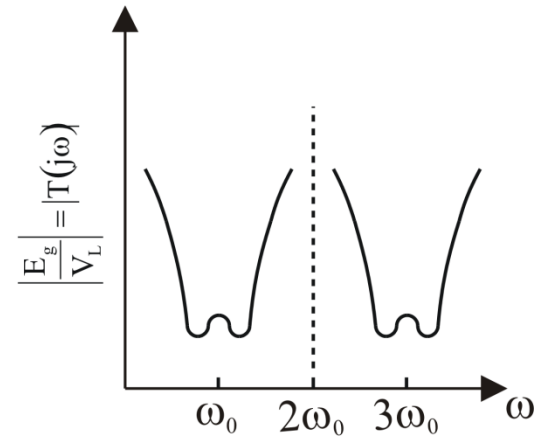
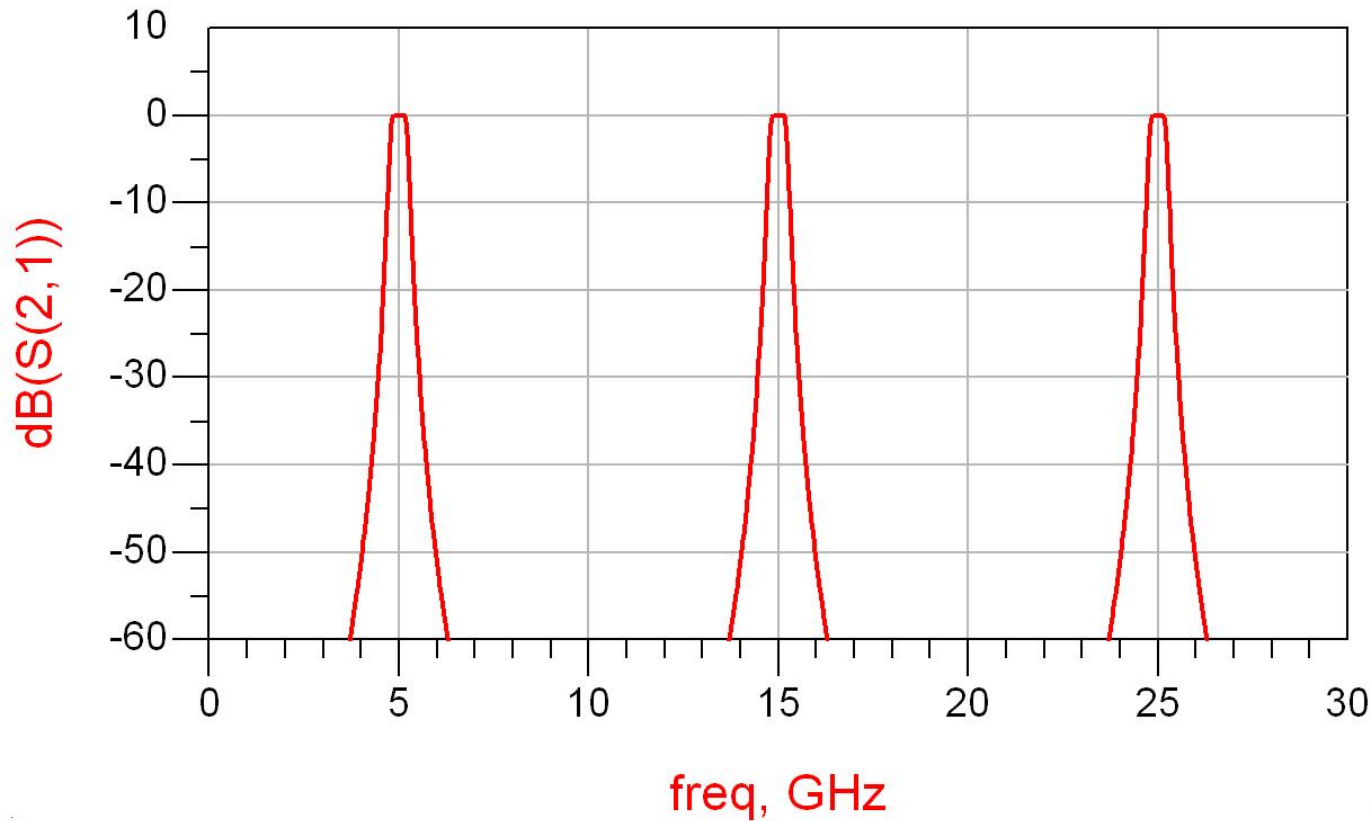
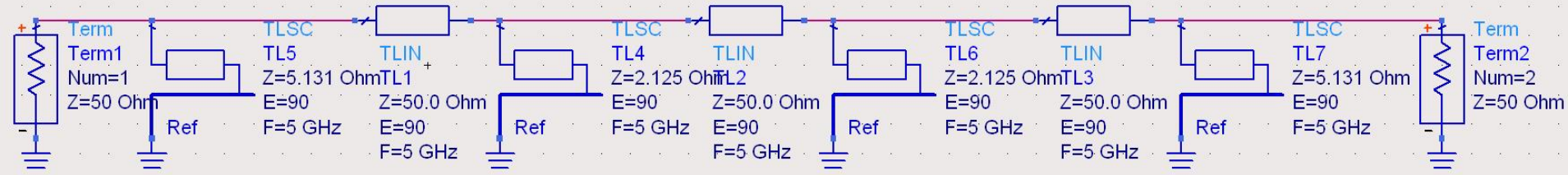
# Example

- Similar to a project assignment
- Follows the amplifier designed as in L8
- 4<sup>th</sup> order bandpass filter,  $f_0 = 5\text{GHz}$ , fractional bandwidth of the passband 10 %
- maximally flat table or formulas for  $g_n$ :

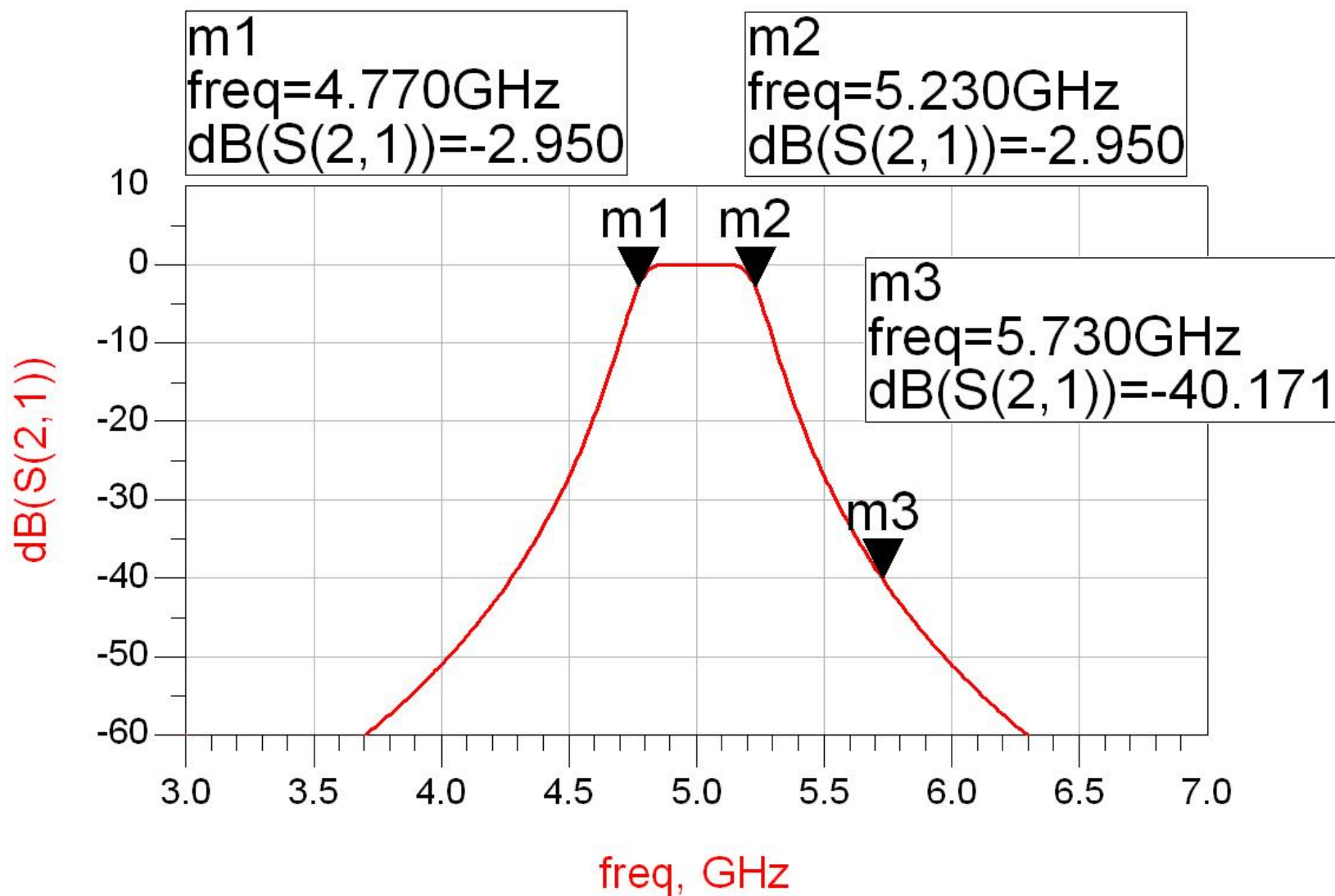
| n | $g_n$  | $Z_{0n}(\Omega)$ |
|---|--------|------------------|
| 1 | 0.7654 | 5.131            |
| 2 | 1.8478 | 2.125            |
| 3 | 1.8478 | 2.125            |
| 4 | 0.7654 | 5.131            |

$$Z_{0n} \approx \frac{\pi \cdot Z_0 \cdot \Delta}{4 \cdot g_n}$$

# ADS – BPF

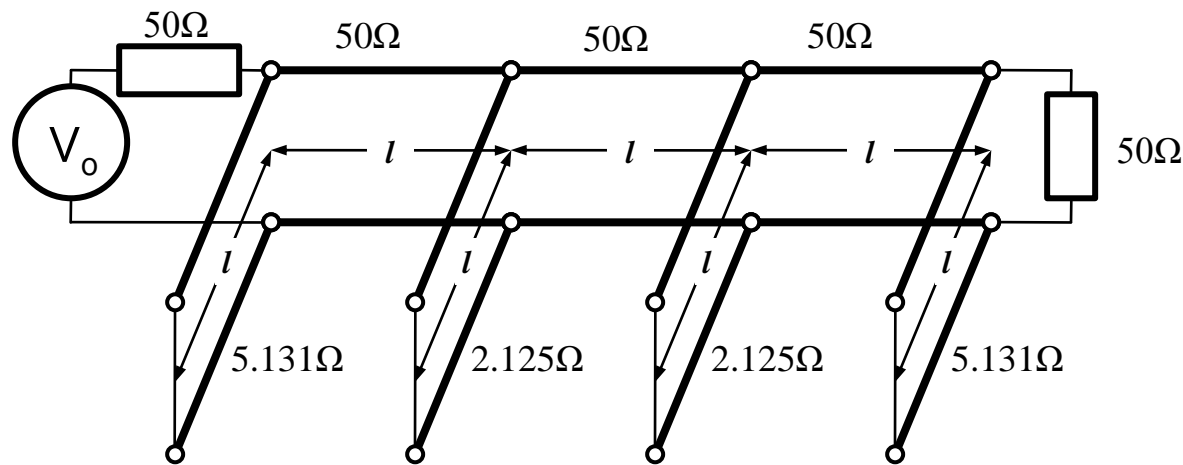


# ADS – BPF



# Example

$$l = \frac{\lambda}{4} \Rightarrow \beta \cdot l = \frac{\pi}{2}$$

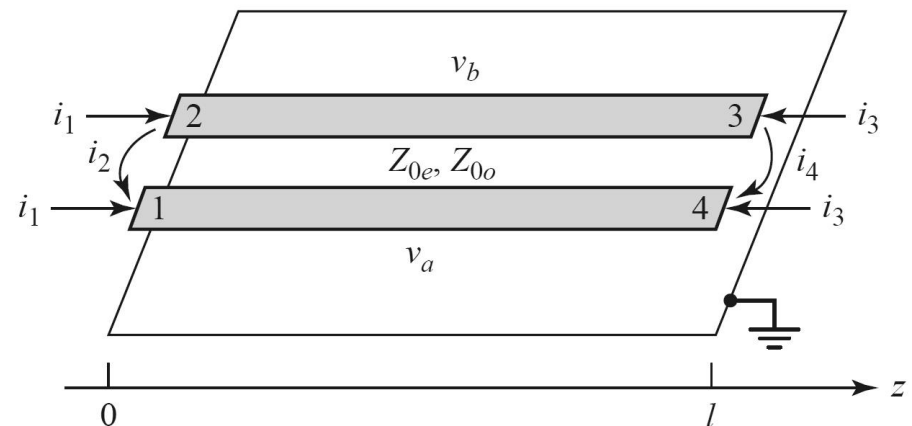
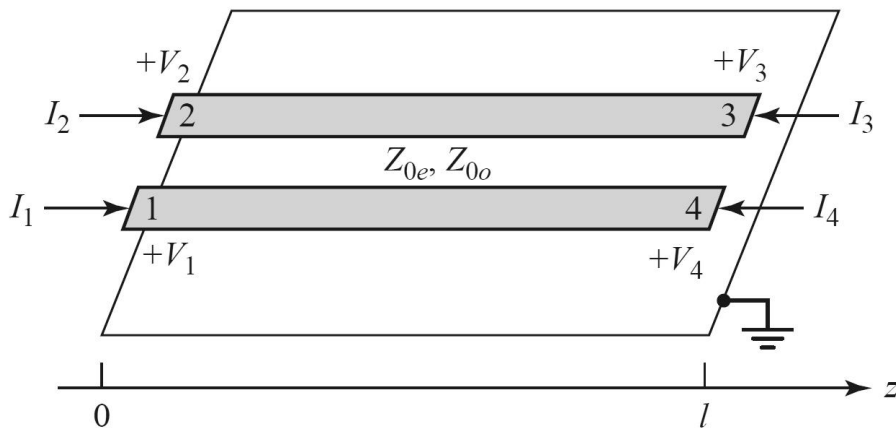


- Disadvantages of the filters using impedance inverters and lines as resonators:
  - short-circuited stubs (via-hole) for BPF
  - often the **characteristic impedances** for the stubs have **values** difficult to implement ( $2.125\Omega$ )



# Coupled Line Filters

- A parallel coupled line section model is obtained by even/odd mode analysis
- Even and odd modes are characterized by the characteristic even/odd mode impedances whose required values will impose the lines' geometry (width / distance between lines, depending on the line technology we use)



# Coupled Lines

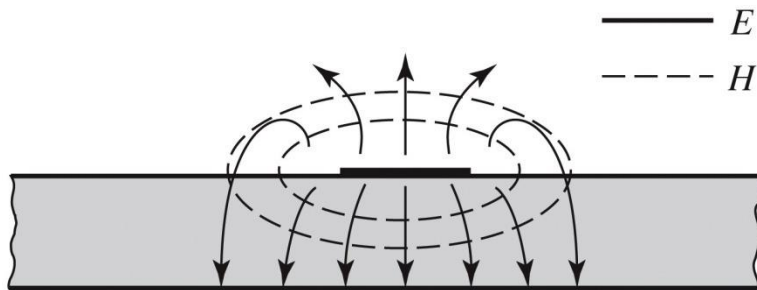
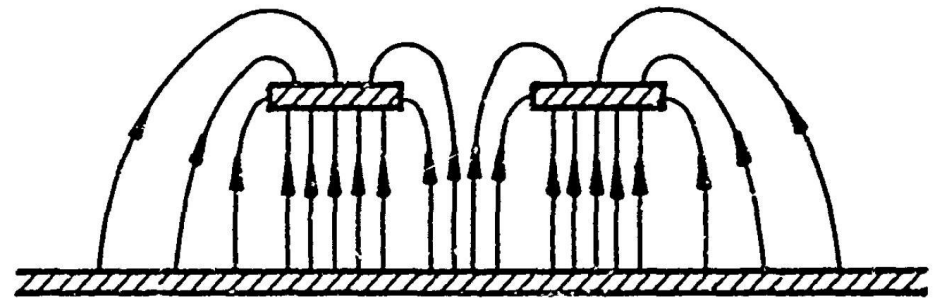
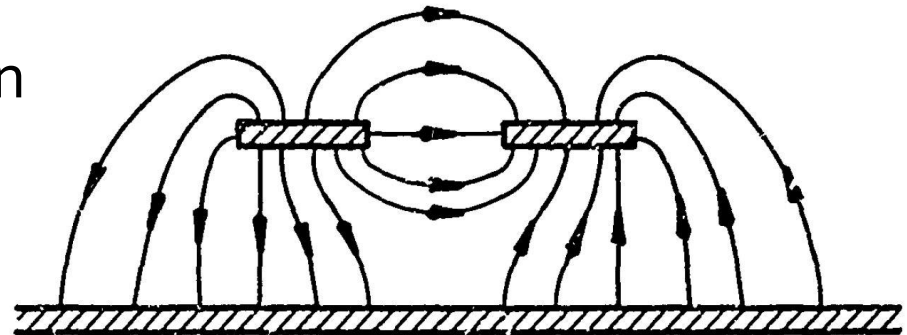


Figure 3.25b  
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b) EVEN MODE ELECTRIC FIELD PATTERN (SCHEMATIC)

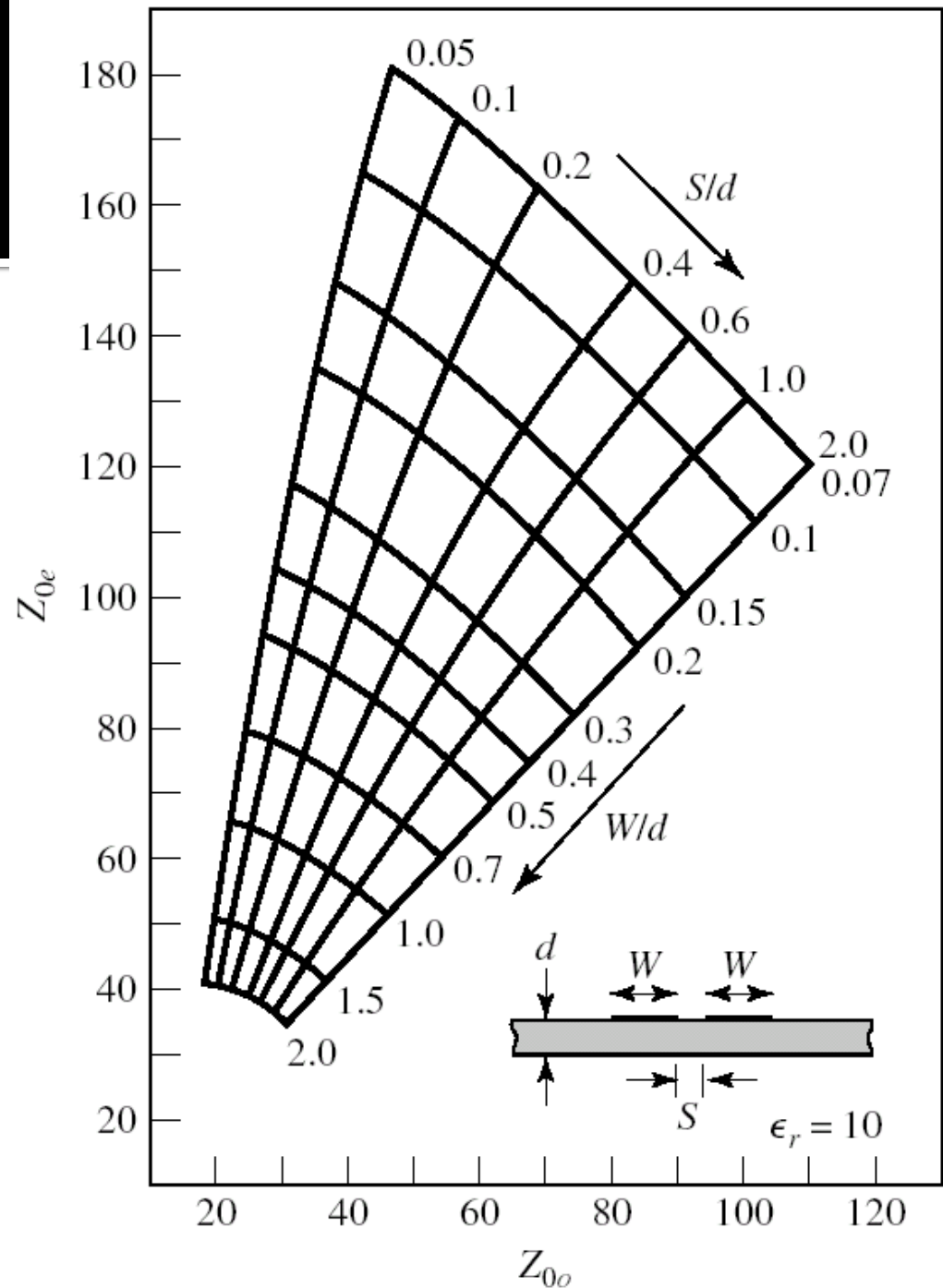


c) ODD MODE ELECTRIC FIELD PATTERN (SCHEMATIC)

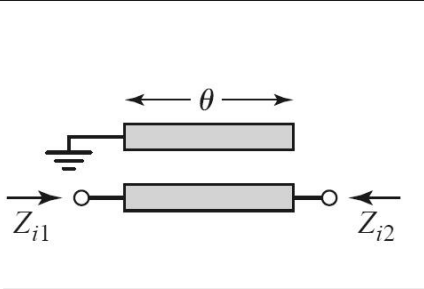
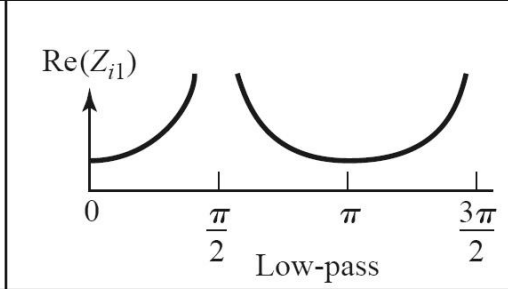
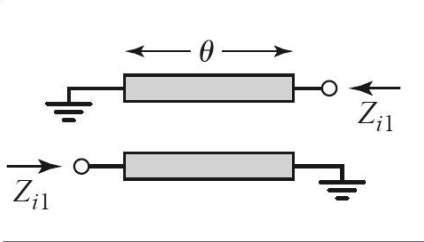
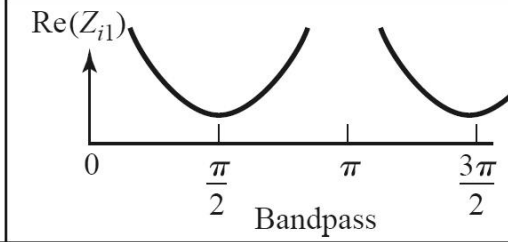
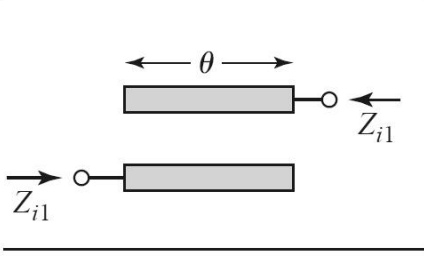
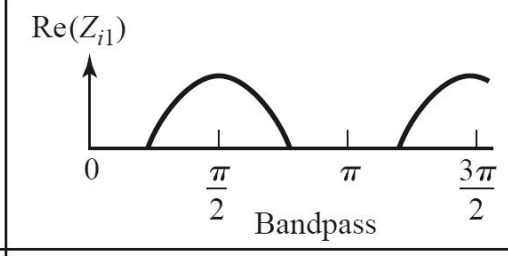
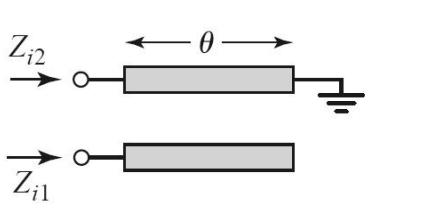
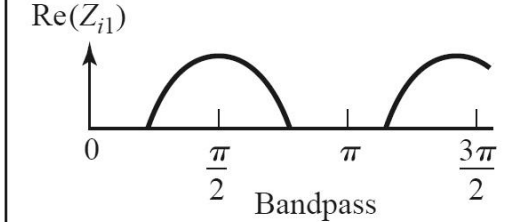
- Even mode - characterizes the common mode signal on the two lines
- Odd mode - characterizes the differential mode signal between the two lines
- Each of the two modes is characterized by **different** characteristic impedances

# Even- and odd-mode characteristic impedance

- Even- and odd-mode characteristic impedance design data for coupled microstrip lines on a substrate with  $\epsilon_r = 10$ .



# Coupled Line Filters

| Circuit   | Image Impedance  | Response  |
|---|--|---|
|    | $Z_{i1} = \frac{2Z_{0e}Z_{0o} \cos \theta}{\sqrt{(Z_{0e} + Z_{0o})^2 \cos^2 \theta - (Z_{0e} - Z_{0o})^2}}$ $Z_{i2} = \frac{Z_{0e}Z_{0o}}{Z_{i1}}$                         |  <p style="text-align: center;">Low-pass</p>   |
|    | $Z_{i1} = \frac{2Z_{0e}Z_{0o} \sin \theta}{\sqrt{(Z_{0e} - Z_{0o})^2 - (Z_{0e} + Z_{0o})^2 \cos^2 \theta}}$  |  <p style="text-align: center;">Bandpass</p>   |
|   | $Z_{i1} = \frac{\sqrt{(Z_{0e} - Z_{0o})^2 - (Z_{0e} + Z_{0o})^2 \cos^2 \theta}}{2 \sin \theta}$  |  <p style="text-align: center;">Bandpass</p>  |
|  | $Z_{i1} = \frac{\sqrt{Z_{0e}Z_{0o}} \sqrt{(Z_{0e} - Z_{0o})^2 - (Z_{0e} + Z_{0o})^2 \cos^2 \theta}}{(Z_{0e} + Z_{0o}) \sin \theta}$ $Z_{i2} = \frac{Z_{0e}Z_{0o}}{Z_{i1}}$ |  <p style="text-align: center;">Bandpass</p> |



# Coupled Line Filters

- Bandpass filter with resonance at  $\theta = \pi/2$  ( $l = \lambda/4$ )

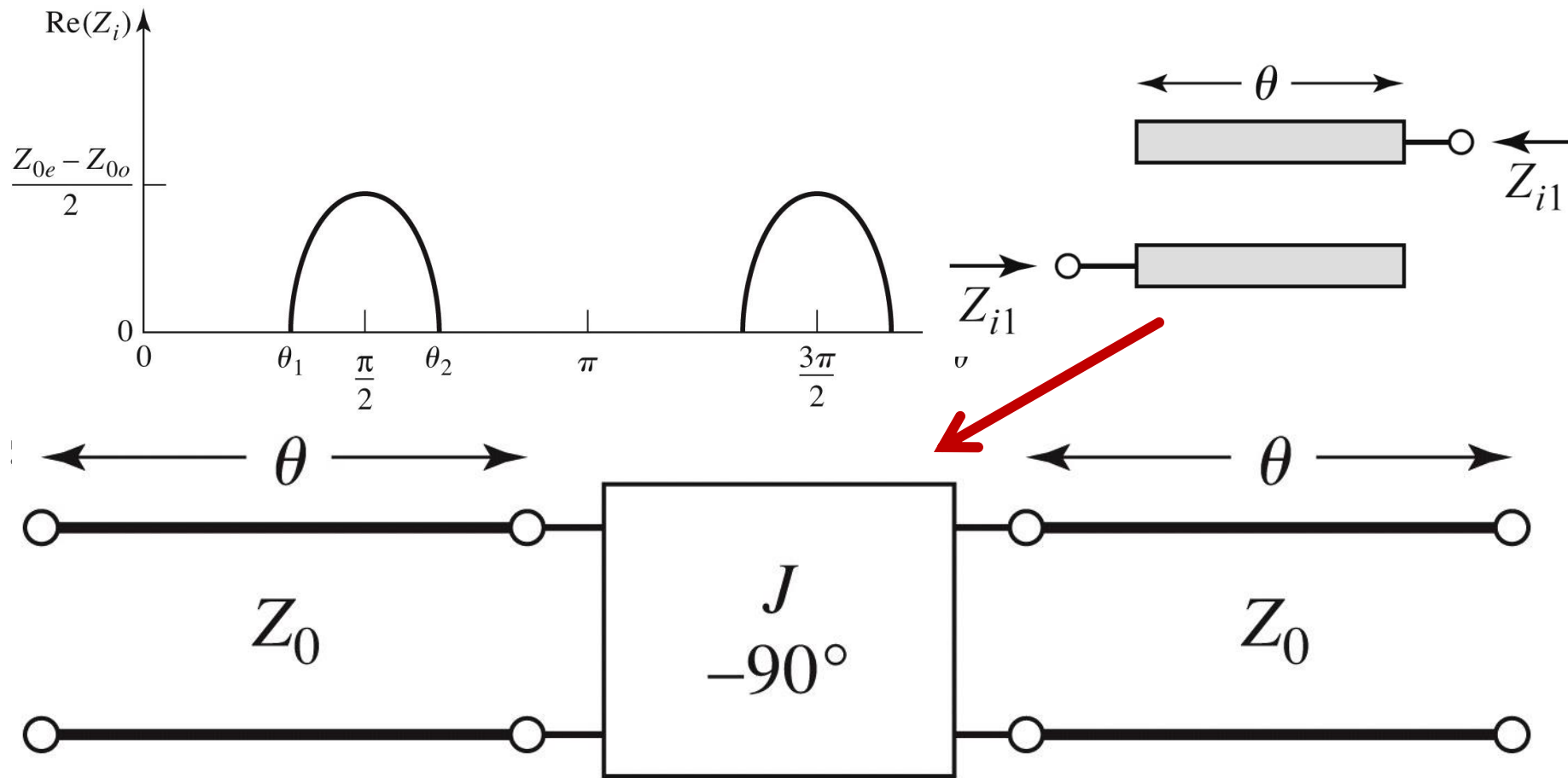
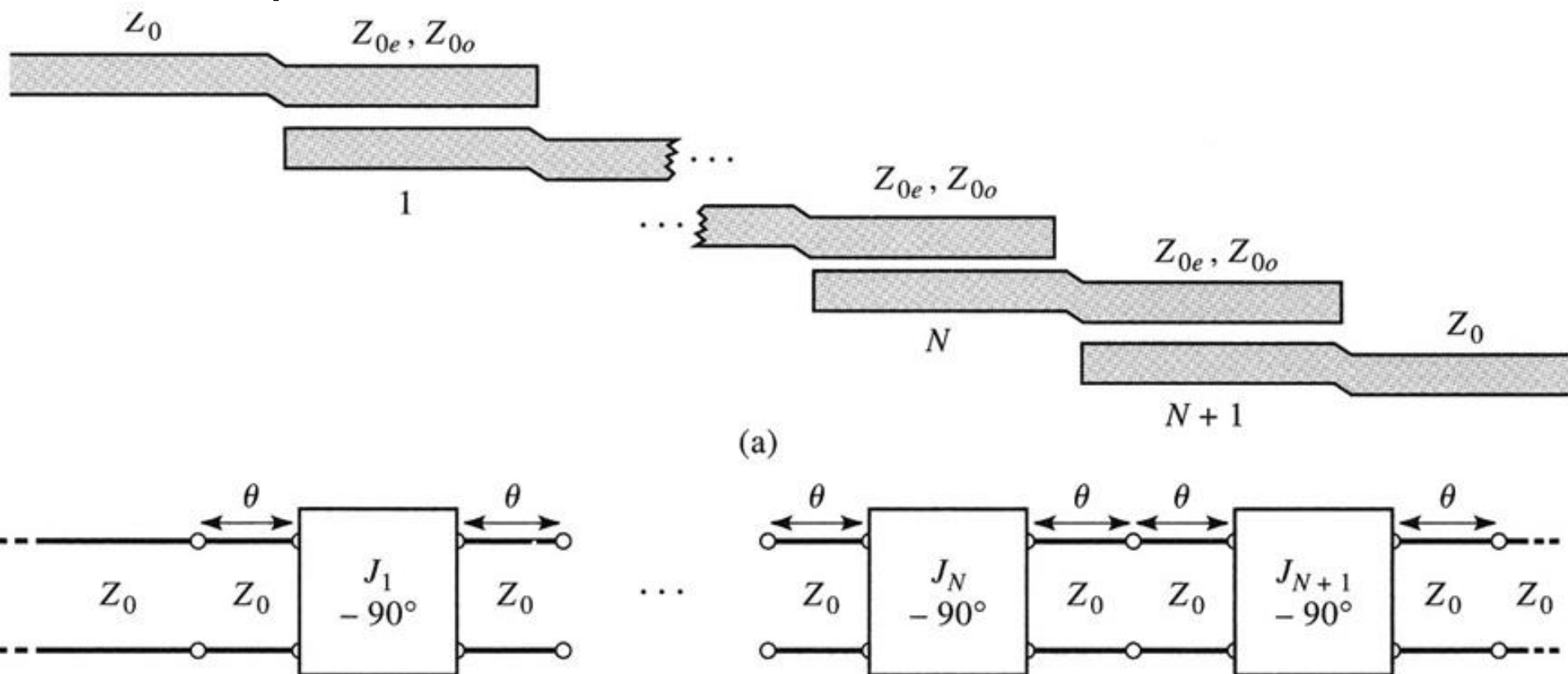


Figure 8.44

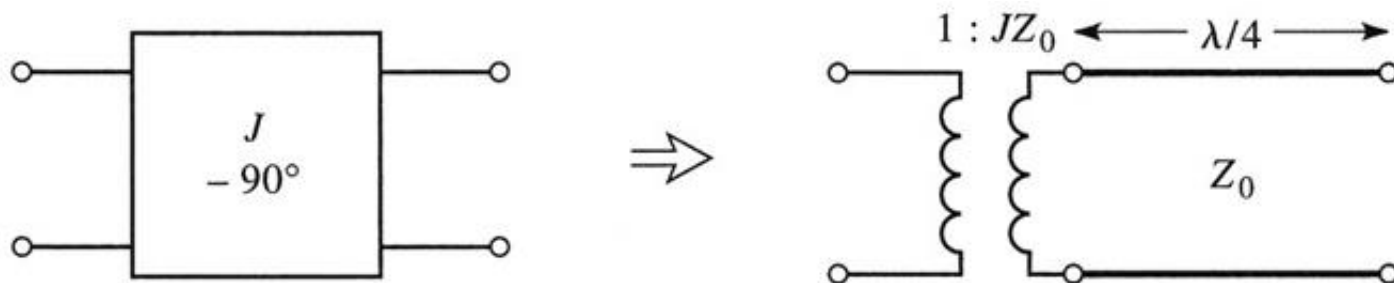
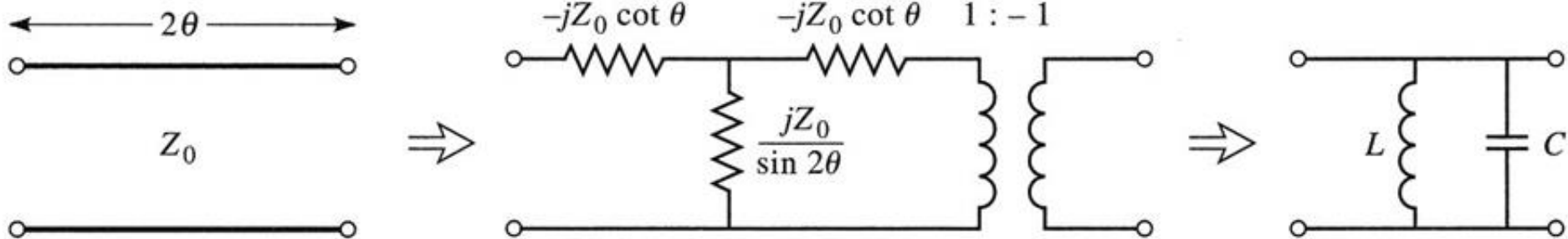
# Coupled Line Filters

- We get a  $N^{\text{th}}$  order filter with  $N+1$  parallel coupled line section



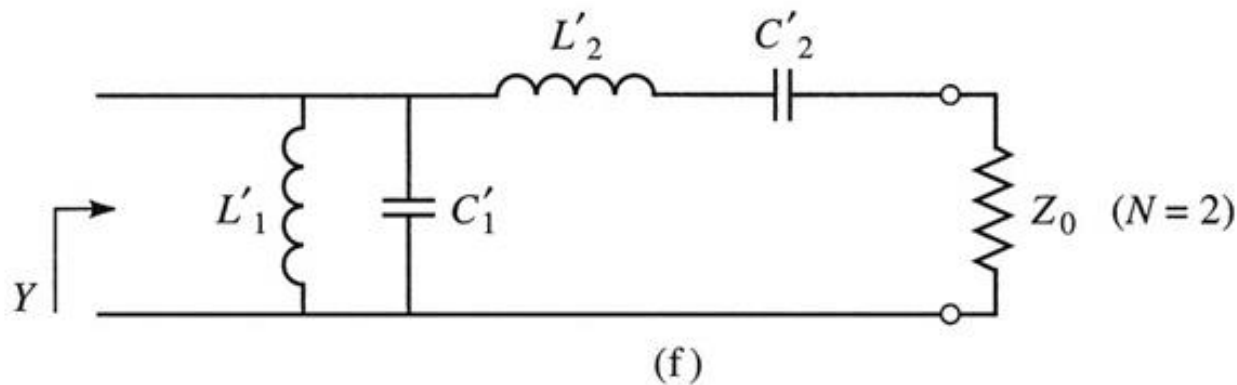
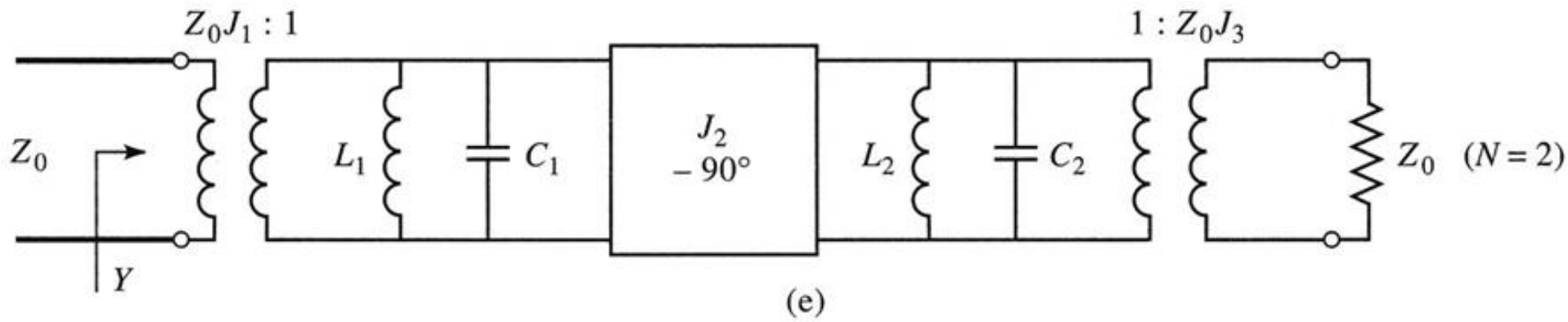
# Coupled Line Filters

- Equivalent circuits for
  - transmission lines of length  $2\theta$
  - admittance inverters



# Coupled Line Filters N=2

- We get a 2<sup>nd</sup> order BPF behavior with 3 coupled lines sections





# Coupled Line Filters design formulas

- Compute the inverters from prototype parameters

$$Z_0 \cdot J_1 = \sqrt{\frac{\pi \cdot \Delta}{2 \cdot g_1}} \quad Z_0 \cdot J_n = \frac{\pi \cdot \Delta}{2 \cdot \sqrt{g_{n-1} \cdot g_n}}, n = \overline{2, N} \quad Z_0 \cdot J_{N+1} = \sqrt{\frac{\pi \cdot \Delta}{2 \cdot g_N \cdot g_{N+1}}}$$

- Compute coupled line parameters  $Z_{oe}/Z_{oo}$  (all of length  $l = \lambda/4$ )

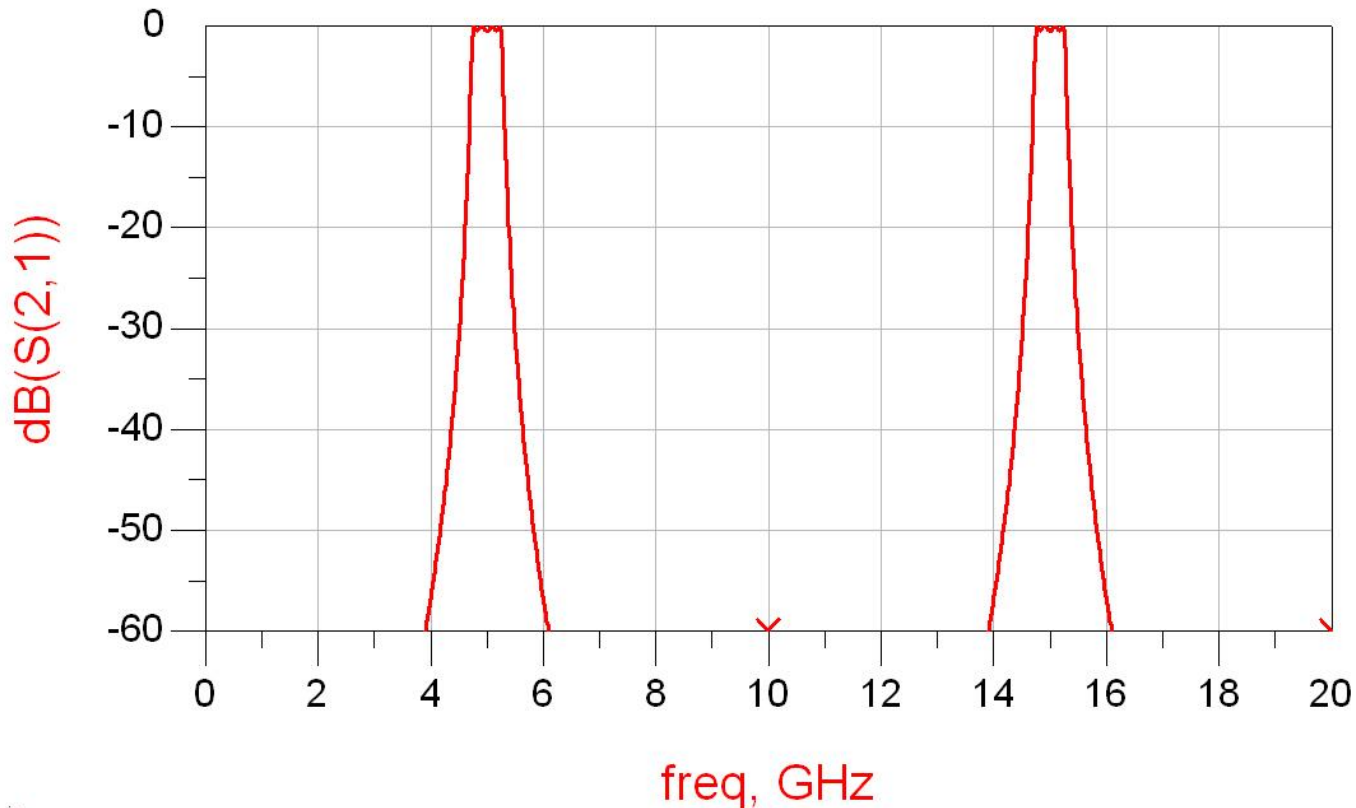
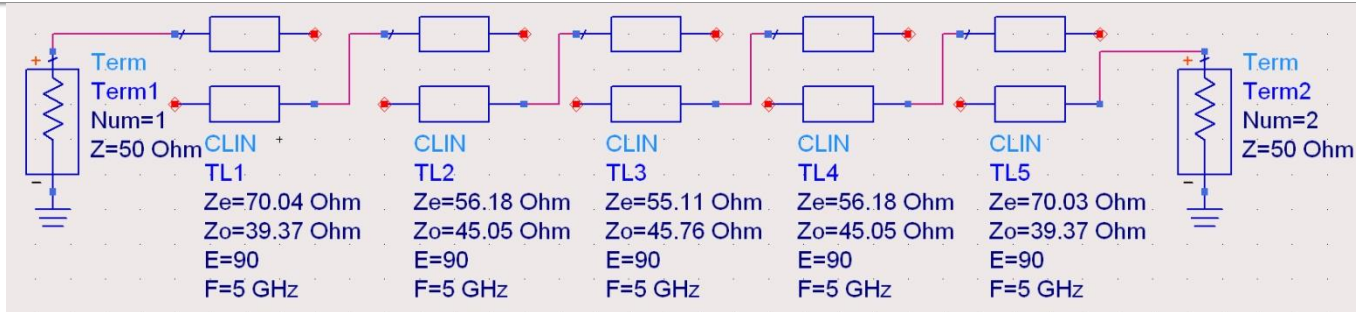
$$\begin{aligned} Z_{oe,n} &= Z_0 \cdot \left[ 1 + J_n \cdot Z_0 + (J_n \cdot Z_0)^2 \right] \\ Z_{oo,n} &= Z_0 \cdot \left[ 1 - J_n \cdot Z_0 + (J_n \cdot Z_0)^2 \right] \end{aligned} \quad n = \overline{1, N+1}$$

# Example

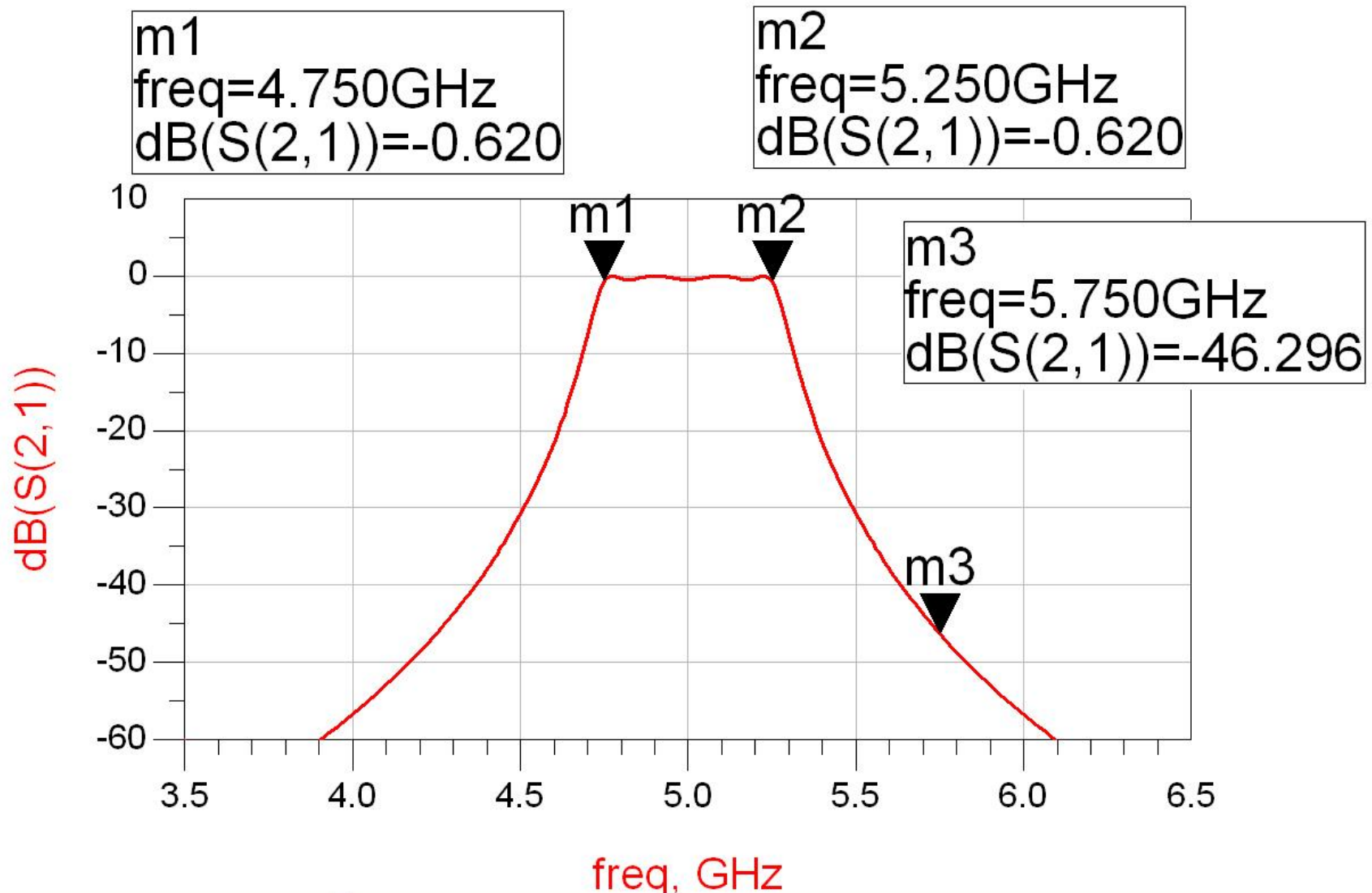
- Similar to a project assignment
- Follows the amplifier designed as in L10
- 4<sup>th</sup> order bandpass filter,  $f_0 = 5\text{GHz}$ , fractional bandwidth of the passband 10 %
- 0.5dB equal-ripple table for  $g_n$  followed by filter design formulas

| n | g      | ZoJn     | Zoe   | Zoo   |
|---|--------|----------|-------|-------|
| 1 | 1.6703 | 0.306664 | 70.04 | 39.37 |
| 2 | 1.1926 | 0.111295 | 56.18 | 45.05 |
| 3 | 2.3661 | 0.09351  | 55.11 | 45.76 |
| 4 | 0.8419 | 0.111294 | 56.18 | 45.05 |
| 5 | 1.9841 | 0.306653 | 70.03 | 39.37 |

# ADS – coupled line BPF



# ADS – coupled line BPF



# Examples

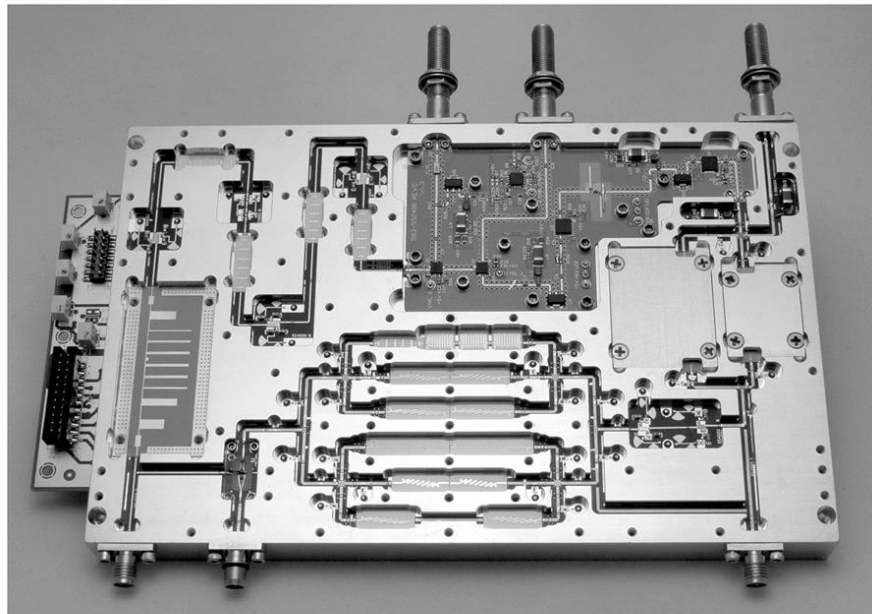
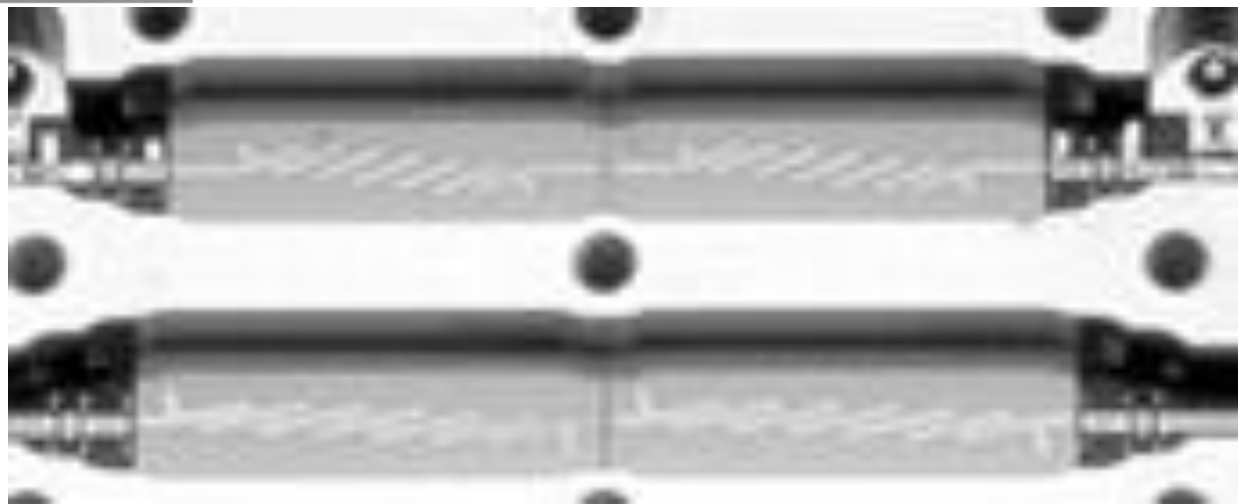
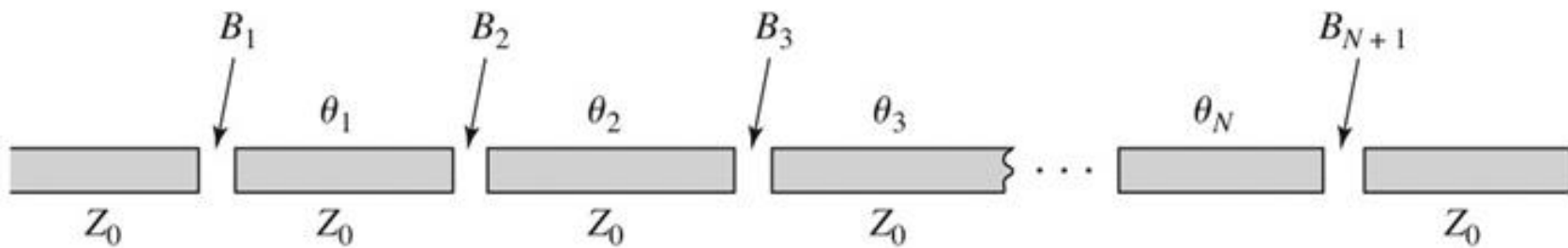


Figure 8.55  
Courtesy of LNX Corporation, Salem, N.H.

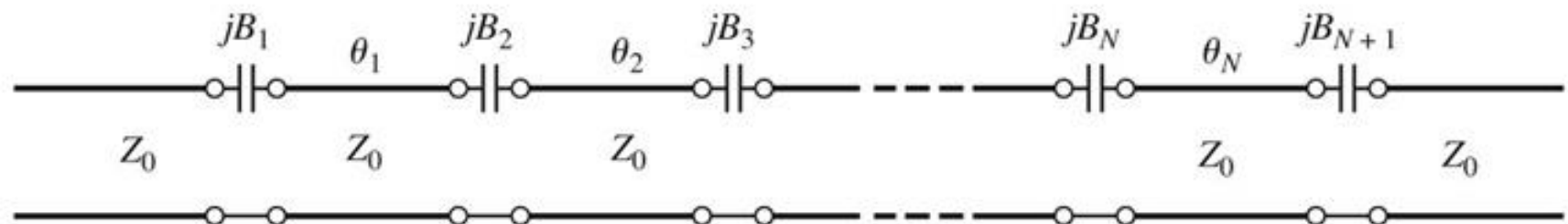


# Bandpass Filters Using Capacitively Coupled Series Resonators

- The gaps between the resonators ( $\sim \lambda/2$ ) generate a capacitive coupling between two resonators and can be approximated as series capacitors



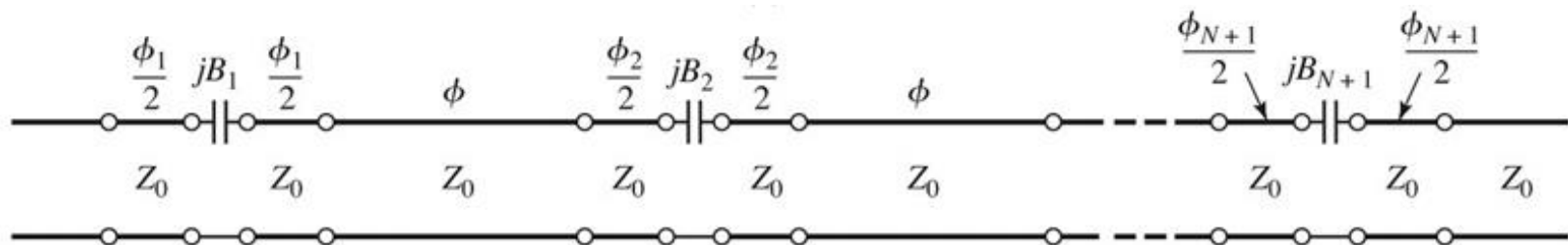
(a)



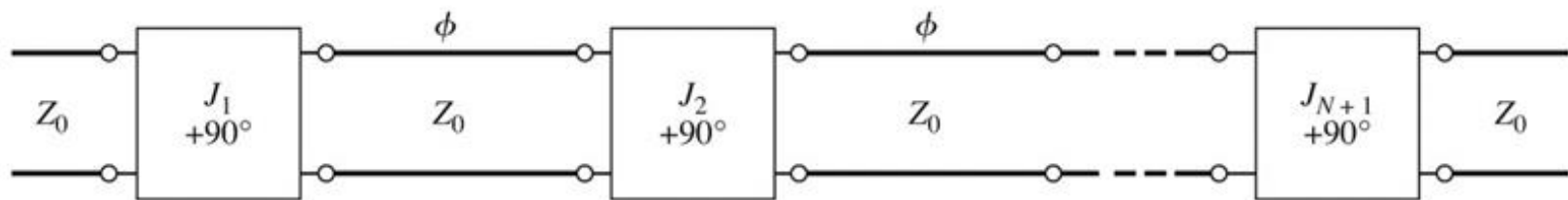
(b)

# Bandpass Filters Using Capacitively Coupled Series Resonators

- From the real physical length of the resonators, some part is used implement a admittance inverter (the remainder  $\phi = \pi$ ,  $l = \lambda/2$ , resonator)



(c)



(d)

Figure 8.50

# Bandpass Filters Using Capacitively Coupled Series Resonators design

- Compute the inverters (similar to coupled lines)

$$Z_0 \cdot J_1 = \sqrt{\frac{\pi \cdot \Delta}{2 \cdot g_1}} \quad Z_0 \cdot J_n = \frac{\pi \cdot \Delta}{2 \cdot \sqrt{g_{n-1} \cdot g_n}}, n = \overline{2, N} \quad Z_0 \cdot J_{N+1} = \sqrt{\frac{\pi \cdot \Delta}{2 \cdot g_N \cdot g_{N+1}}}$$

- Compute capacitive susceptances

$$B_n = \frac{J_n}{1 - (Z_0 \cdot J_n)^2}, n = \overline{1, N+1}$$

- Compute the line lengths that must be “borrowed” to implement the inverters

$$\phi_n = -\tan^{-1}(2 \cdot Z_0 \cdot B_n), n = \overline{1, N+1} \quad \phi_n < 0, n = \overline{1, N+1}$$

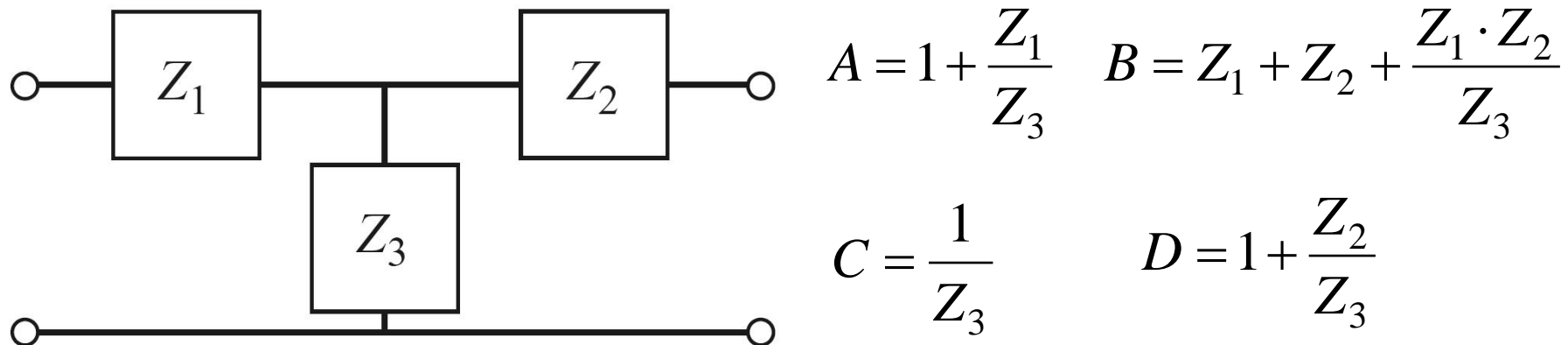
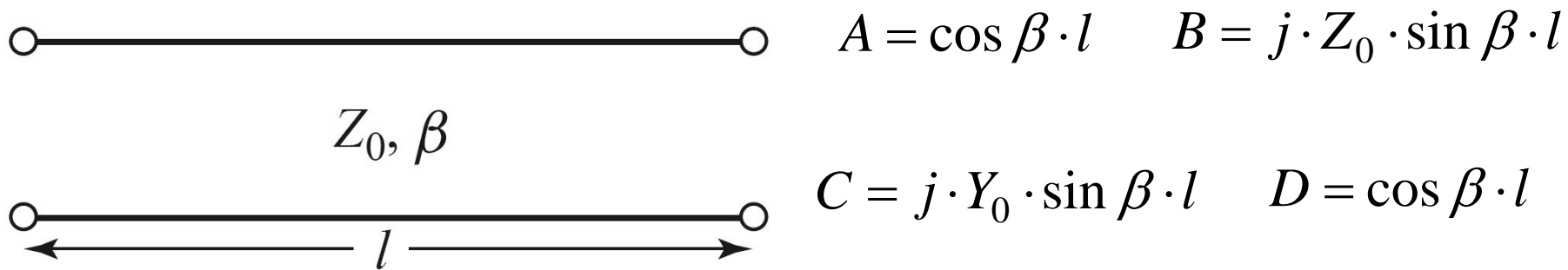
- Compute the actual length of the lines ( $\lambda/2 + \text{borr.}$ )

$$\theta_i = \pi + \frac{1}{2} \cdot (\phi_i + \phi_{i+1}) = \pi - \frac{1}{2} \cdot \left[ \tan^{-1}(2 \cdot Z_0 \cdot B_i) + \tan^{-1}(2 \cdot Z_0 \cdot B_{i+1}) \right], i = \overline{1, N}$$



# Equivalent circuits for short sections of transmission lines

- ABCD matrix (L5)
- short line, model with lumped elements is valid



# Equivalent circuits for short sections of transmission lines

- The shunt element is capacitive

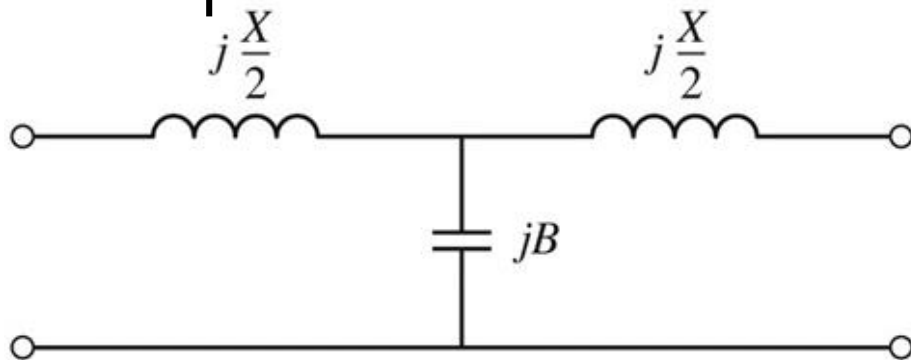
$$Z_3 = \frac{1}{j \cdot Y_0 \cdot \sin \beta \cdot l}$$

- Series elements are equal, and inductive

$$\cos \beta \cdot l = 1 + \frac{Z_1}{Z_3} = 1 + \frac{Z_2}{Z_3}$$

$$Z_1 = Z_2 = Z_3 \cdot (\cos \beta \cdot l - 1) = -j \cdot Z_0 \cdot \frac{\cos \beta \cdot l - 1}{\sin \beta \cdot l} = j \cdot Z_0 \cdot \tan \frac{\beta \cdot l}{2}$$

- Equivalent circuit



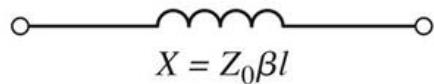
$$\frac{X}{2} = Z_0 \cdot \tan \frac{\beta \cdot l}{2}$$

$$B = \frac{1}{Z_0} \cdot \sin \beta \cdot l$$

# Equivalent circuits for short sections of transmission lines

- depending on the characteristic impedance:

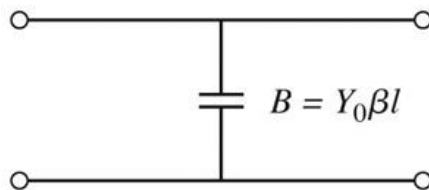
- high  $Z_0 \gg$



$$X \cong Z_0 \cdot \beta \cdot l \quad \beta \cdot l < \frac{\pi}{4} \quad Z_0 = Z_h$$



- low  $Z_0 \ll$



$$B \cong Y_0 \cdot \beta \cdot l \quad \beta \cdot l < \frac{\pi}{4} \quad Z_0 = Z_l$$

# Stepped-impedance low-pass filter

- Series L, shunt C, we realize low-pass filters
- We use

- lines with high characteristic impedance to implement an series inductor

$$\beta \cdot l = \frac{L \cdot R_0}{Z_h}$$

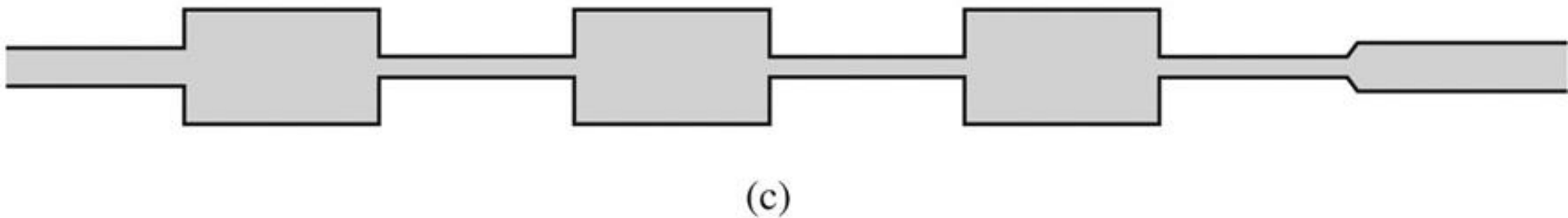
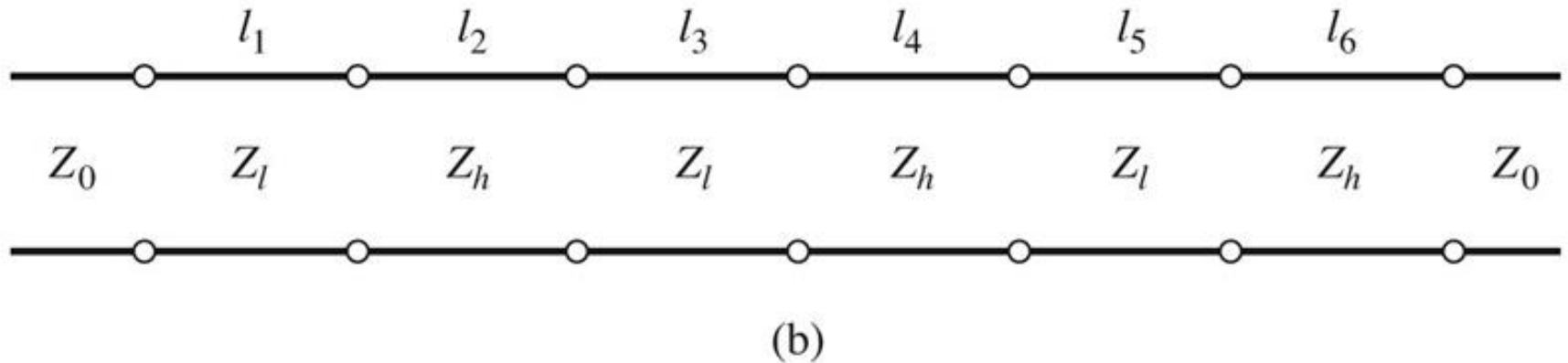
- lines with low characteristic impedance to implement a shunt capacitor

$$\beta \cdot l = \frac{C \cdot Z_l}{R_0}$$

- usually the highest and lowest characteristic impedance that can be practically fabricated

# Stepped-impedance LPF

- Not all the lines will result with the same length so the filter response is not periodic in frequency

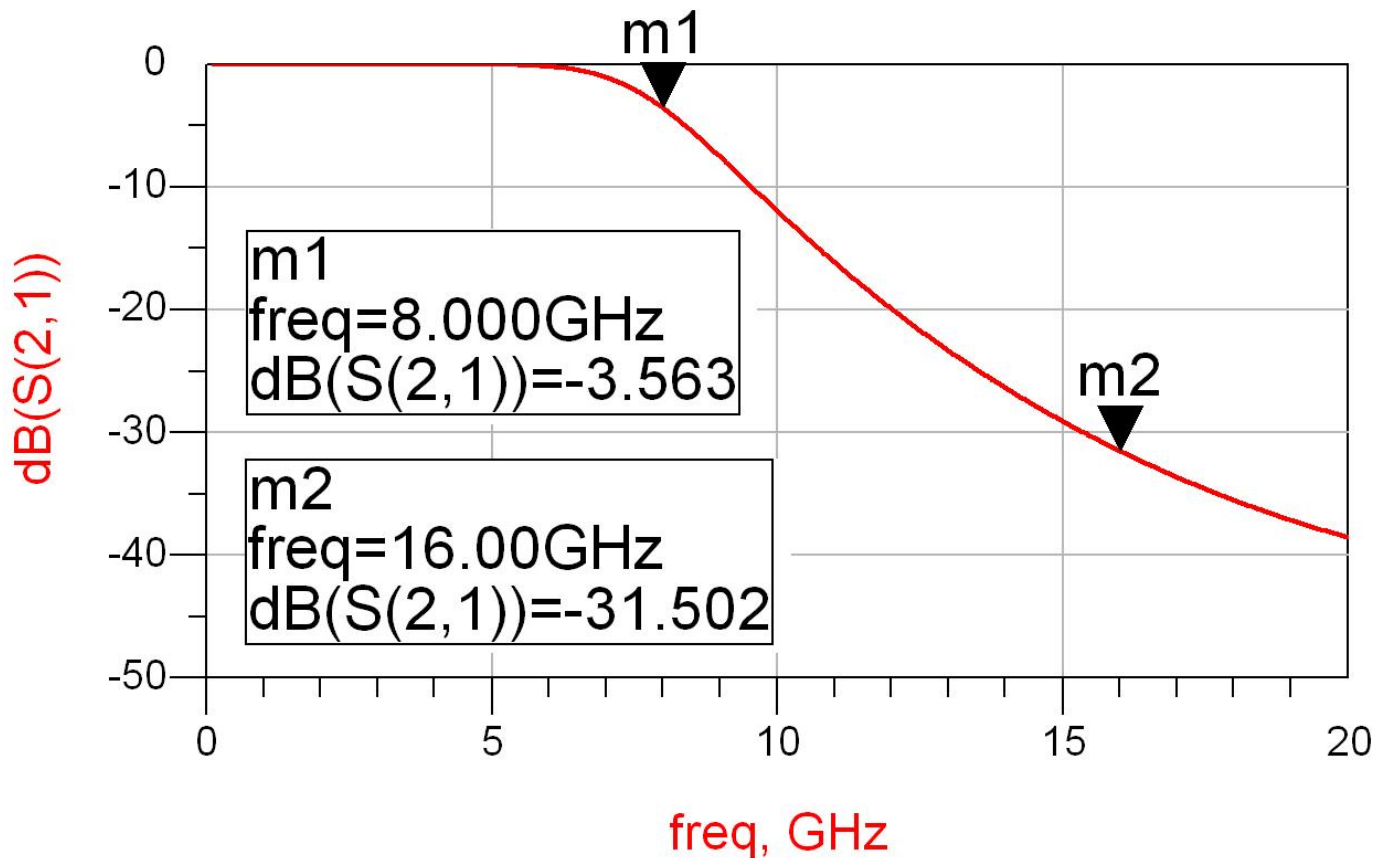
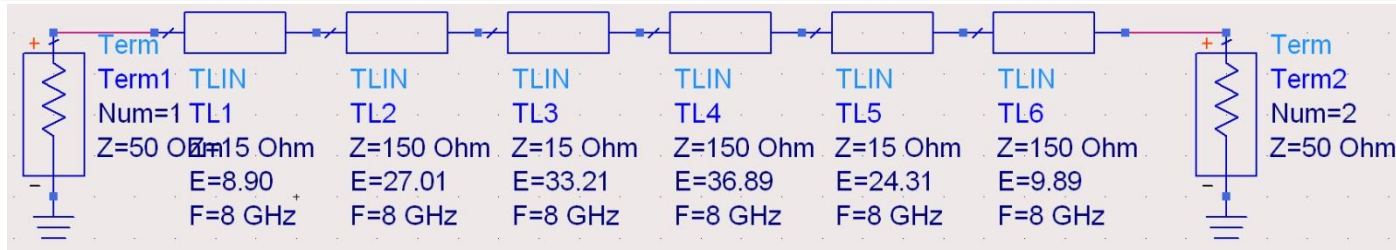


# Example

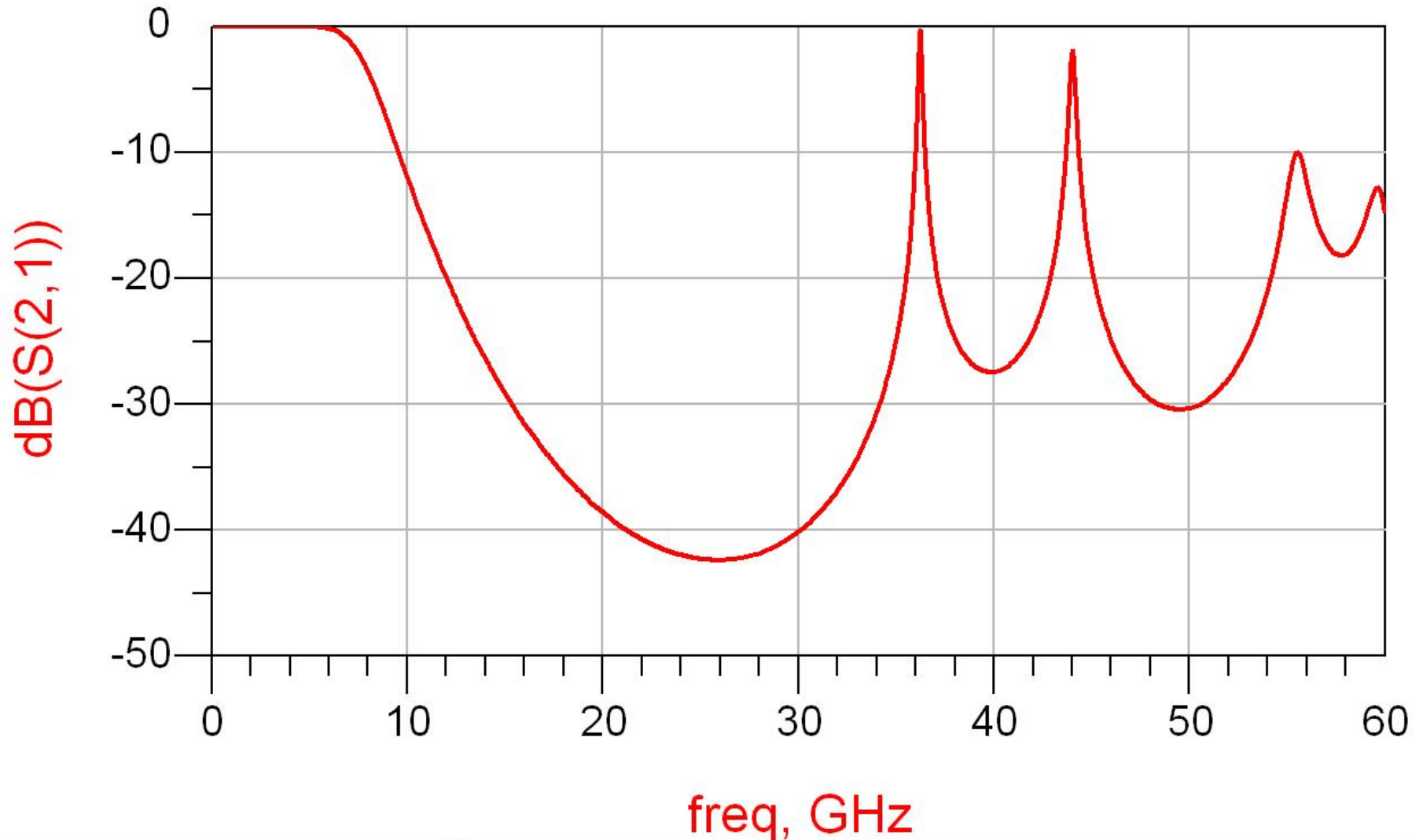
- LPF with 8GHz cutoff frequency, 6<sup>th</sup> order. Maximum realizable impedance is 150 $\Omega$  and lowest 15 $\Omega$ .

| n | $g_n$  | L/C <sub>n</sub> | Z   | $\theta_n$ [rad] | $\theta_n$ [°] |
|---|--------|------------------|-----|------------------|----------------|
| 1 | 0.5176 | 0.206pF          | 15  | 0.155            | 8.90           |
| 2 | 1.4142 | 1.407nH          | 150 | 0.471            | 27.01          |
| 3 | 1.9318 | 0.769pF          | 15  | 0.580            | 33.21          |
| 4 | 1.9318 | 1.922nH          | 150 | 0.644            | 36.89          |
| 5 | 1.4142 | 0.563pF          | 15  | 0.424            | 24.31          |
| 6 | 0.5176 | 0.515nH          | 150 | 0.173            | 9.89           |

# ADS – Stepped-impedance LPF

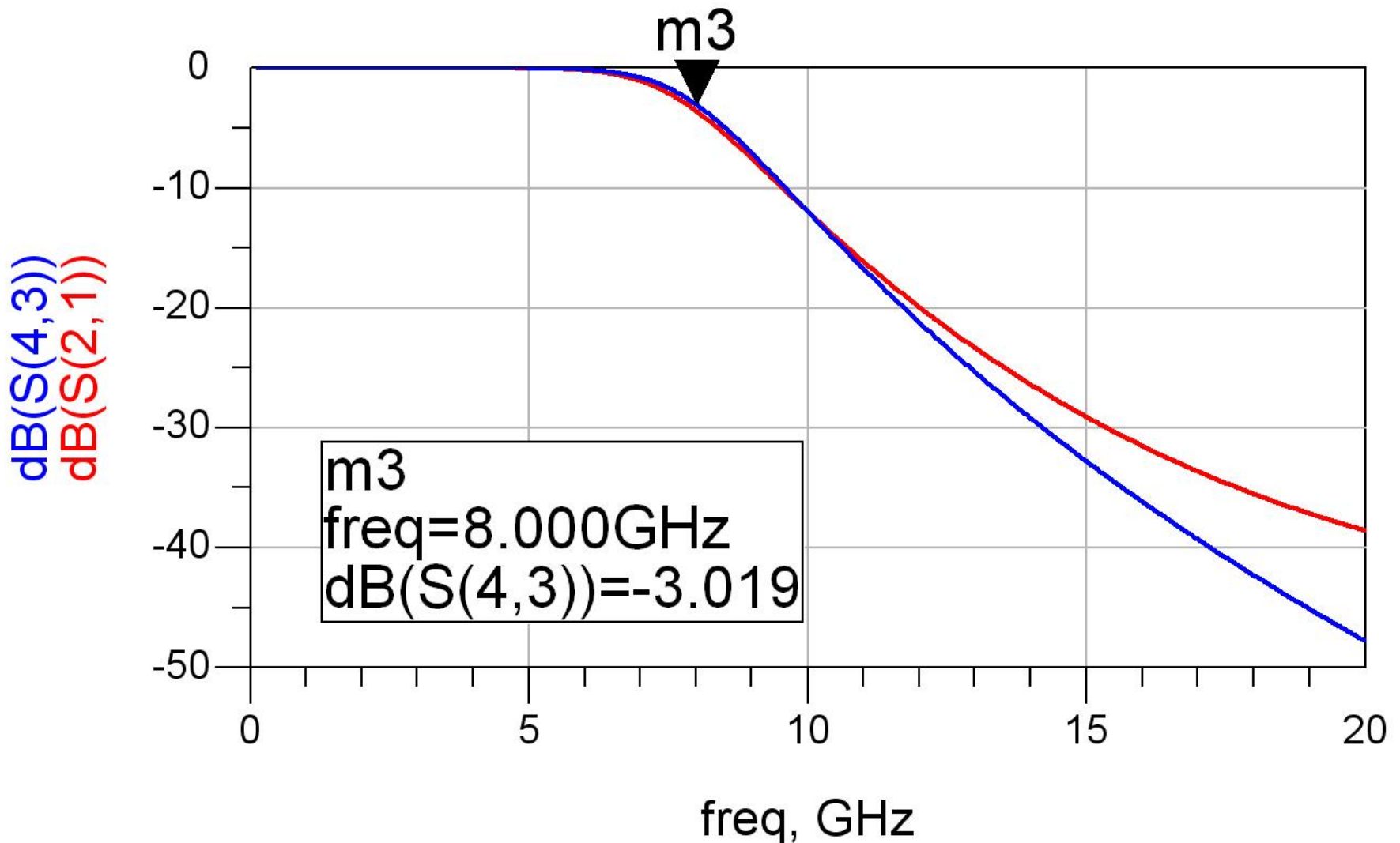


# ADS – Stepped-impedance LPF





# ADS – Stepped-impedance LPF – compared with lumped elements



# Examples

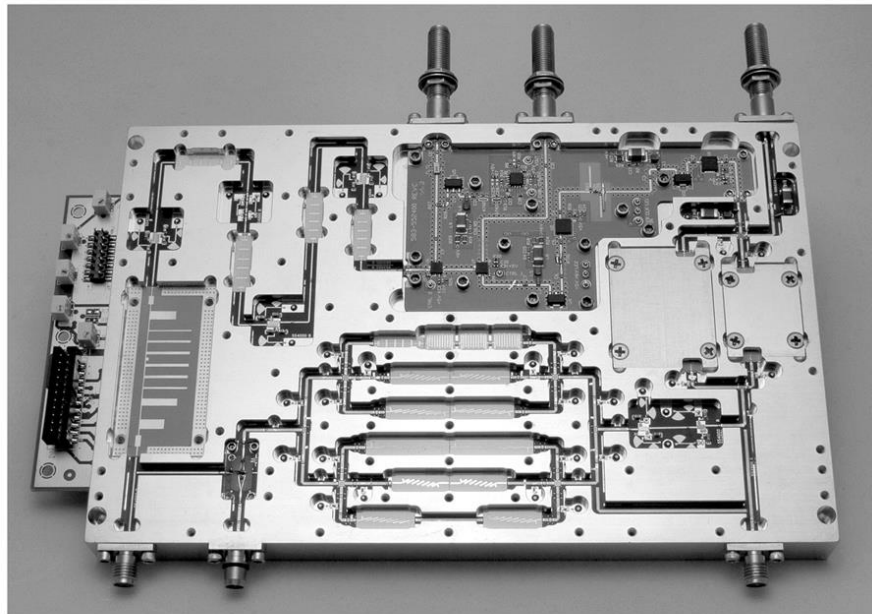
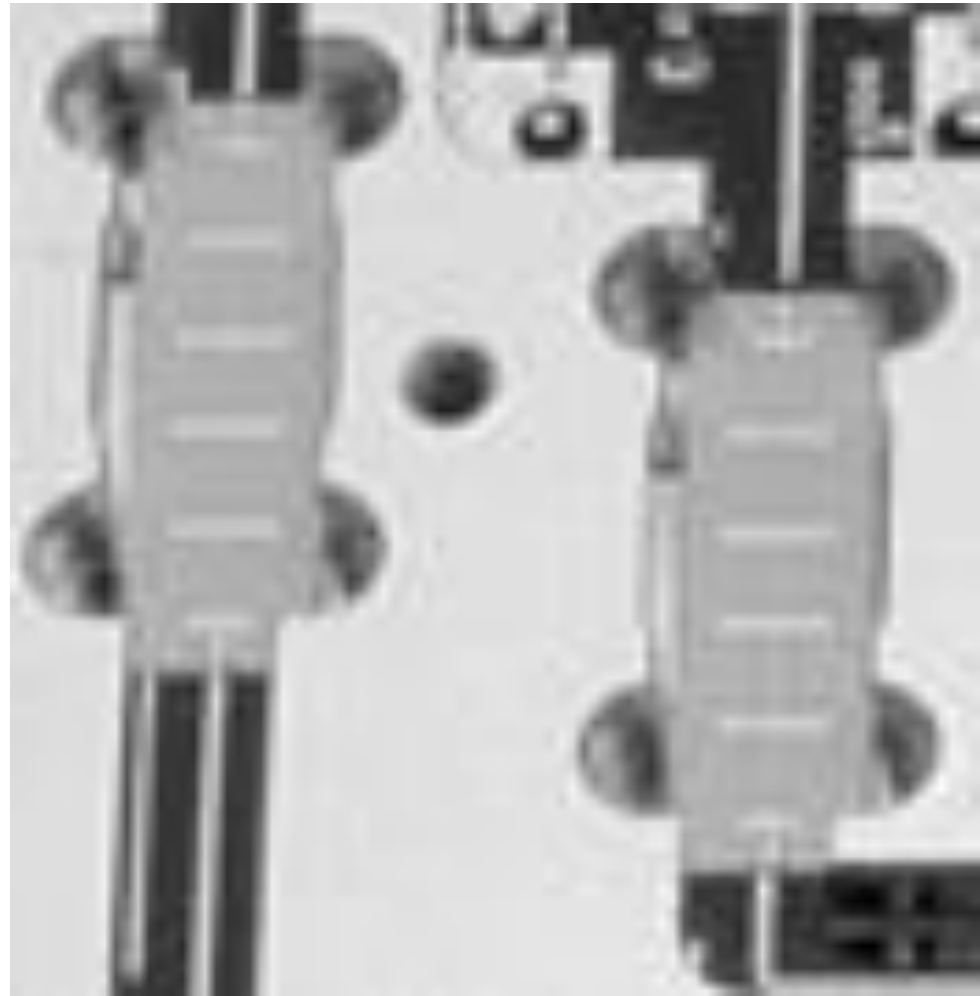


Figure 8.55  
Courtesy of LNX Corporation, Salem, N.H.



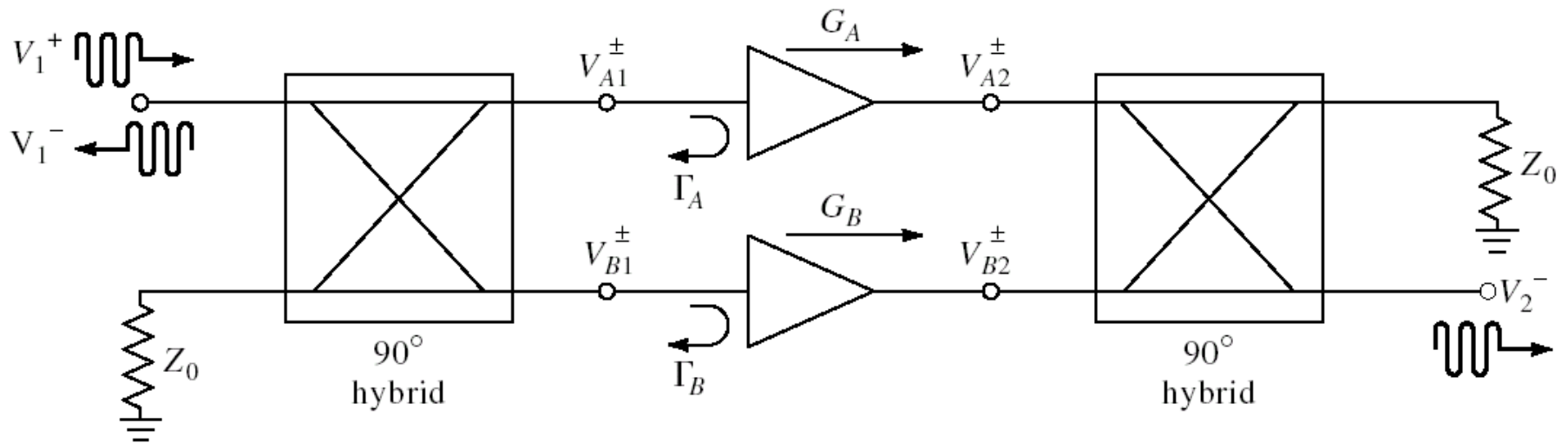
Microwave Amplifiers

# Broadband amplifiers

# Broadband/Wideband amplifiers

- Achieved by some design techniques (only at the expense of gain, complexity)
  1. Compensated matching networks
  2. Resistive matching networks
  3. Negative feedback
  4. Balanced amplifiers
  5. Distributed amplifiers
  6. Differential amplifiers

# Balanced amplifiers



- two identical amplifiers with two hybrid couplers  
3 dB / 90° to cancel input and output reflections

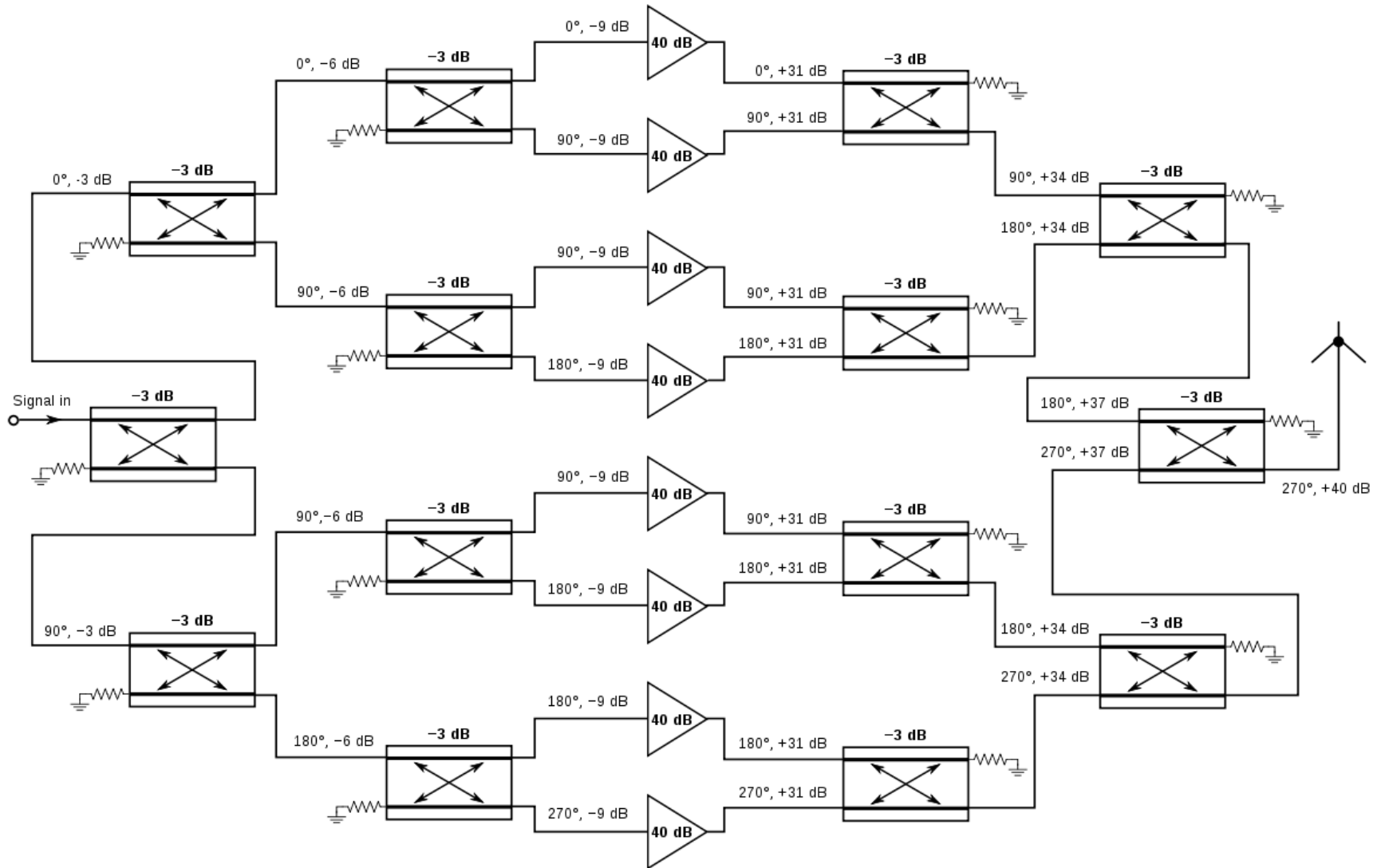
$$S_{21} = \frac{-j}{2} \cdot (G_A + G_B)$$

$$S_{21}|_{A=B} = -j \cdot G$$

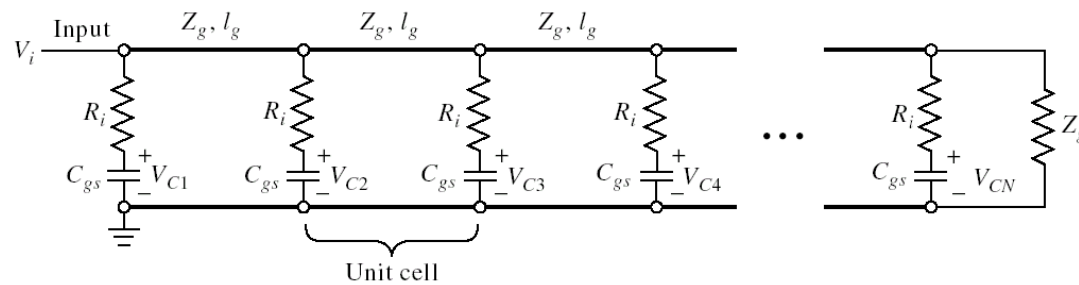
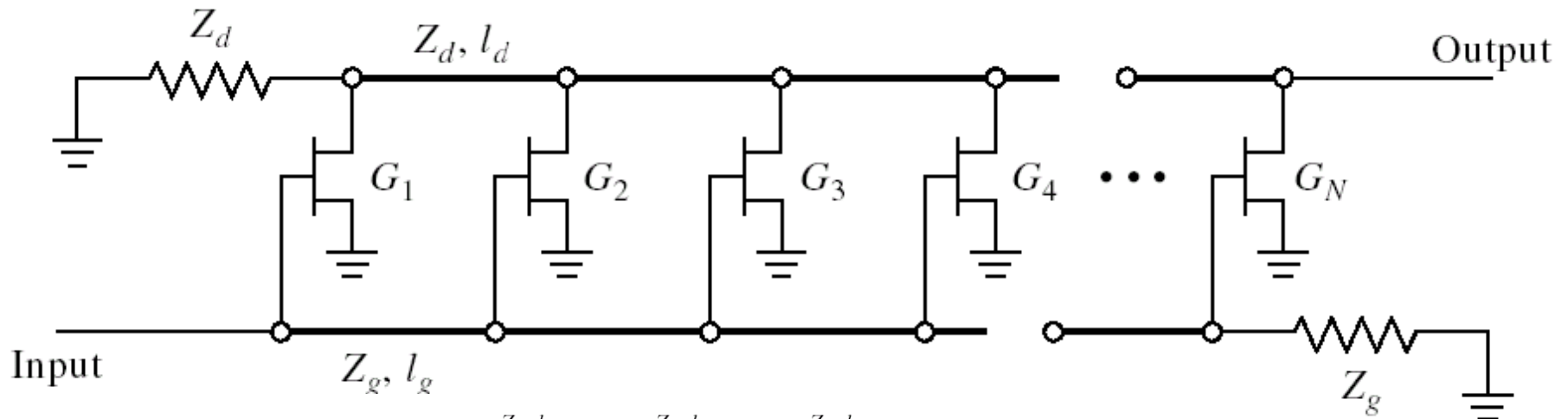
$$S_{11} = \frac{1}{2} \cdot (\Gamma_A - \Gamma_B) \quad F = \frac{1}{2} \cdot (F_A + F_B)$$

$$S_{11}|_{A=B} = 0$$

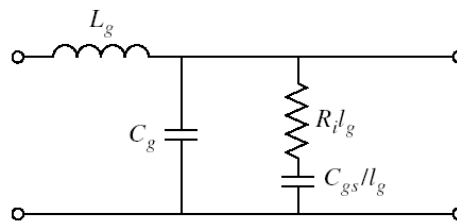
# Balanced amplifiers



# Distributed amplifiers



(a)



(b)

# Distributed amplifiers

- the phase delays on the gate (input) and drain (output) lines are synchronized

$$\gamma_g = \alpha_g + j \cdot \beta_g \quad \gamma_d = \alpha_d + j \cdot \beta_d \quad \beta_g \cdot l_g = \beta_d \cdot l_d$$

- Power gain

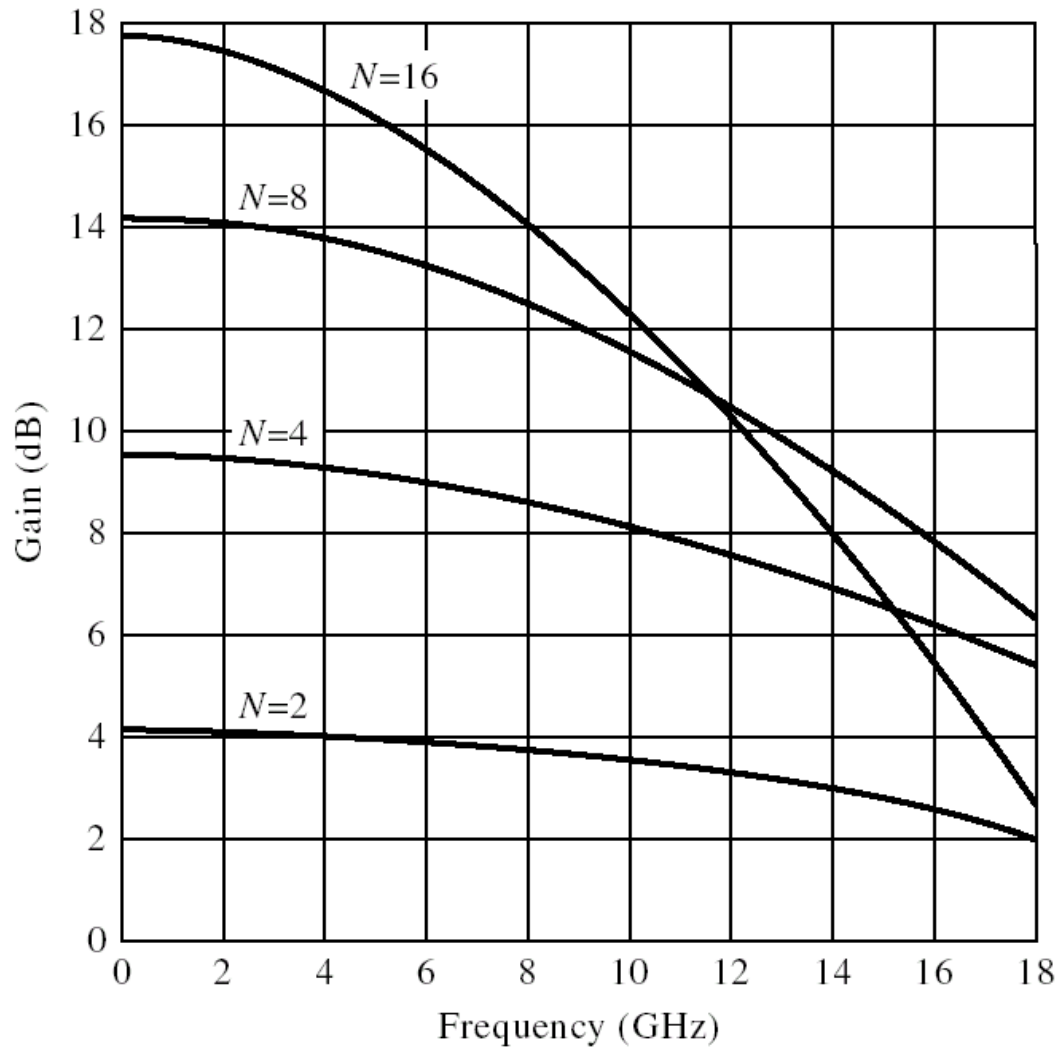
$$G = \frac{g_m^2 \cdot Z_d \cdot Z_g}{4} \cdot \frac{\left( e^{-N \cdot \alpha_g \cdot l_g} - e^{-N \cdot \alpha_d \cdot l_d} \right)^2}{\left( e^{-\alpha_g \cdot l_g} - e^{-\alpha_d \cdot l_d} \right)^2}$$

- Lossless power gain

$$G = \frac{g_m^2 \cdot Z_d \cdot Z_g \cdot N^2}{4}$$



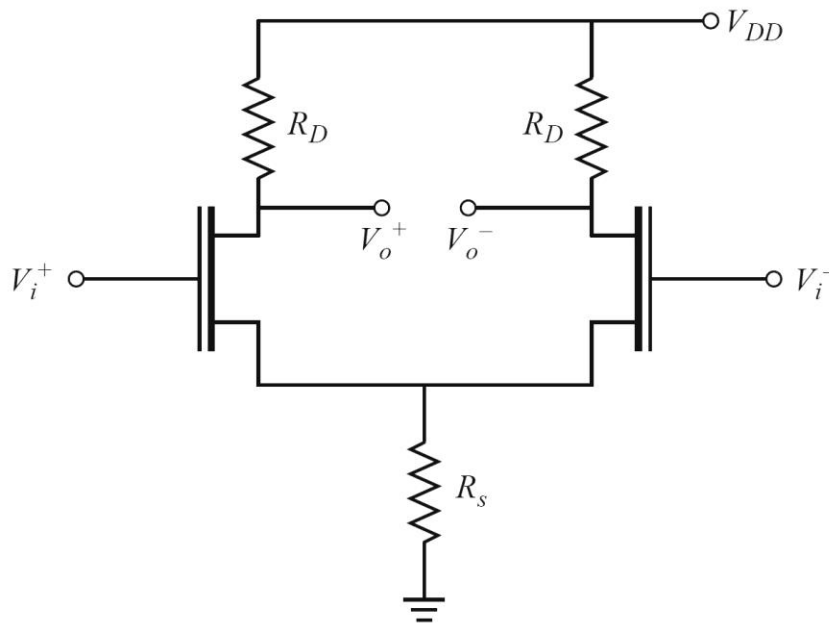
# Distributed amplifiers



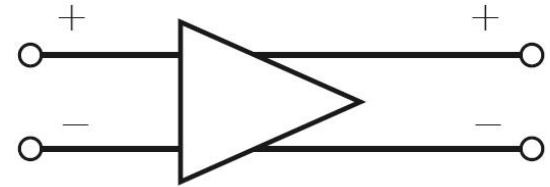
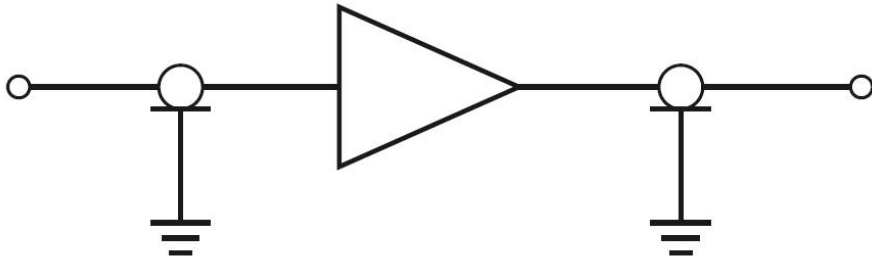
$$N_{opt} = \frac{\ln(\alpha_g \cdot l_g) - \ln(\alpha_d \cdot l_d)}{\alpha_g \cdot l_g - \alpha_d \cdot l_d}$$

# Differential amplifiers

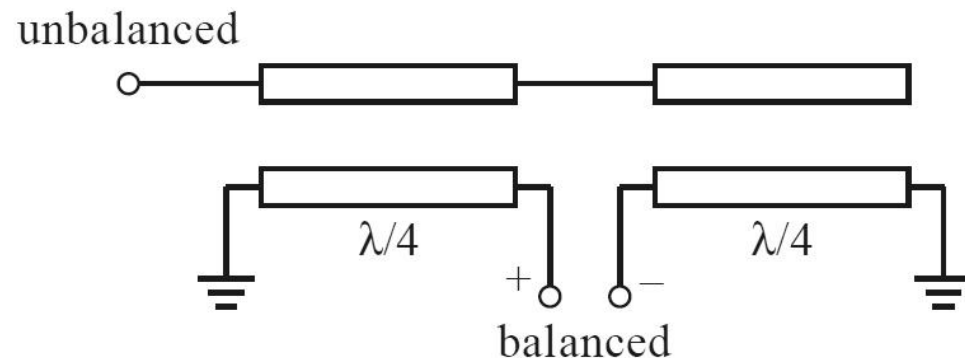
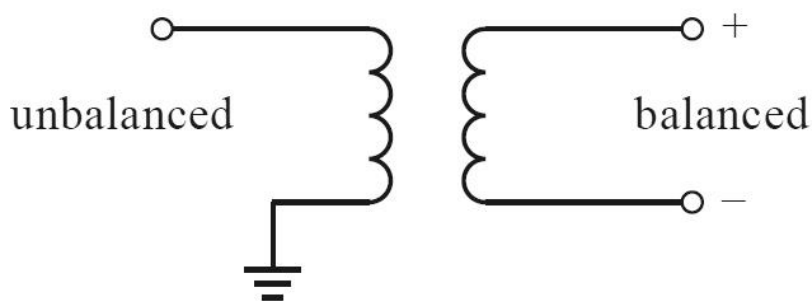
- In differential mode the input capacitances of the two transistors are connected in series
- Unity gain frequency is doubled



# Differential amplifiers

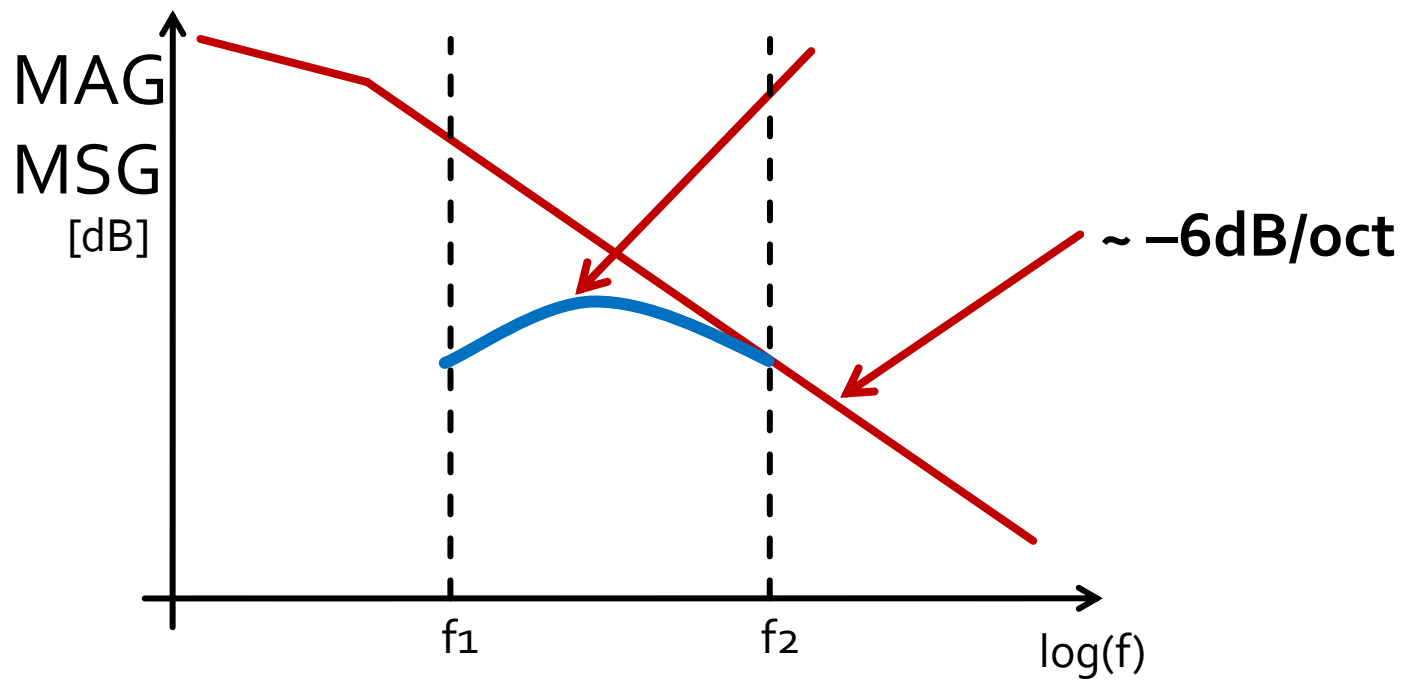


- We use circuits to transition from an unbalanced signal to a balanced signal (or vice versa)
  - hybrid couplers  $3\text{dB} / 180^\circ$
  - "balun" (balanced - unbalanced)



# Compensated matching networks

- Control the design of the matching networks at more (at least 2) frequencies and impose the same gain

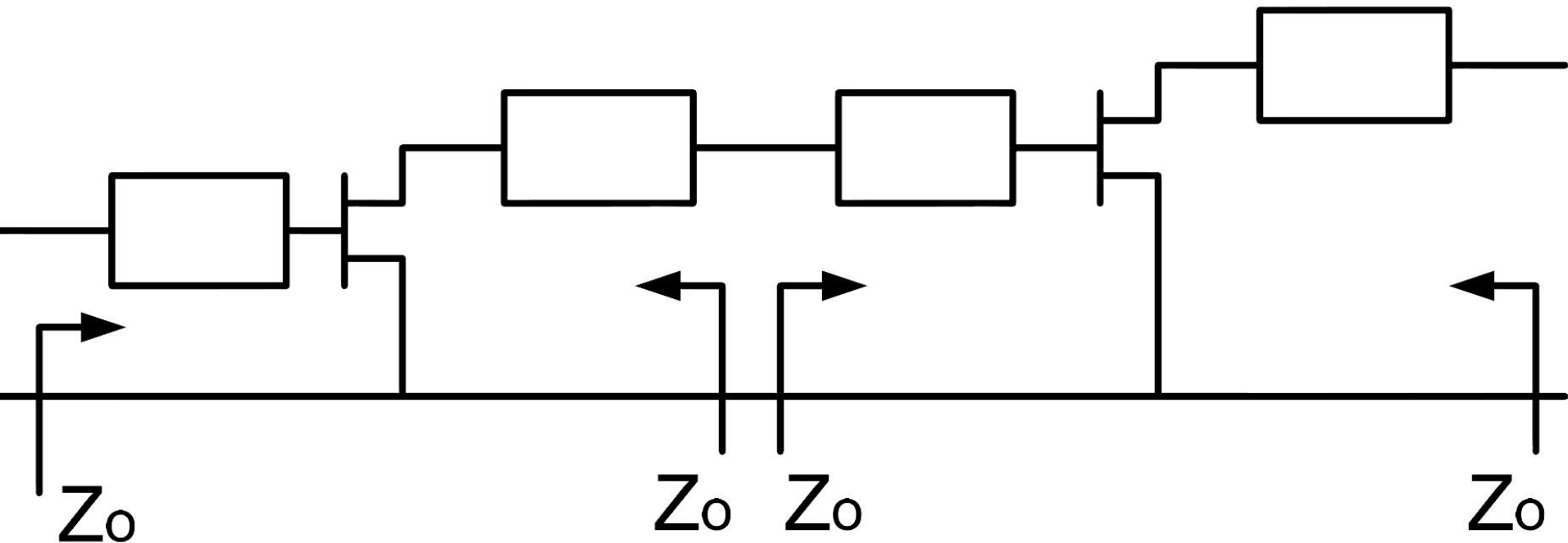


Microwave Amplifiers

# Multistage Amplifier Design

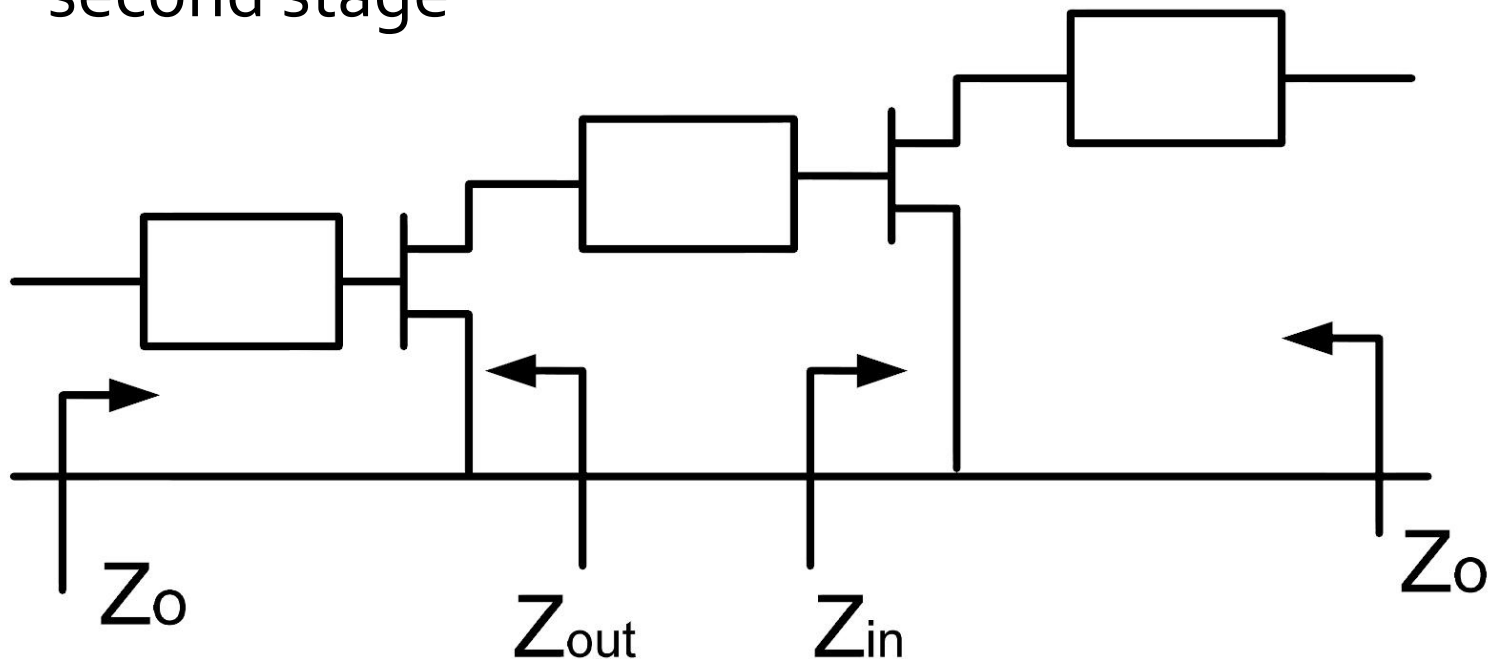
# Multistage amplifiers

- Interstage matching can be designed in two modes:
  - Each stage is matched to a virtual  $\Gamma = 0$



# Multistage amplifiers

- Interstage matching can be designed in two modes:
  - One stage is matched to offer necessary  $\Gamma$  for the second stage



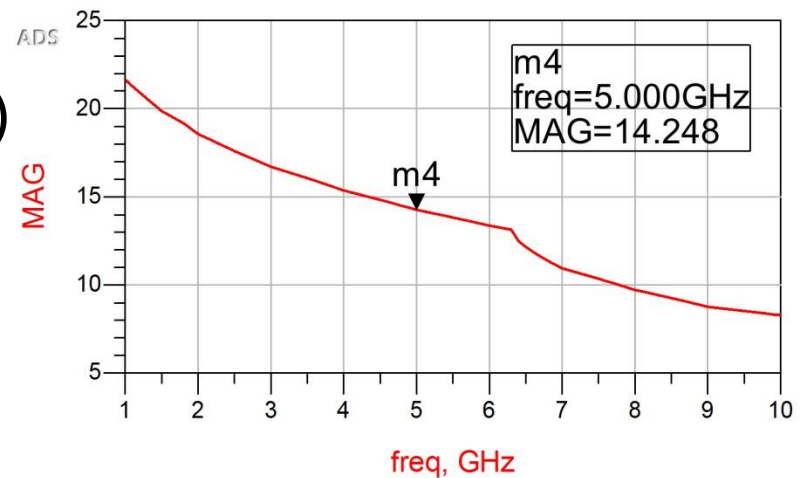
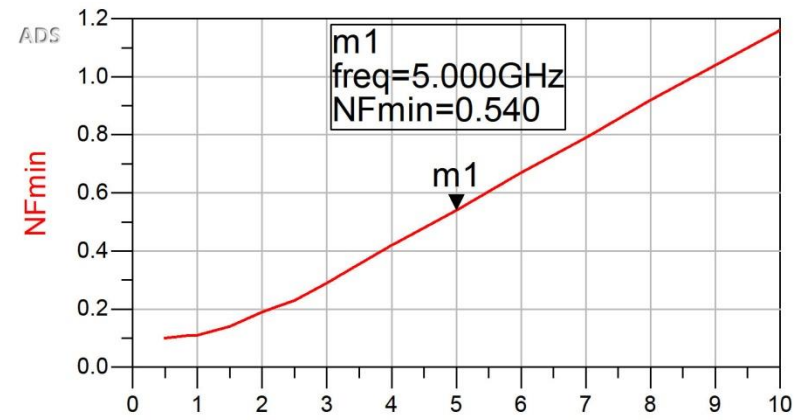
# Example multistage LNA

- Similar to the project assignment
- LNA using ATF-34143 providing:
  - $G = 20\text{dB}$
  - $F = 1\text{dB}$
  - $@f = 5\text{GHz}$



# Example

- ATF-34143 at  $V_{ds}=3V$   $I_d=20mA$ .
- @5GHz
  - $S_{11} = 0.64 \angle 139^\circ$
  - $S_{12} = 0.119 \angle -21^\circ$
  - $S_{21} = 3.165 \angle 16^\circ$
  - $S_{22} = 0.22 \angle 146^\circ$
  - $F_{min} = 0.54$  (typically[dB] !)
  - $\Gamma_{opt} = 0.45 \angle 174^\circ$
  - $r_n = 0.03$



# Example, LNA @ 5 GHz

- ATF-34143 at  $V_{ds}=3V$   $I_d=20mA$ .
- @5GHz
  - $S_{11} = 0.64 \angle 139^\circ$
  - $S_{12} = 0.119 \angle -21^\circ$
  - $S_{21} = 3.165 \angle 16^\circ$  →
  - $S_{22} = 0.22 \angle 146^\circ$
  - $F_{min} = 0.54$  (tipic [dB])
  - $\Gamma_{opt} = 0.45 \angle 174^\circ$
  - $r_n = 0.03$  →

```

IATF-34143
IS-PARAMETERS at Vds=3V Id=20mA. LAST UPDATED 01-29-99

# ghz s ma r 50

2.0 0.75 -126 6.306 90 0.088 23 0.26 -120
2.5 0.72 -145 5.438 75 0.095 15 0.25 -140
3.0 0.69 -162 4.762 62 0.102 7 0.23 -156
4.0 0.65 166 3.806 38 0.111 -8 0.22 174
5.0 0.64 139 3.165 16 0.119 -21 0.22 146
6.0 0.65 114 2.706 -5 0.125 -35 0.23 118
7.0 0.66 89 2.326 -27 0.129 -49 0.25 91
8.0 0.69 67 2.017 -47 0.133 -62 0.29 67
9.0 0.72 48 1.758 -66 0.135 -75 0.34 46

IFREQ Fopt GAMMA OPT RN/Zo
IGHZ dB MAG ANG -
2.0 0.19 0.71 66 0.09
2.5 0.23 0.65 83 0.07
3.0 0.29 0.59 102 0.06
4.0 0.42 0.51 138 0.03
5.0 0.54 0.45 174 0.03
6.0 0.67 0.42 -151 0.05
7.0 0.79 0.42 -118 0.10
8.0 0.92 0.45 -88 0.18
9.0 1.04 0.51 -63 0.30
10.0 1.16 0.61 -43 0.46
    
```

# Multistage amplifiers

- If we need more power gain than only one transistor can supply
  - design target 20dB
  - $MAG @ 5GHz = 14.248 \text{ dB} < 20\text{dB}$
- We use Friis formula to separate the target:
  - Power gain
  - Noise
- on two amplifier stages

# Friis Formula (noise)

$$F_{cas} = F_1 + \frac{F_2 - 1}{G_1} + \frac{F_3 - 1}{G_1 \cdot G_2} + \frac{F_4 - 1}{G_1 \cdot G_2 \cdot G_3} + \dots$$

- Effects of Friis Formula:
  - it's essential that the first stage is as **noiseless** as possible even if that means sacrificing power
  - the second stage can be optimized for power **gain**
- Friis Formula **must** be used in **linear scale!**
- **Avago/Broadcom AppCAD**
  - AppCAD Free Design Assistant Tool for Microsoft Windows → Google

# Friis Formula (noise)

$$G_{cas} = G_1 \cdot G_2$$

$$F_{cas} = F_1 + \frac{1}{G_1} (F_2 - 1)$$

- Friis formula
  - first stage: low noise factor, probably resulting in a smaller gain
  - second stage: high gain, probably resulting in higher noise factor
- It's essential to introduce a design margin (reserve:  $\Delta F$ ,  $\Delta G$ )
  - $G = G_{design} + \Delta G$
  - $F = F_{design} - \Delta F$
- Interpretation of the design target
  - $G > G_{design}$ , better, but it's not required to sacrifice other parameters to maximize the gain
  - $F < F_{design}$ , better, the smaller the better, we must target **the smallest possible noise** factor as long as the other design parameters **are met**

# Friis Formula (noise)

- Friis formula
  - first stage: low noise factor, probably resulting in a smaller gain
  - second stage: high gain, probably resulting in higher noise factor
- Separation of the design parameters on the 2 amplification stages (Estimated!)
  - input stage:  $F_1 = 0.7 \text{ dB}$ ,  $G_1 = 9 \text{ dB}$
  - output stage:  $F_2 = 1.2 \text{ dB}$ ,  $G_2 = 13 \text{ dB}$
- To verify the result apply Friis formula
- First transform to **linear scale !**

$$F_1 = 10^{\frac{F_1[dB]}{10}} = 10^{0.07} = 1.175$$

$$F_2 = 10^{\frac{F_2[dB]}{10}} = 10^{0.12} = 1.318$$

$$F_{cas} = F_1 + \frac{1}{G_1} (F_2 - 1) = 1.215$$

$$F_{cas} = 10 \cdot \log(1.215) = 0.846 \text{ dB}$$

$$G_1 = 10^{\frac{G_1[dB]}{10}} = 10^{0.9} = 7.943$$

$$G_2 = 10^{\frac{G_2[dB]}{10}} = 10^{1.3} = 19.953$$

$$G_{cas} = G_1 \cdot G_2 = 158.49$$

$$G_{cas} = 10 \cdot \log(158.49) = 22 \text{ dB}$$



# Friis Formula (noise)

- Avago/Broadcom AppCAD

AppCAD - [NoiseCalc]

File Calculate Application Examples Options Help

NoiseCalc    Set Number of Stages = 2    [Calculate [F4]]

|                        |              | Stage 1   | Stage 2   |
|------------------------|--------------|---|---|
|                        |              |  |  |
| <b>Stage Data</b>      | <b>Units</b> |   |   |
| Stage Name:            |              | Avago Duplexer  | Avago ATF-36xxx   |
| Noise Figure           | dB           | 0.7   | 1.2   |
| Gain                   | dB           | 9   | 13  |
| Output IP3             | dBm          | 100   | 14.5  |
| dNF/dTemp              | dB/°C        | 0   | 0   |
| dG/dTemp               | dB/°C        | 0   | 0   |
| <b>Stage Analysis:</b> |              |   |   |
| NF (Temp corr)         | dB           | 0.70  | 1.20  |
| Gain (Temp corr)       | dB           | 9.00  | 13.00   |
| Input Power            | dBm          | -50.00  | -41.00  |
| Output Power           | dBm          | -41.00  | -28.00  |
| d NF/d NF              | dB/dB        | 0.97  | 0.15  |
| d NF/d Gain            | dB/dB        | -0.03   | 0.00  |
| d IP3/d IP3            | dBm/dBm      | 0.00  | 1.00  |

Enter System Parameters:

|                       |     |     |
|-----------------------|-----|-----|
| Input Power           | -50 | dBm |
| Analysis Temperature  | 25  | °C  |
| Noise BW              | 1   | MHz |
| Ref Temperature       | 25  | °C  |
| S/N (for sensitivity) | 10  | dB  |
| Noise Source (Ref)    | 290 | *K  |

System Analysis:

|                |         |        |
|----------------|---------|--------|
| Gain =         | 22.00   | dB     |
| Noise Figure = | 0.85    | dB     |
| Noise Temp =   | 82.94   | *K     |
| SNR =          | 63.13   | dB     |
| MDS =          | -113.13 | dBm    |
| Sensitivity =  | -103.13 | dBm    |
| Noise Floor =  | -173.13 | dBm/Hz |

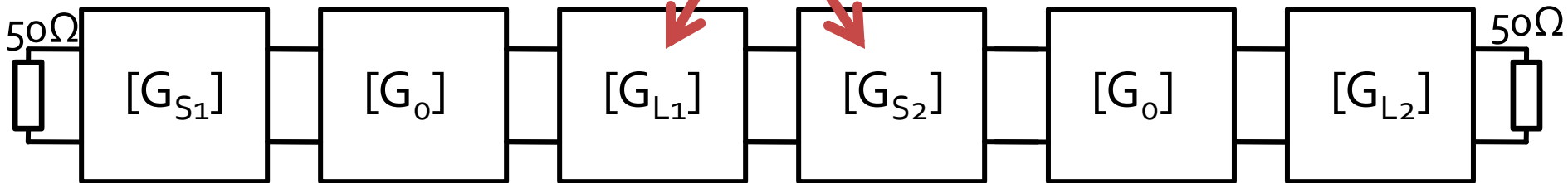
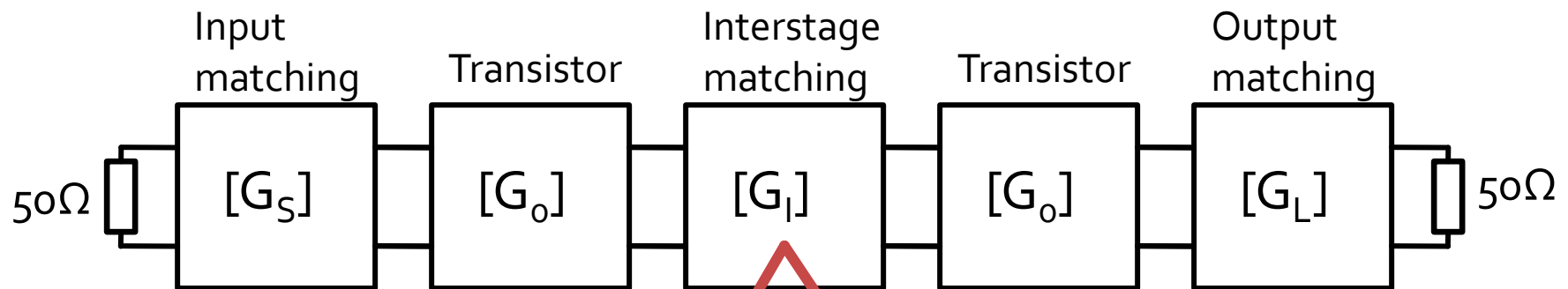
|                   |         |     |
|-------------------|---------|-----|
| Input IP3 =       | -7.50   | dBm |
| Output IP3 =      | 14.50   | dBm |
| Input IM level =  | -135.00 | dBm |
| Input IM level =  | -85.00  | dBc |
| Output IM level = | -113.00 | dBm |
| Output IM level = | -85.00  | dBc |
| SFDR =            | 70.42   | dB  |

# Multistage amplifier design

- Separation of the design parameters on the 2 amplification stages (Estimated!)
  - input stage:  $F_1 = 0.7$  dB,  $G_1 = 9$  dB
  - output stage:  $F_2 = 1.2$  dB,  $G_2 = 13$  dB
  - total:  $F = 0.85$  dB,  $G = 22$  dB
- Meets design specifications (with design margin)
- We can reuse some of the results in the single stage LNA design (Lecture 10)
  - input matching can be used for the input of the first stage – very low noise, good enough power gain
  - output matching was designed for maximum gain, can be used for the output of the second stage
  - input and output matching were designed for  $50\Omega$  source and load, similar to current conditions

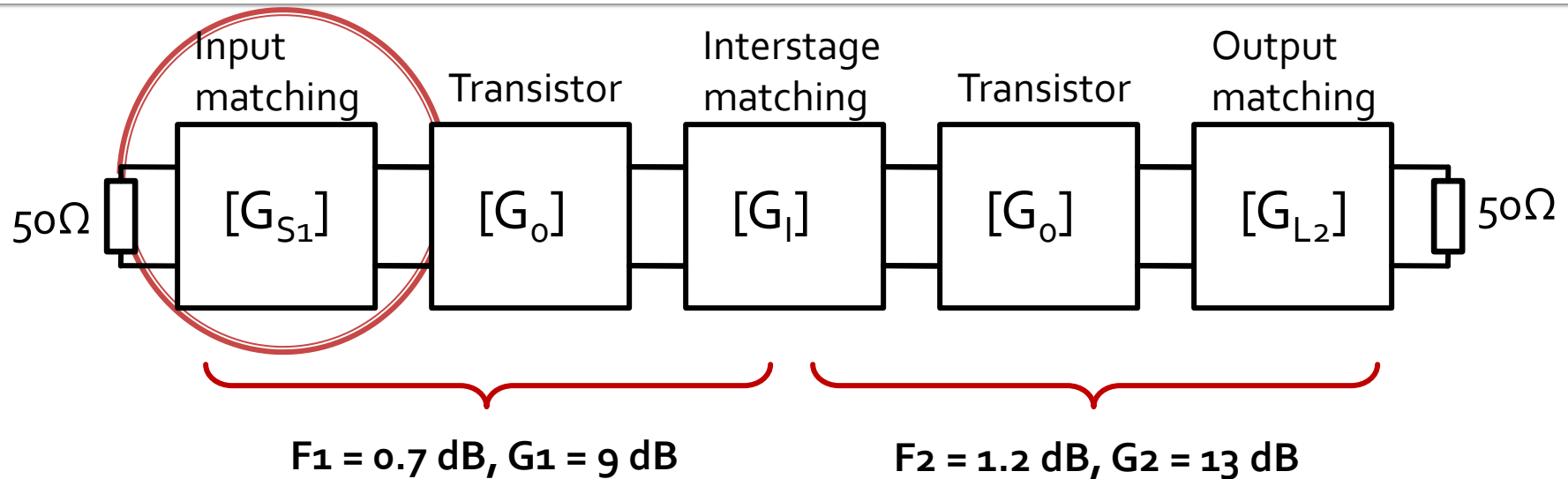


# Multistage amplifier design



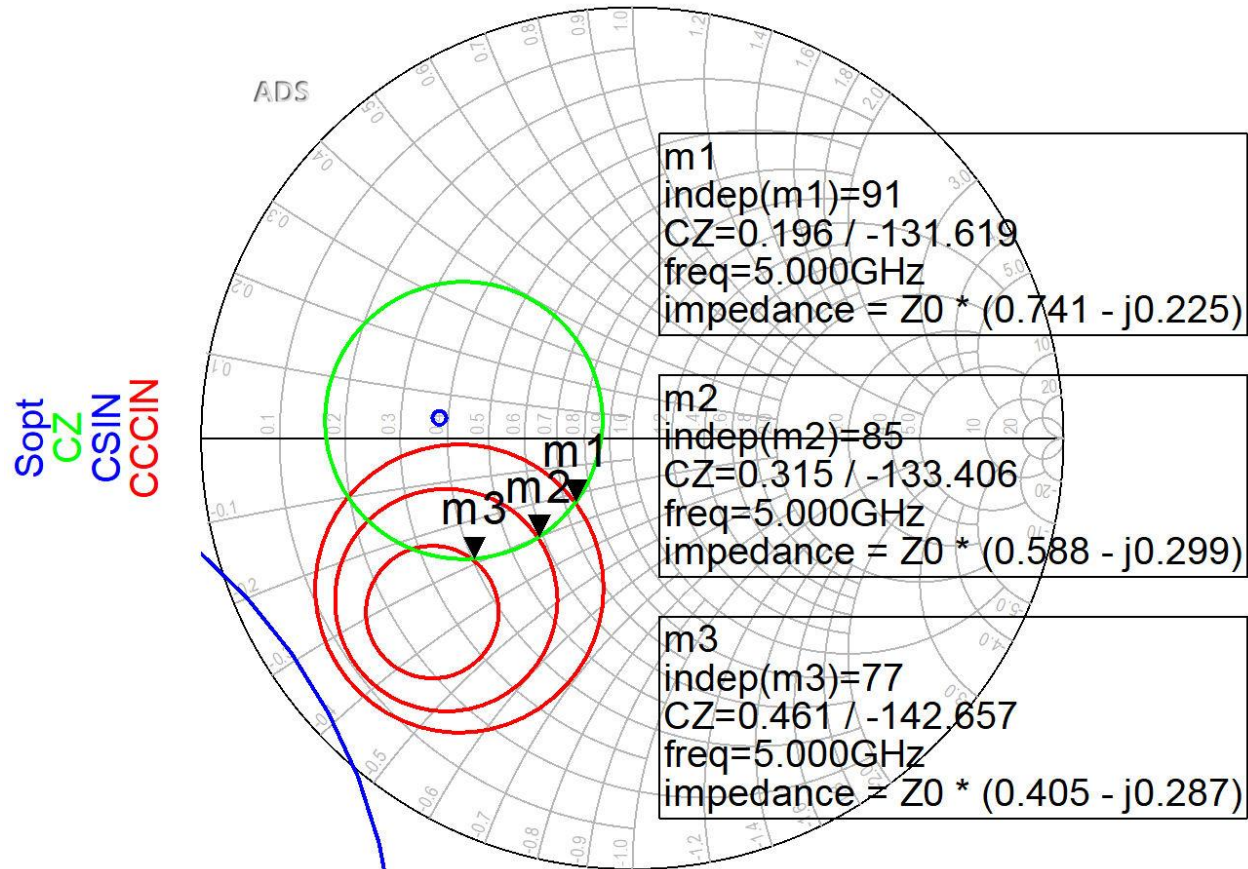
- Gain computation
  - Interstage matching can supplement the gain for both amplifier stages
  - The design for input and output matching must be achieved on a single transistor schematic (recommended: easier)

# Input matching stage 1 (S<sub>1</sub>)



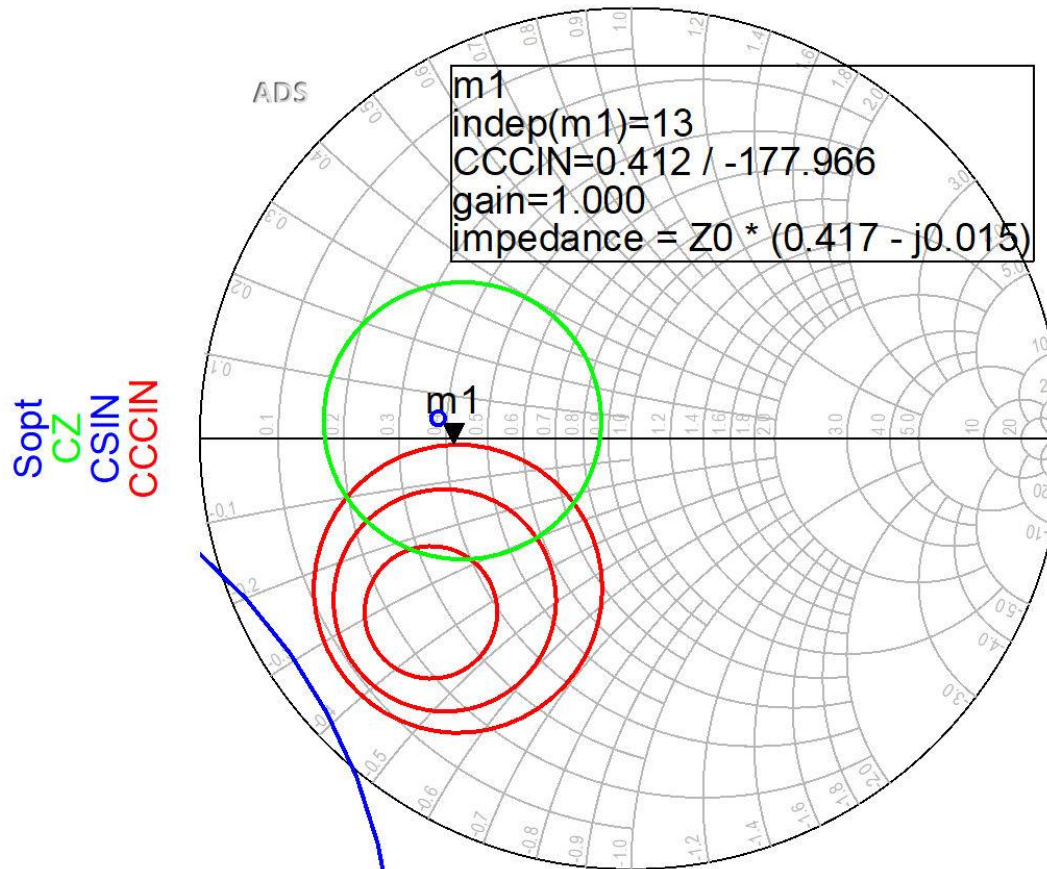
- We favor optimization for **noise** (low/minimum)
- Also considered
  - Power gain (can be lower, but not too much)
  - Bandwidth (through  $Q$ , quality factor)
  - Stability

# Input matching stage 1 (S<sub>1</sub>)



- For the input matching circuit
  - noise circle CZ: 0.75dB
  - input constant gain circles CCCIN: 1dB, 1.5dB, 2 dB
- We choose (small Q → wide bandwidth) position m<sub>1</sub>

# Input matching stage 1 (S<sub>1</sub>)



- If we can afford a 1.2dB decrease of the input gain for better NF, Q (Gs = 1 dB), position m1 above is better
- We favor **better** (smaller) **NF**

# Input matching stage 1 (S<sub>1</sub>)

- **G<sub>S1</sub>**: Position m<sub>1</sub> in complex plane, **1dB**

$$\Gamma_S = 0.412 \angle -178^\circ$$

$$|\Gamma_S| = 0.412; \quad \varphi = -178^\circ$$

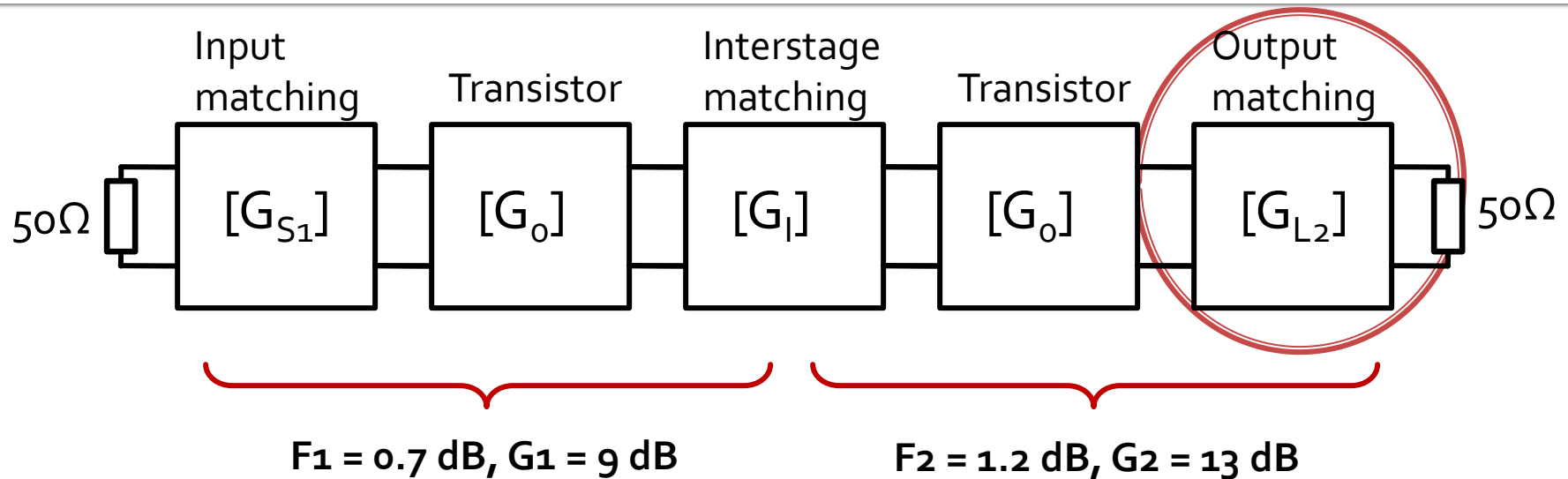
$$\cos(\varphi + 2\theta) = -|\Gamma_S| \quad \text{Im}[y_S(\theta)] = \frac{\mp 2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}}$$

$$\cos(\varphi + 2\theta) = -0.412 \Rightarrow (\varphi + 2\theta) = \pm 114.33^\circ$$

$$\theta_{sp} = \tan^{-1}(\text{Im}[y_S(\theta)]) = \tan^{-1}\left(\frac{\mp 2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}}\right)$$

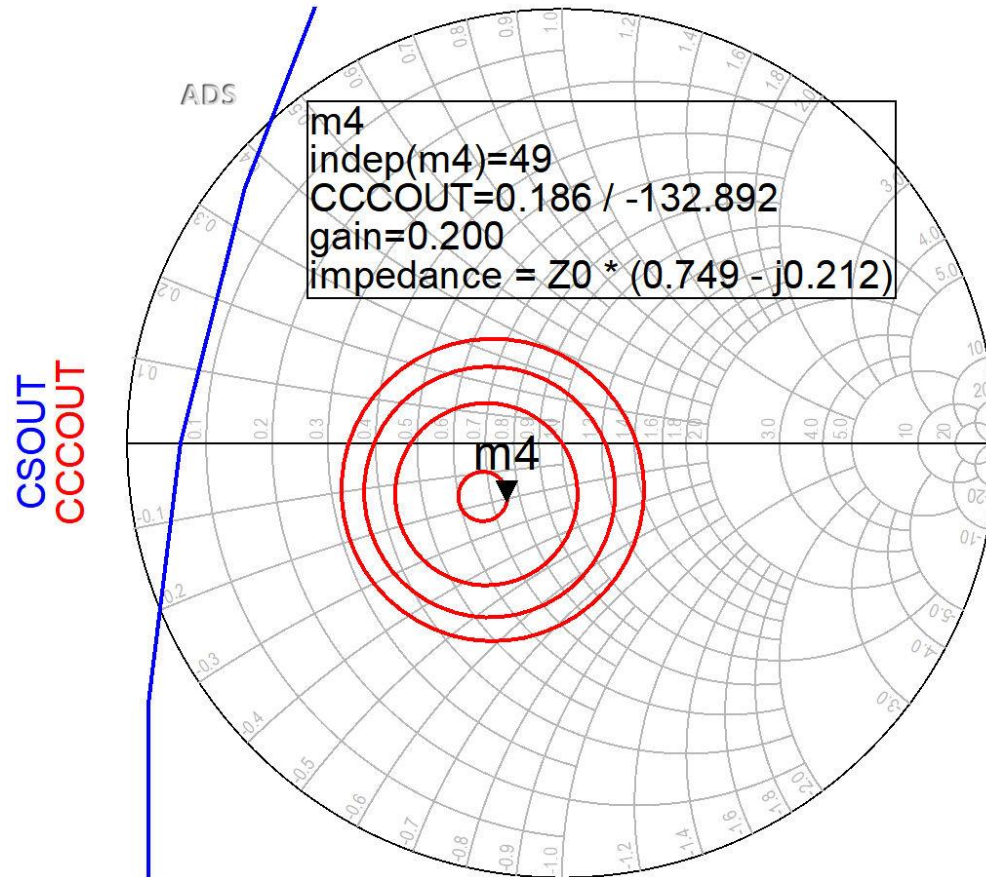
$$(\varphi + 2\theta) = \begin{cases} +114.33^\circ \\ -114.33^\circ \end{cases} \quad \theta = \begin{cases} 146.2^\circ \\ 31.8^\circ \end{cases} \quad \text{Im}[y_S(\theta)] = \begin{cases} -0.904 \\ +0.904 \end{cases} \quad \theta_{sp} = \begin{cases} 137.9^\circ \\ 42.1^\circ \end{cases}$$

# Output matching stage 2 (L2)



- We favor optimization for **gain** (high/maximum)
- Also considered
  - Bandwidth (through  $Q$ , quality factor)
  - Stability
- noise is **not** an issue, output matching doesn't influence noise factor

# Output matching stage 2 (L2)



- output constant gain circles CCCOUT: -0.4dB, -0.2dB, 0dB, +0.2dB
- The lack of noise restrictions allows optimization for better gain (close to maximum – position m4)

# Output matching stage 2 (L2)

- $\mathbf{G_{L2}}$ : Position  $m_4$  in complex plane, **0.2dB**

$$\Gamma_L = 0.186 \angle -132.9^\circ$$

$$|\Gamma_L| = 0.186; \quad \varphi = -132.9^\circ$$

$$\cos(\varphi + 2\theta) = -|\Gamma_L|$$

$$\text{Im}[y_L(\theta)] = \frac{-2 \cdot |\Gamma_L|}{\sqrt{1 - |\Gamma_L|^2}} = -0.379$$

$$\cos(\varphi + 2\theta) = -0.186 \Rightarrow (\varphi + 2\theta) = \pm 100.72^\circ$$

$$\theta_{sp} = \tan^{-1}(\text{Im}[y_L(\theta)]) = \tan^{-1}\left(\frac{\mp 2 \cdot |\Gamma_L|}{\sqrt{1 - |\Gamma_L|^2}}\right)$$

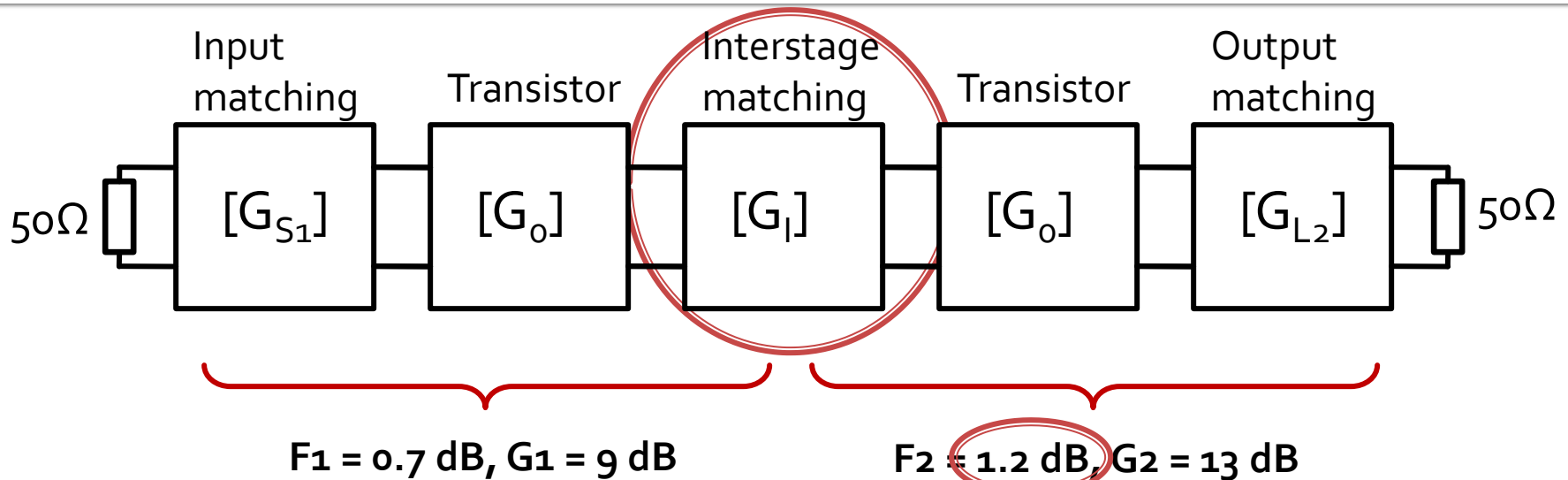
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$$(\varphi + 2\theta) = \begin{cases} +100.72^\circ \\ -100.72^\circ \end{cases} \quad \theta = \begin{cases} 116.8^\circ \\ 16.1^\circ \end{cases} \quad \text{Im}[y_L(\theta)] = \begin{cases} -0.379 \\ +0.379 \end{cases} \quad \theta_{sp} = \begin{cases} 159.3^\circ \\ 20.7^\circ \end{cases}$$

---



# Interstage matching (I)



- We take into account **gain** (high) but also **noise**
- Also considered
  - Bandwidth (through Q, quality factor)
  - Stability
- We influence the noise factor of the second stage, the noise must be considered but with less restrictive conditions (Friis shows that higher noise is acceptable).

# Multistage amplifier

- Power gain

$$G_T [dB] = G_{S1} [dB] + G_0 [dB] + G_I [dB] + G_0 [dB] + G_{L2} [dB]$$

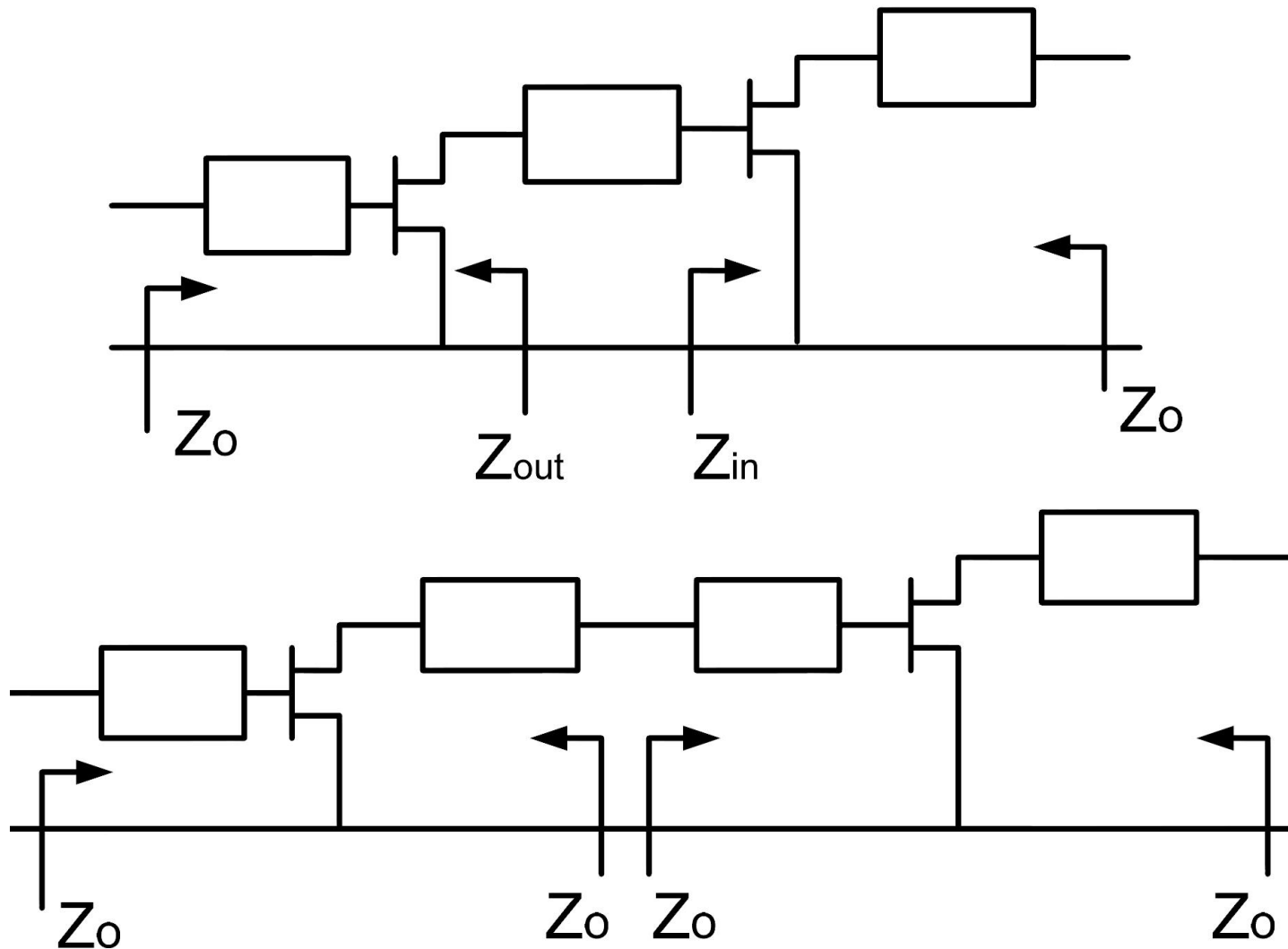
$$G_0 = |S_{21}|^2 = 10.017 = 10.007 \text{ dB}$$

$$G_T [dB] = 1 \text{ dB} + 10 \text{ dB} + G_I [dB] + 10 \text{ dB} + 0.2 \text{ dB}$$

$$G_T [dB] = 21.2 \text{ dB} + G_I [dB]$$

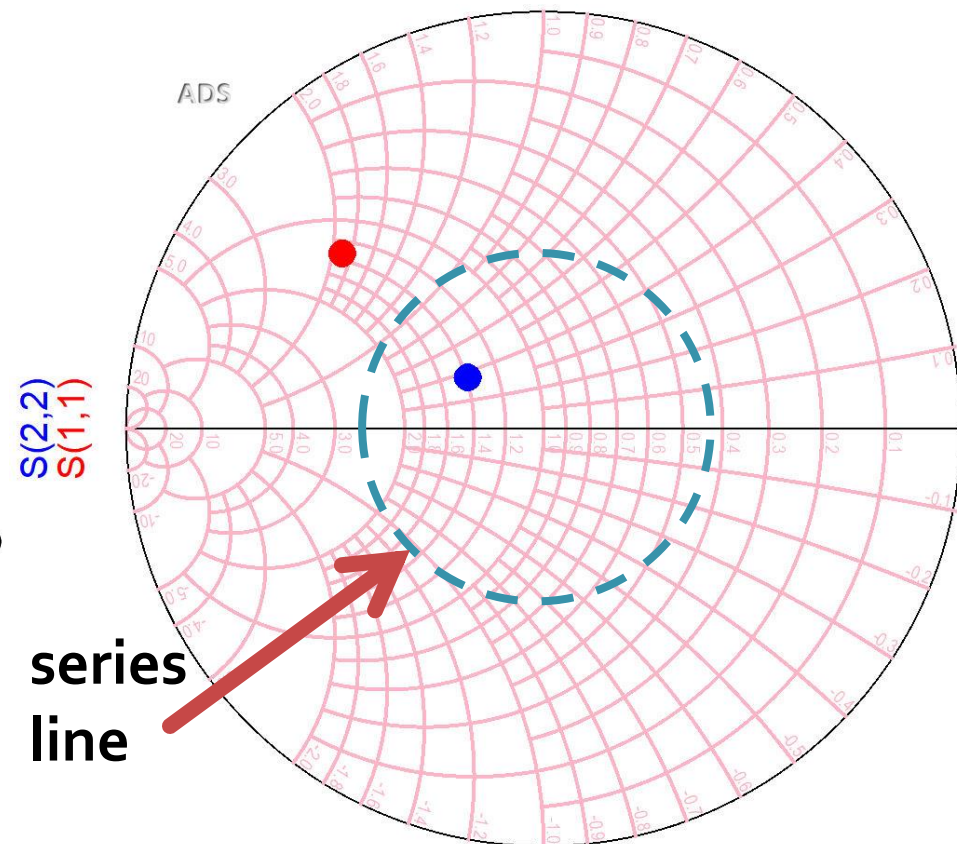
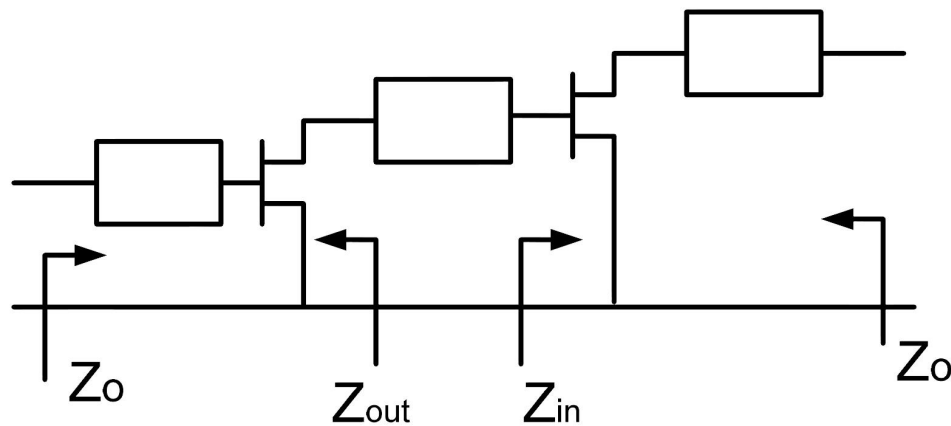
- Interstage match design must provide at least 0.8dB gain to meet specifications, by better match for the output of the first transistor and for the input of the second transistor

# Interstage matching 1/2



# Interstage matching 1

- A single transmission line keeps constant the magnitude of the reflection coefficient
  - a circle around the Smith Chart center

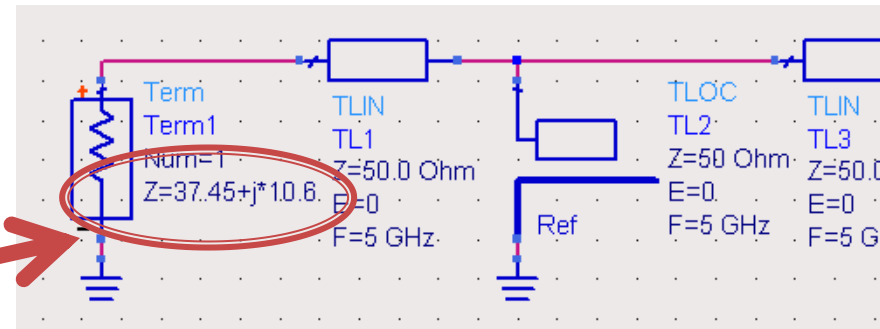
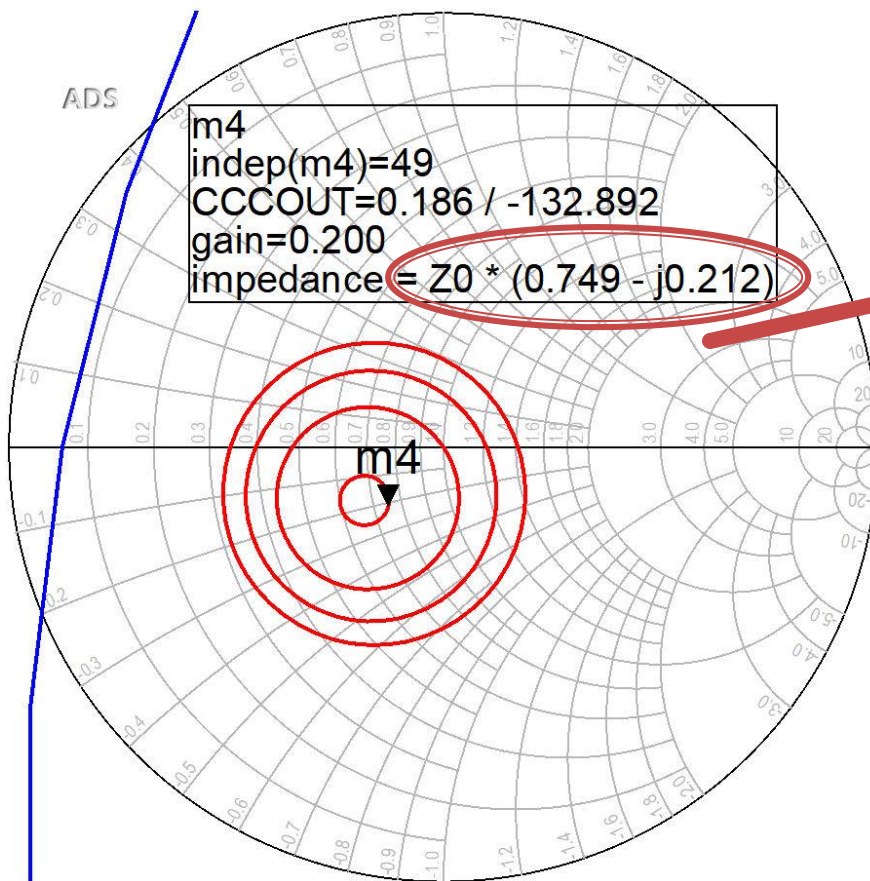


# Interstage matching 1

- Can be designed in two ways:
  - starting from the output of the first stage (reflection coefficient  $S_{22}^*$ ) towards the circles (drawn for the second stage):
    - stability
    - gain
    - noise
  - starting from the input of the second stage (reflection coefficient  $S_{11}^*$ ) towards the circles (drawn for the first stage):
    - stability
    - gain
- First design direction has the advantage to offer control over the noise introduced by the second stage

# Interstage matching 1

- Starting point – complex conjugate



$$Z = 50\Omega \cdot (0.749 - j \cdot 0.212)$$

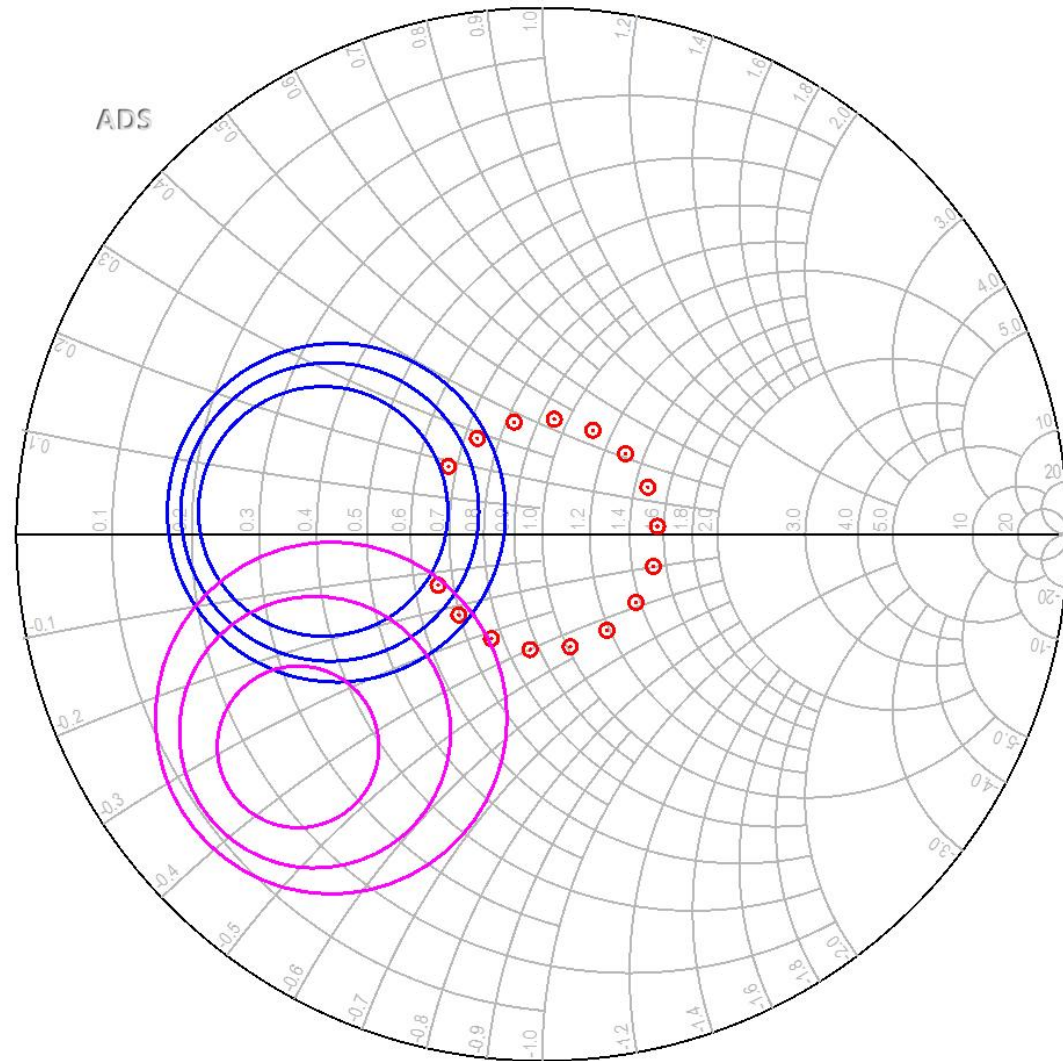
$$Z = 37.45\Omega - j \cdot 10.6\Omega$$

$$Z^* = 37.45\Omega + j \cdot 10.6\Omega$$

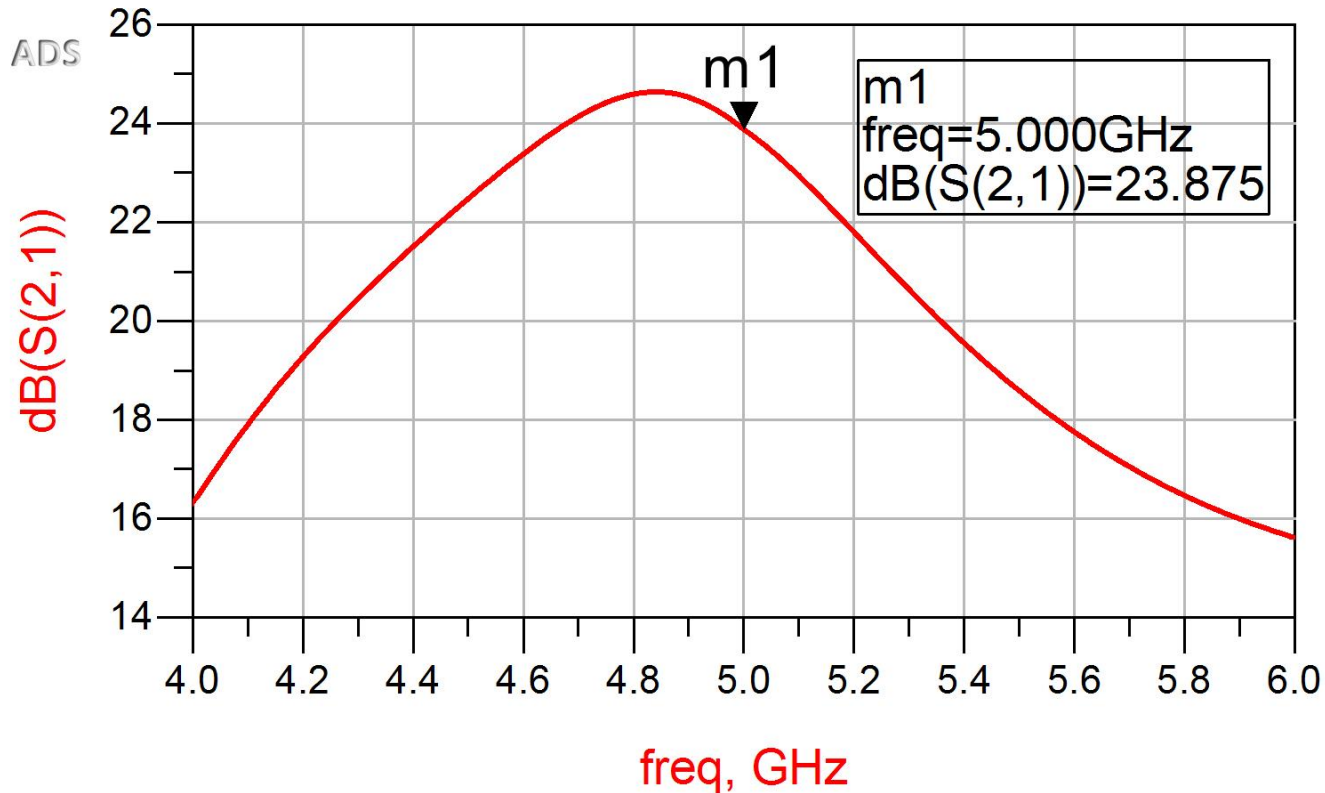
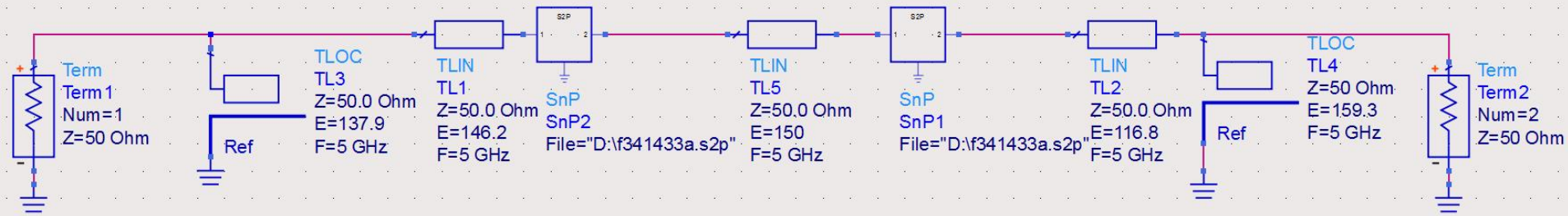
# Interstage matching 1

- A **single** transmission line allows reaching a point that cannot be optimized
  - $G_{L1} = 0.2 \text{ dB}$
  - $G_{S2} = 1 \text{ dB}$
  - $F_2 = 0.7 \text{ dB}$
- Only one parameter is available for wide band performance tuning

ref..CCCIN  
ref..CZ  
S(2,2)

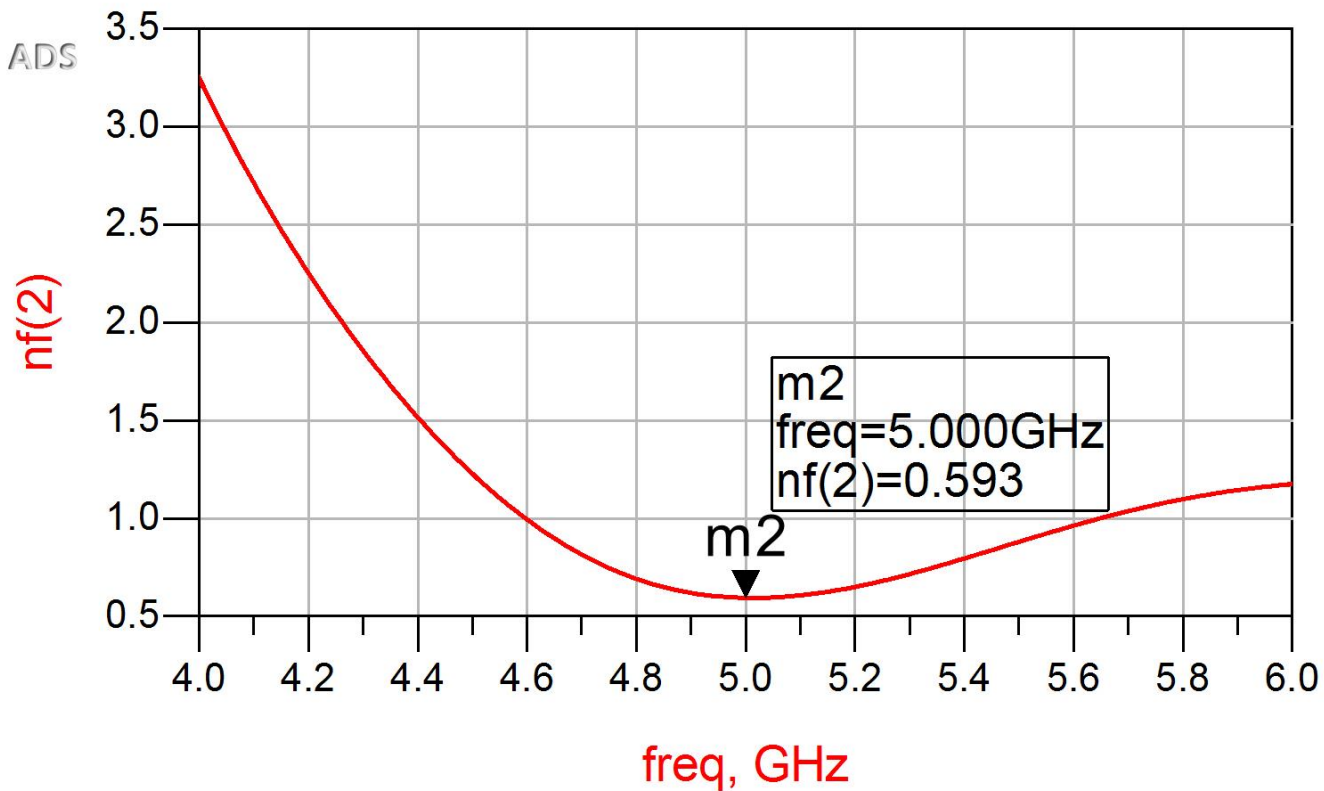
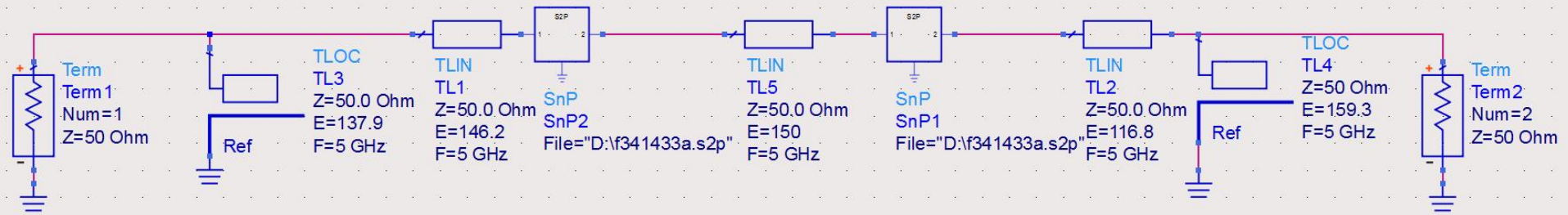


# ADS



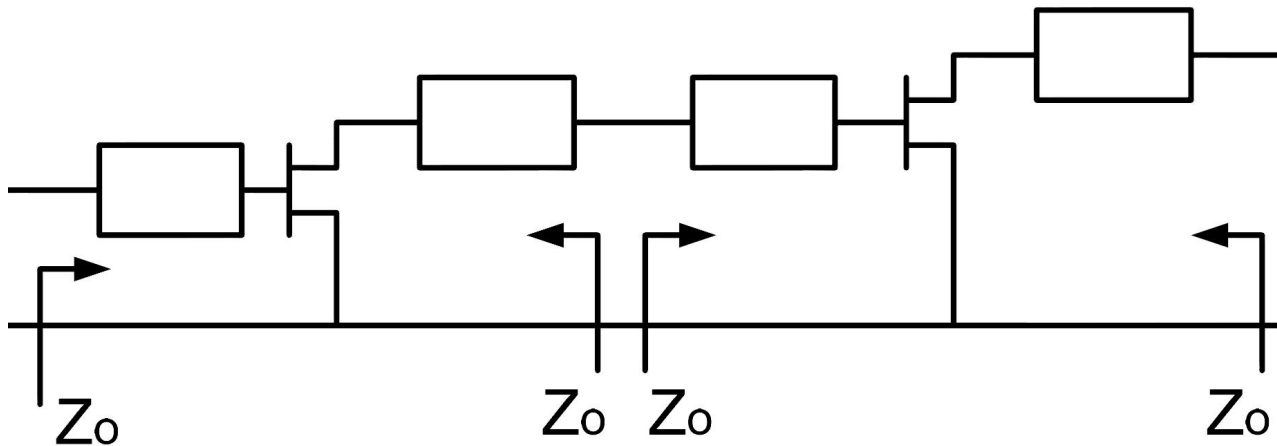


# ADS

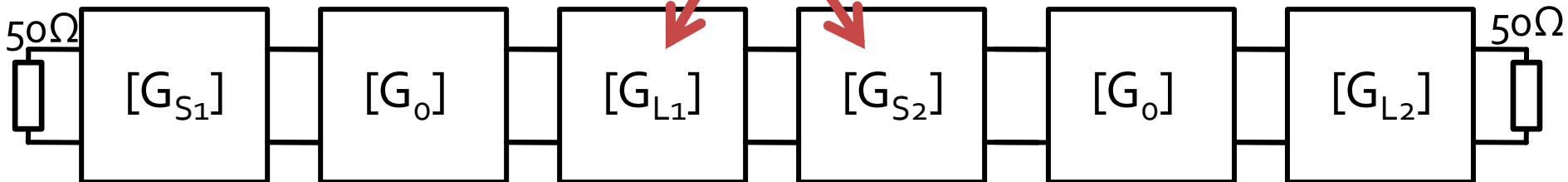
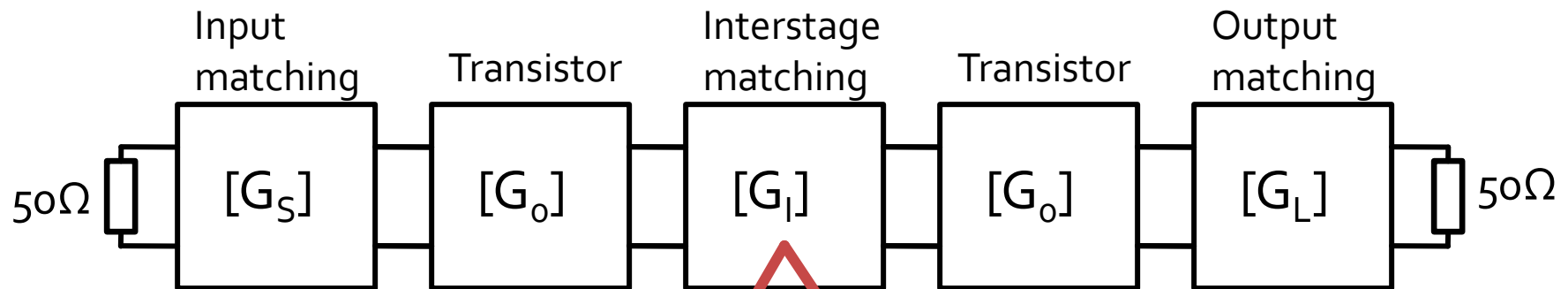


# Interstage matching 2

- Using multiple transmission lines for matching each stage to a intermediate  $\Gamma=0$  (virtual) allows detailed control over final reflection coefficient (and thus gain/noise)



# Interstage matching 2



- Instead of a single match design we have to design two matching networks
- However both matching networks are anchored to a fixed point ( $50\Omega$ ,  $\Gamma=0$ ) so we can use design **formulas** (Impedance Matching with Stubs)
- Also, due to the presence of multiple networks, we can target **precise** positions (reflection coefficients) on both stages

# Multistage amplifier

- Power gain

$$G_T [dB] = G_{S1} [dB] + G_0 [dB] + G_{L1} [dB] + G_{S2} [dB] + G_0 [dB] + G_{L2} [dB]$$

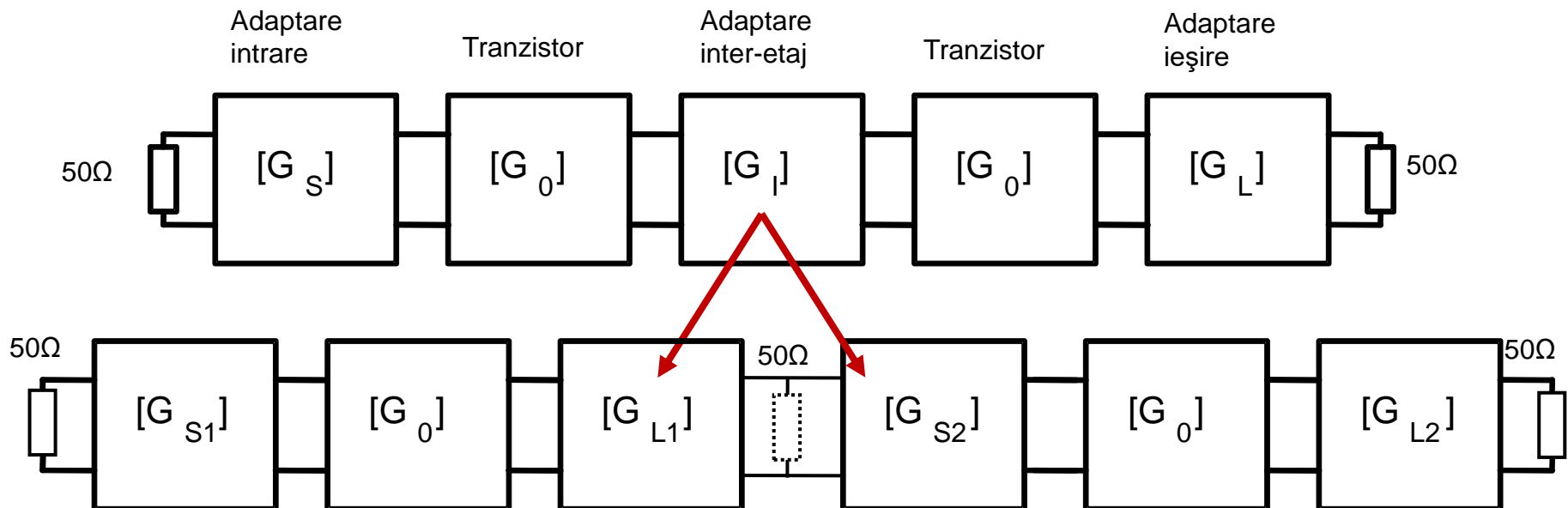
$$G_T [dB] = 1 \text{ dB} + 10 \text{ dB} + G_{L1} [dB] + G_{S2} [dB] + 10 \text{ dB} + 0.2 \text{ dB}$$

$$G_T [dB] = 21.2 \text{ dB} + \underbrace{G_{L1} [dB] + G_{S2} [dB]}$$

- Interstage match design must provide at least 0.8dB **in total** gain to meet specifications, by separately better matching the output of the first transistor and for the input of the second transistor

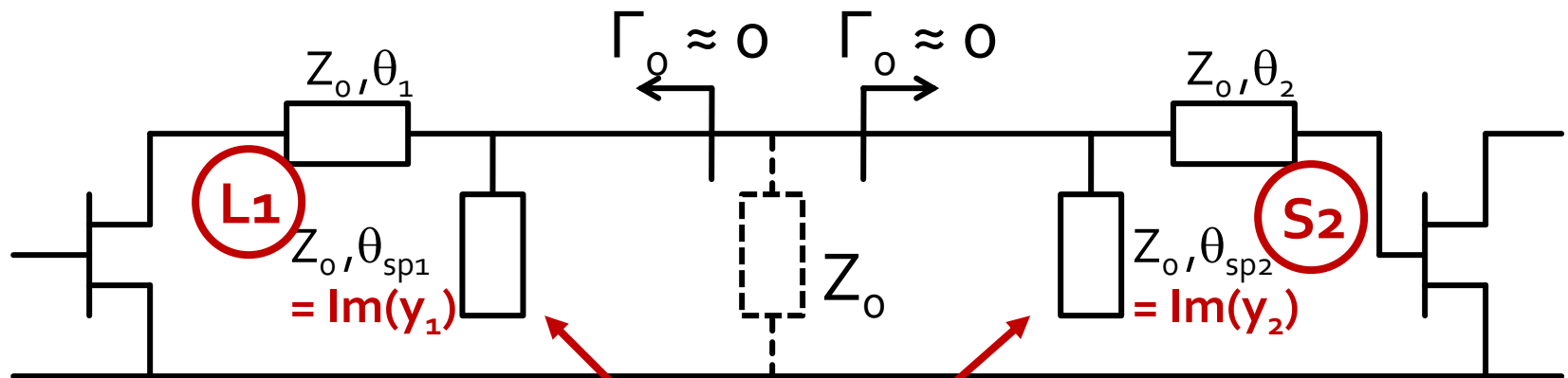
# Interstage matching 2

- Using multiple transmission lines for matching each stage to a intermediate  $\Gamma=0$  (virtual) allows detailed control over reflection coefficient on both stages



# Interstage matching 2

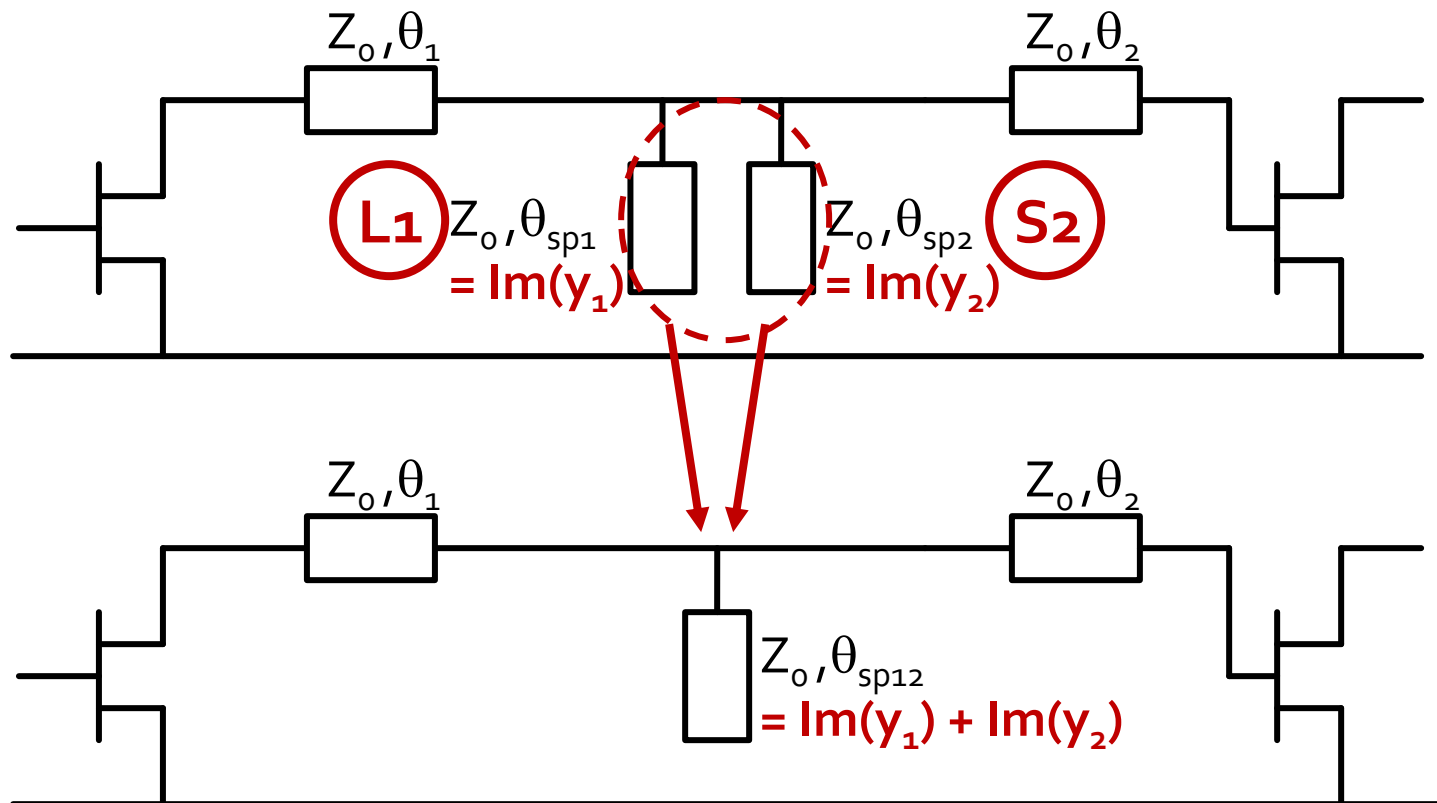
- One of the stages **creates** through its matching network a reflection coefficient  $\Gamma=0$  towards which the other stage is matched



The two shunt stubs combine into a single one

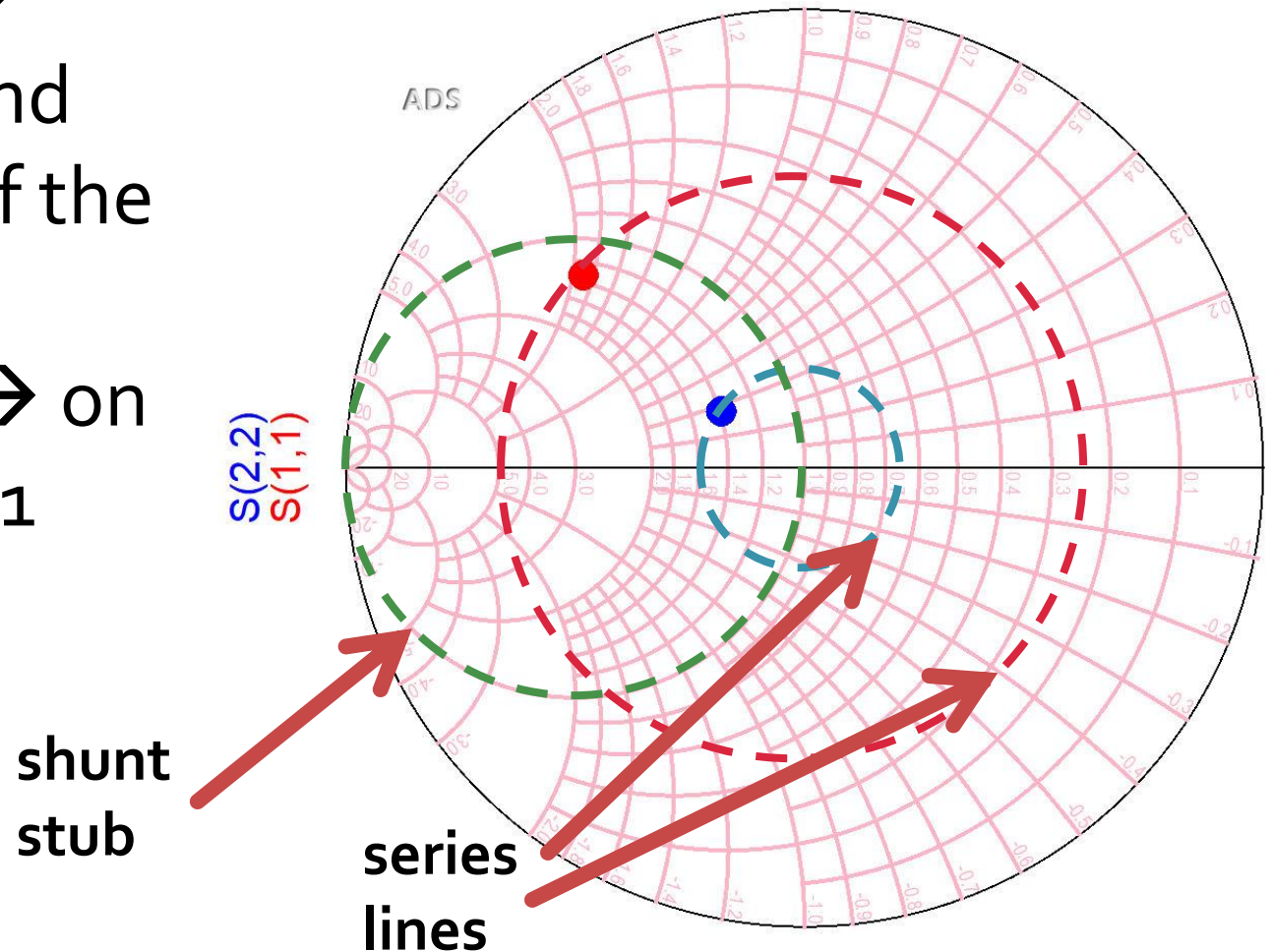
# Interstage matching 2

- The two shunt stubs combine into a single one



# Interstage matching 2

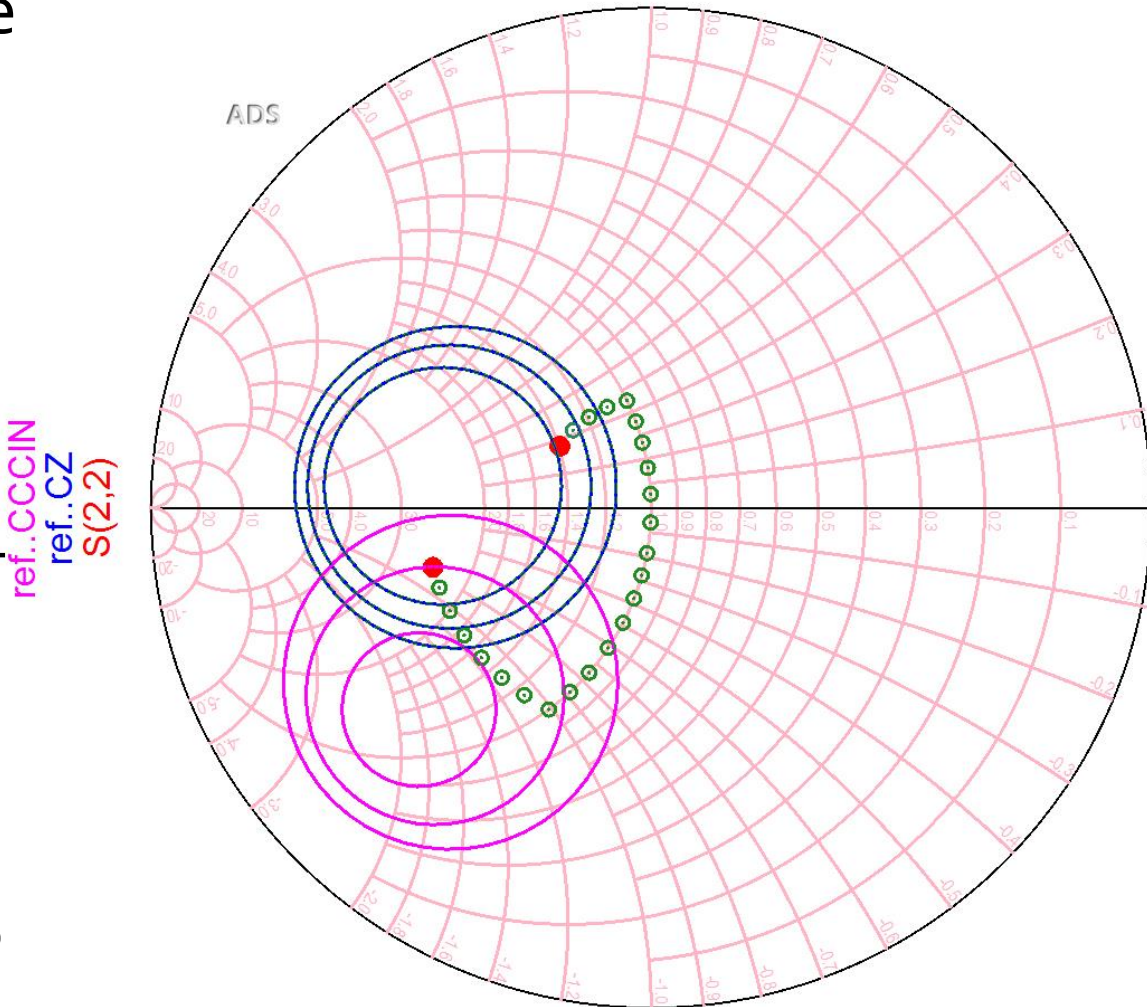
- series line  $\rightarrow$  moves around the center of the SC
- shunt stub  $\rightarrow$  on the circle  $g=1$





# Interstage matching 2

- For every stage we use a series line and a shunt stub
  - the series line moves the reflection coefficient from the desired starting point on the unity conductance circle  $g=1$
  - the shunt stub moves the point to the center of the Smith Chart ( $Z_0$  match)
- The two shunt stubs will then combine into one



# Output matching stage 1 (L1)

- $G_{L1}$  (we use the same point <- output L2), **0.2dB**

$$\Gamma_L = 0.186 \angle -132.9^\circ$$

$$|\Gamma_L| = 0.186; \quad \varphi = -132.9^\circ$$

$$\cos(\varphi + 2\theta) = -|\Gamma_L| \qquad \text{Im}[y_L(\theta)] = \frac{-2 \cdot |\Gamma_L|}{\sqrt{1 - |\Gamma_L|^2}} = -0.379$$

$$\cos(\varphi + 2\theta) = -0.186 \Rightarrow (\varphi + 2\theta) = \pm 100.72^\circ$$

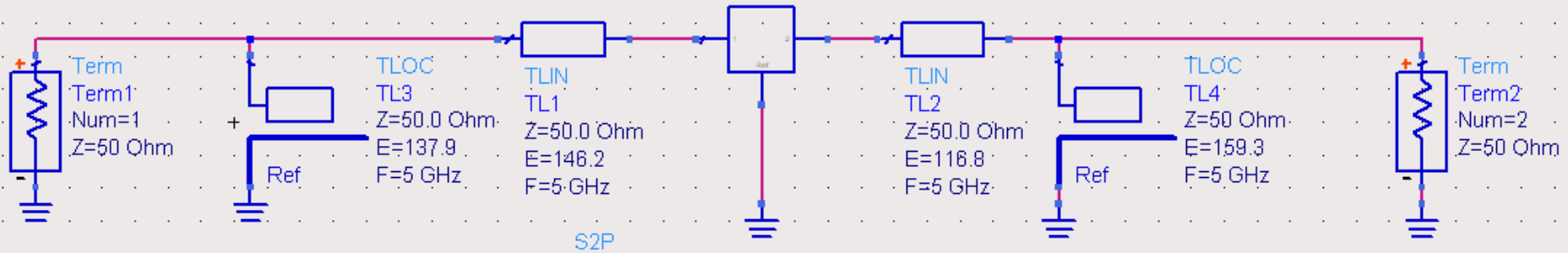
- the length of the shunt stub  $\theta_{sp}$  is not calculated because it is **not** needed

$$(\varphi + 2\theta) = \begin{cases} +100.72^\circ \\ -100.72^\circ \end{cases} \quad \theta = \begin{cases} 116.8^\circ \\ 16.1^\circ \end{cases} \quad \text{Im}[y_L(\theta)] = \begin{cases} -0.379 \\ +0.379 \end{cases}$$

# Output matching stage 1 (L1)

| <b>Equation</b>        | <b>Solution L1A</b> | <b>Solution L1B</b> |
|------------------------|---------------------|---------------------|
| $\Phi+2\theta$         | $+100.72^\circ$     | $-100.72^\circ$     |
| $\theta$               | $116.8^\circ$       | $16.1^\circ$        |
| $\text{Im}[y(\theta)]$ | $-0.379$            | $+0.379$            |

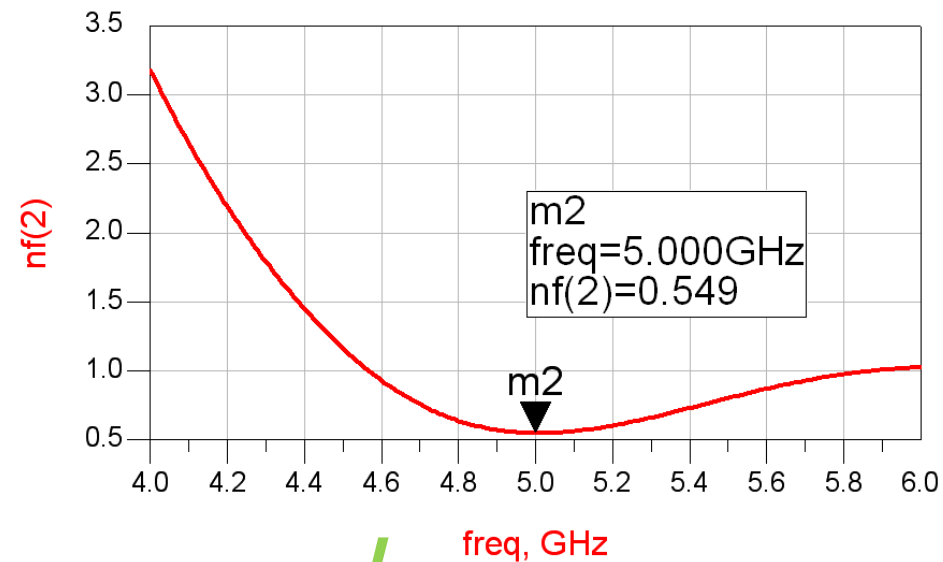
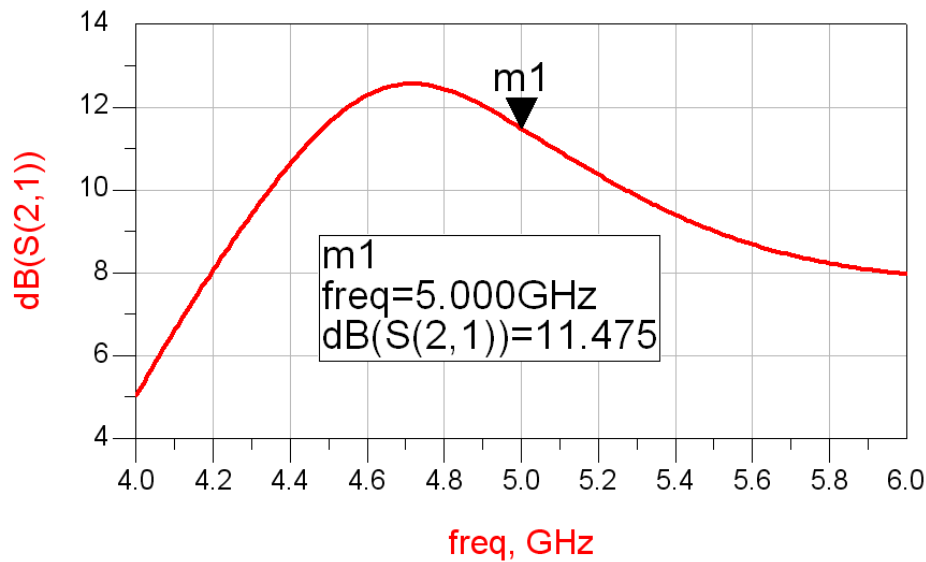
# Verify stage 1



$G_{S1}$

$G_0$

$G_{L1}$



$F_1 < 0.7 \text{ dB}, G_1 > 9 \text{ dB}$  ✓

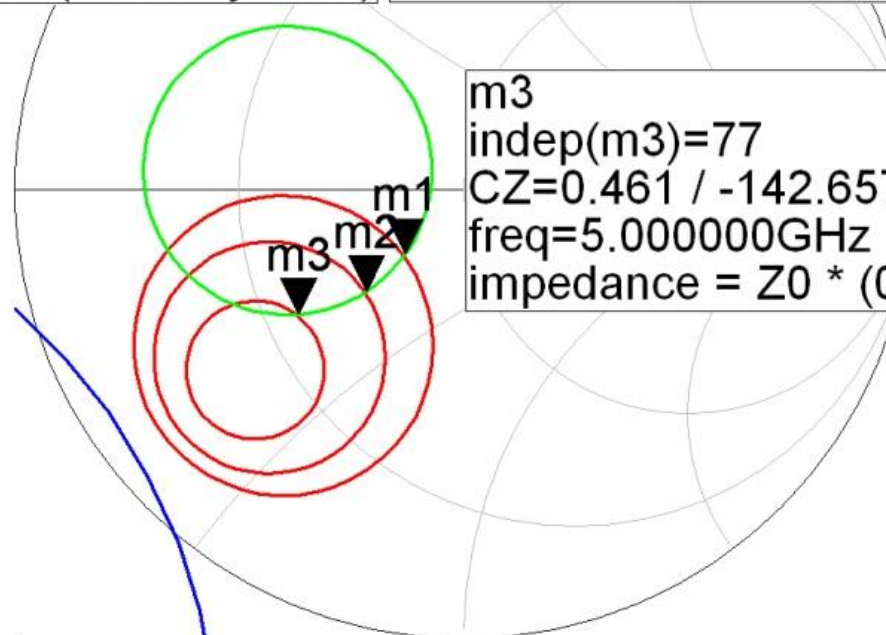
# Input matching stage 2 (S2)

- $G_{S_2}$  (moving from  $\Gamma_{S_2}$  we choose towards complex plane origin – **m3** – gain 2dB)

m1  
indep(m1)=91  
CZ=0.196 / -131.619  
freq=5.000000GHz  
impedance =  $Z_0 * (0.741 - j0.225)$

m2  
indep(m2)=85  
CZ=0.315 / -133.406  
freq=5.000000GHz  
impedance =  $Z_0 * (0.588 - j0.299)$

CZ  
CSIN  
CCCIN



m3  
indep(m3)=77  
CZ=0.461 / -142.657  
freq=5.000000GHz  
impedance =  $Z_0 * (0.405 - j0.287)$

# Input matching stage 2 (S2)

- $G_{S_2}$  (going from  $m_3$  towards origin), **2dB**

$$\Gamma_{S_2} = 0.461 \angle -142.66^\circ \quad |\Gamma_{S_2}| = 0.461; \quad \varphi = -142.66^\circ$$

$$\cos(\varphi + 2\theta) = -|\Gamma_{S_2}| \quad \text{Im}[y_{S_2}(\theta)] = \frac{\mp 2 \cdot |\Gamma_{S_2}|}{\sqrt{1 - |\Gamma_{S_2}|^2}}$$

$$\cos(\varphi + 2\theta) = -0.461 \Rightarrow (\varphi + 2\theta) = \pm 117.45^\circ$$

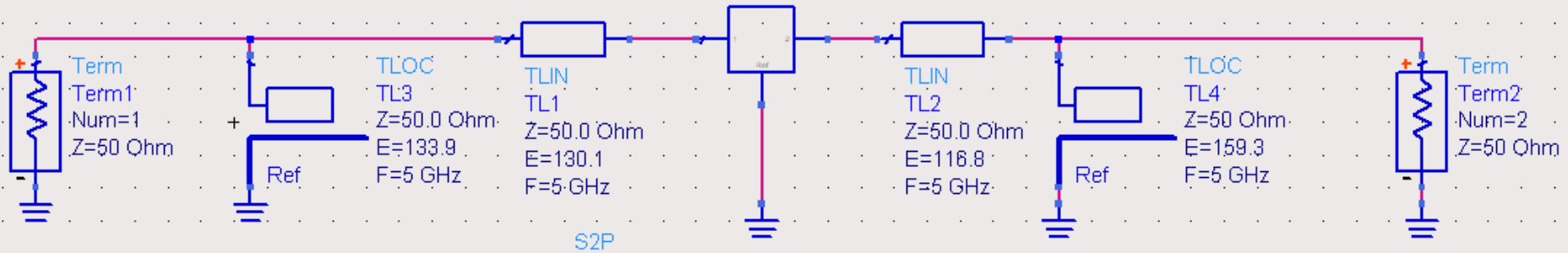
- the length of the shunt stub  $\theta_{sp}$  is not calculated because it is **not** needed

$$(\varphi + 2\theta) = \begin{cases} +117.45^\circ \\ -117.45^\circ \end{cases} \quad \theta = \begin{cases} 130.1^\circ \\ 12.6^\circ \end{cases} \quad \text{Im}[y_{S_2}(\theta)] = \begin{cases} -1.039 \\ +1.039 \end{cases}$$

# Input matching stage 2 (S2)

| <b>Equation</b>        | <b>Solution S2A</b> | <b>Solution S2B</b> |
|------------------------|---------------------|---------------------|
| $\Phi+2\theta$         | $+117.45^\circ$     | $-117.45^\circ$     |
| $\theta$               | $130.1^\circ$       | $12.6^\circ$        |
| $\text{Im}[y(\theta)]$ | $-1.039$            | $+1.039$            |

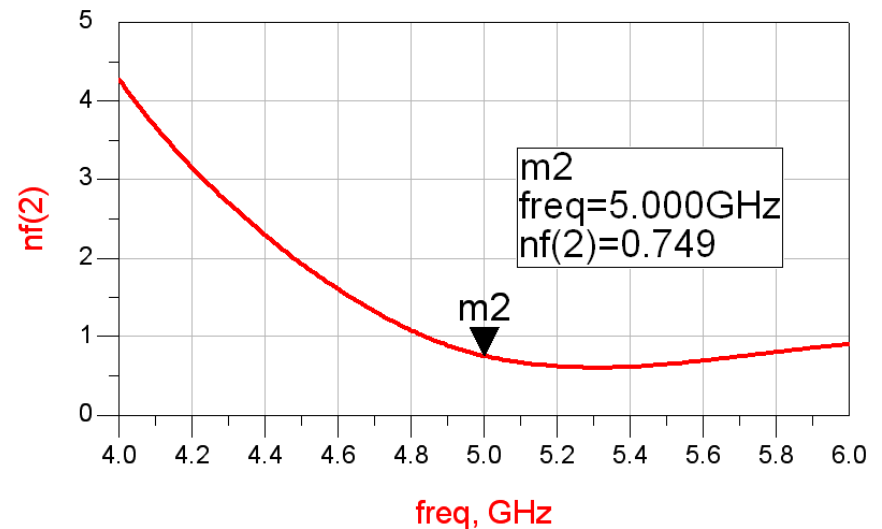
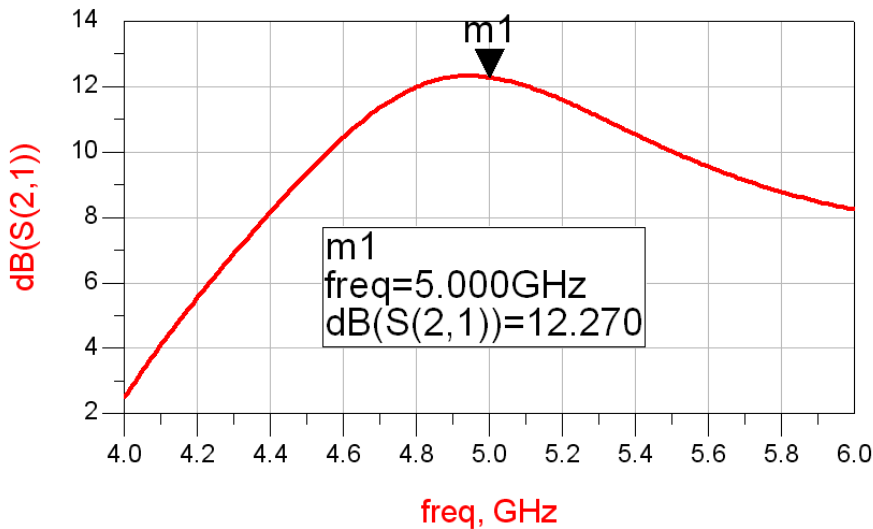
# Verify stage 2



$G_{S1}$

$G_0$

$G_{L1}$

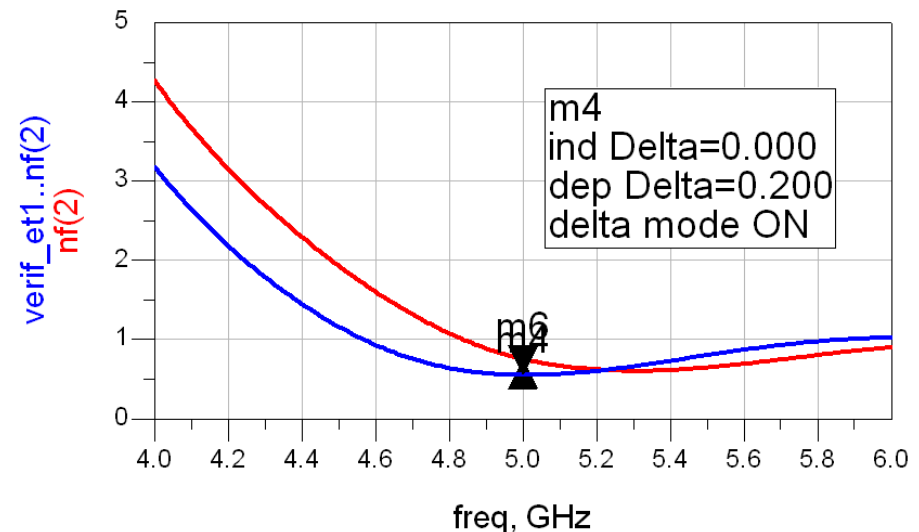
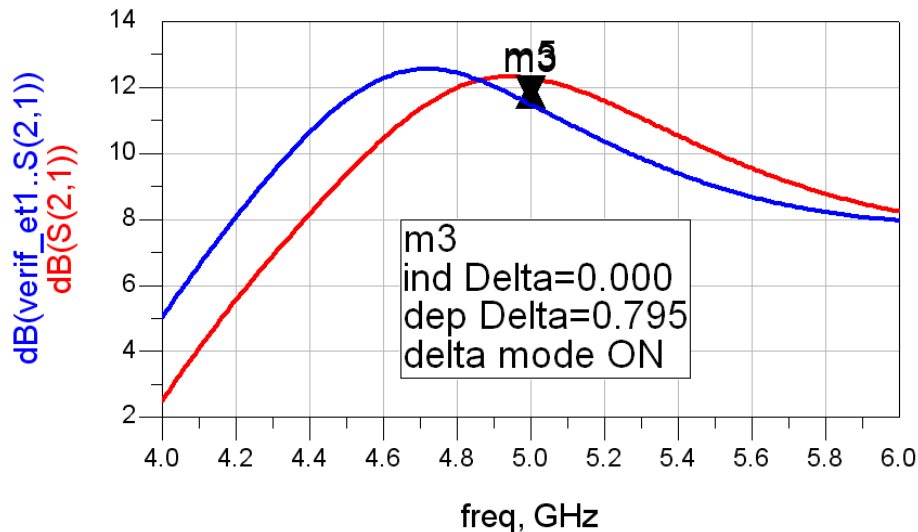


$F_2 < 1.2 \text{ dB}, G_2 < 13 \text{ dB}$  **X**  $G_1 = 11.5 \text{ dB}, G_2 = 12.3 \text{ dB}, G_1 + G_2 > 22 \text{ dB}$  **✓**



# Stage 1/2

- According to the conclusions of the Friis formula, the second stage obtains a higher gain because a higher noise is acceptable.



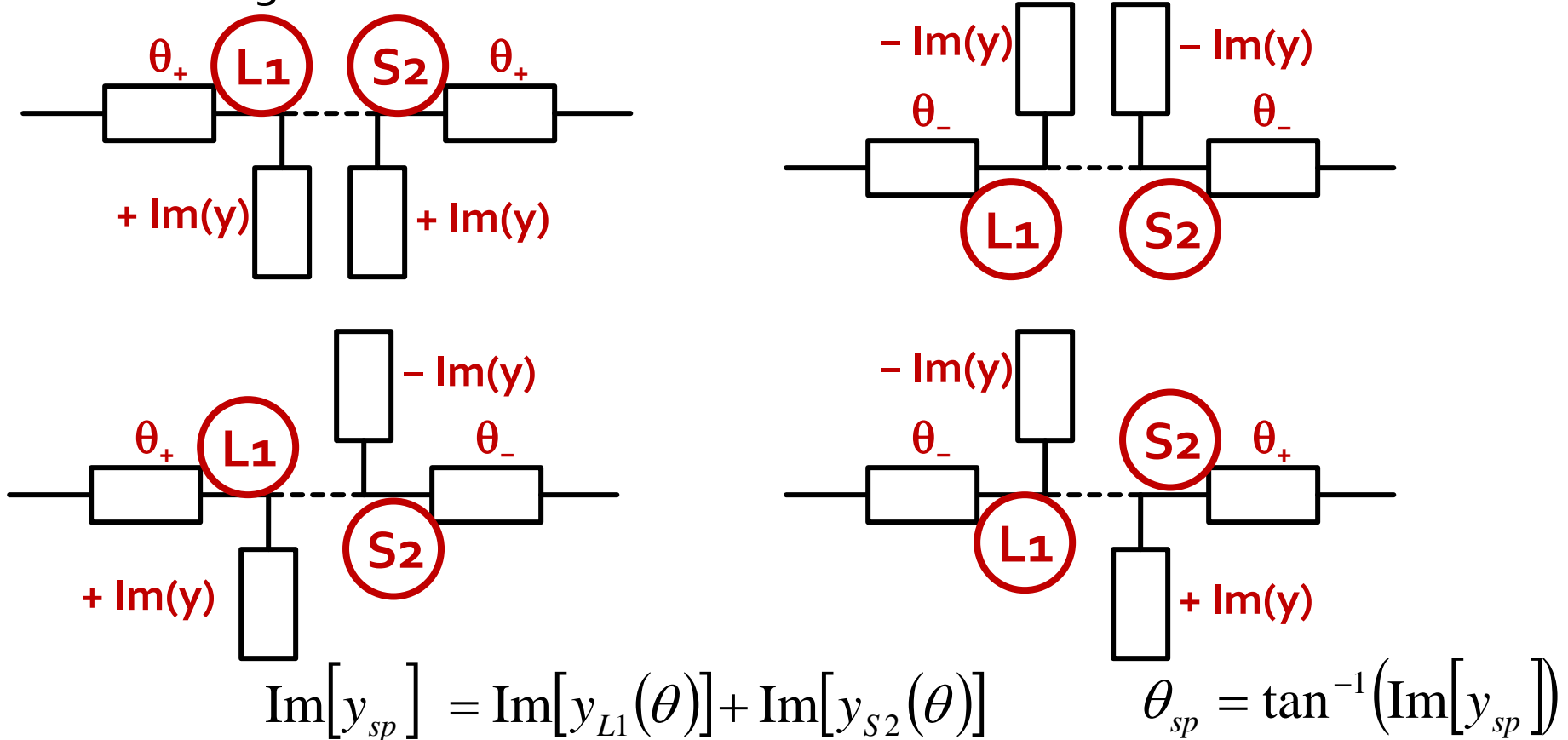
# Merging the two shunt stubs

- **The two shunt stubs merge into a single one**
- There are **4 possible combinations** depending on how we chose the electrical length for the two series lines
  - for each chosen electric length ( $\theta$ ) the corresponding  $\text{Im}[y(\theta)]$  must be used
- Ex:

$$\theta_{L1} = 116.8^\circ \quad \theta_{S2} = 130.1^\circ \quad \text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = -1.418$$
$$\theta_{sp} = \tan^{-1}(\text{Im}[y_{sp}]) \quad \theta_{sp} = 125.2^\circ$$

# Merging the two shunt stubs

- 4 possible combinations
  - the **admittances** are in parallel and **add** up, not the electrical lengths

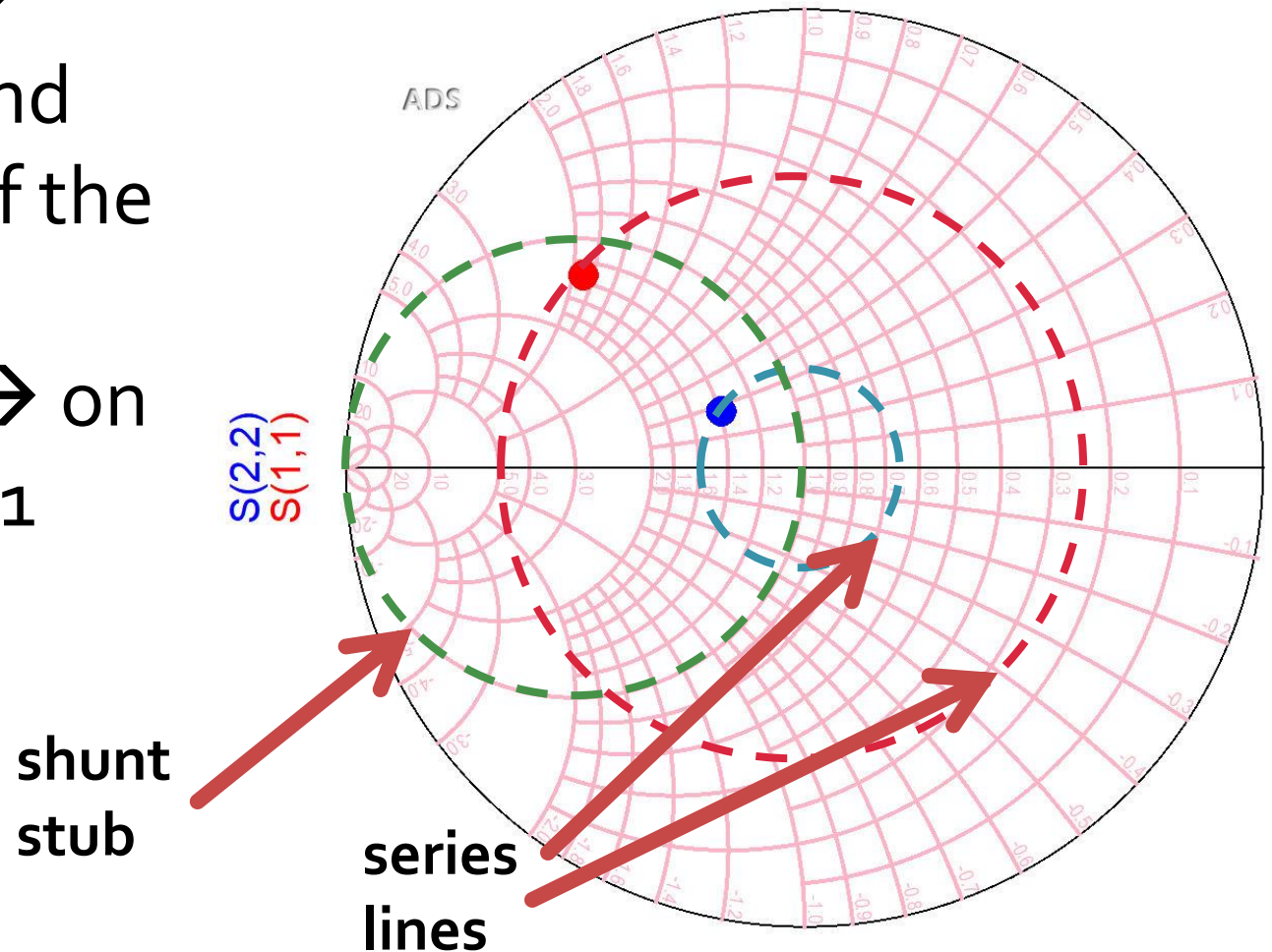


# Merging the two shunt stubs

|                     |   | Solution S2A  | Solution S2B   |
|---------------------|---|---|--|
|                     |   | $\theta = 130.1^\circ$<br>$\text{Im}[y(\theta)] = -1.039$   | $\theta = 12.6^\circ$<br>$\text{Im}[y(\theta)] = +1.039$   |
| <b>Solution L1A</b> | $\theta = 116.8^\circ$<br>$\text{Im}[y(\theta)] = -0.379$ | $\theta_{L1} = 116.8^\circ$<br>$\text{Im}[y(\theta)] = -1.418$<br>$\theta_p = 125.2^\circ$<br>$\theta_{S2} = 130.1^\circ$ | $\theta_{L1} = 116.8^\circ$<br>$\text{Im}[y(\theta)] = +0.66$<br>$\theta_p = 33.4^\circ$<br>$\theta_{S2} = 12.6^\circ$ |
| <b>Solution L1B</b> | $\theta = 16.1^\circ$<br>$\text{Im}[y(\theta)] = +0.379$  | $\theta_{L1} = 16.1^\circ$<br>$\text{Im}[y(\theta)] = -0.66$<br>$\theta_p = 146.6^\circ$<br>$\theta_{S2} = 130.1^\circ$   | $\theta_{L1} = 16.1^\circ$<br>$\text{Im}[y(\theta)] = 1.418$<br>$\theta_p = 54.8^\circ$<br>$\theta_{S2} = 12.6^\circ$  |

# Smith Chart

- series line  $\rightarrow$  moves around the center of the SC
- shunt stub  $\rightarrow$  on the circle  $g=1$



# Merge 1, Smith Chart

$$\theta_{L1} = 116.8^\circ \quad \theta_{S2} = 130.1^\circ$$

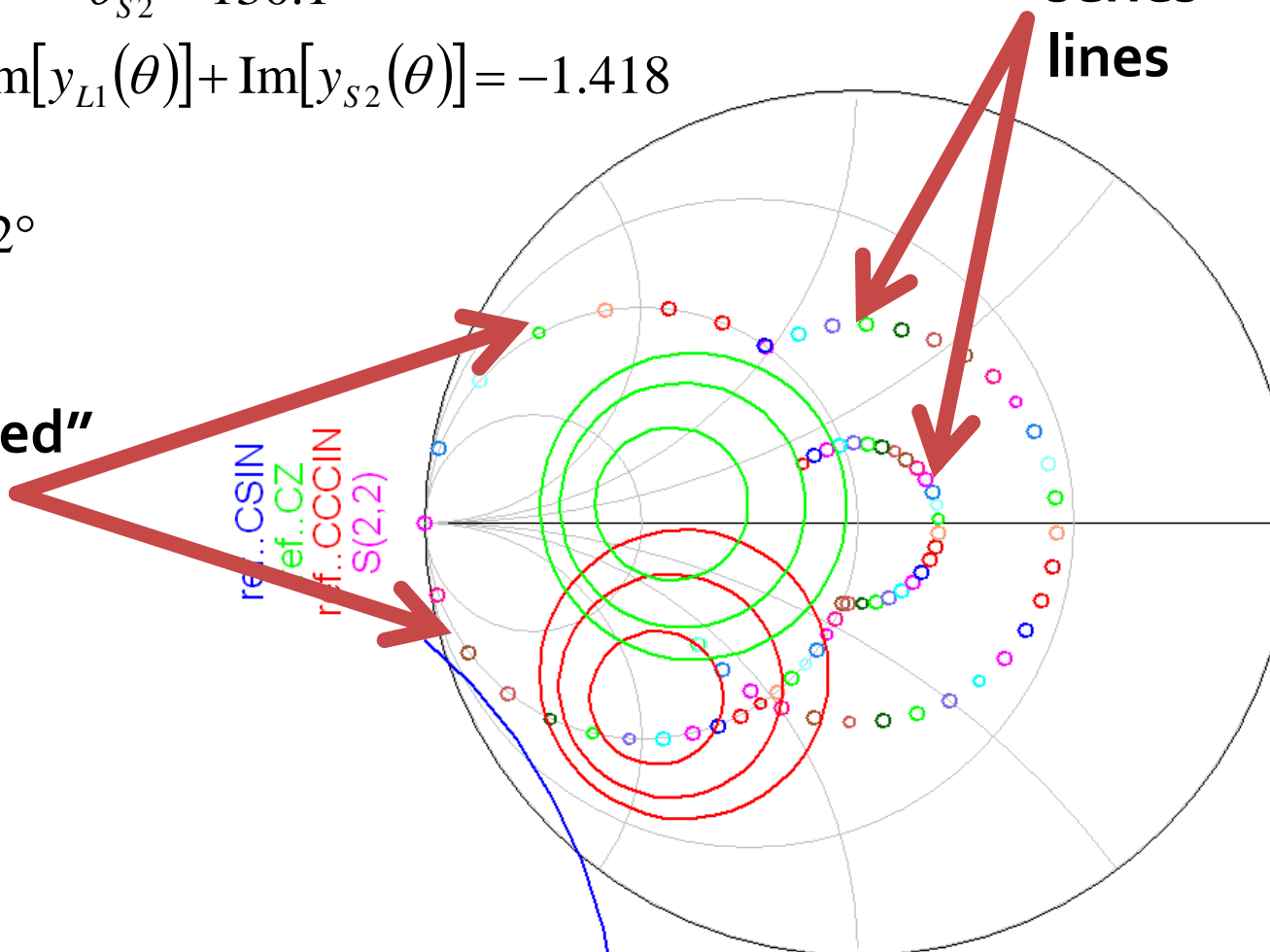
$$\text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = -1.418$$

$$\theta_{sp} = 125.2^\circ$$

“combined”  
stub

ref..CSIN  
ref..CZ  
ref..CCIN  
S(2,2)

series  
lines



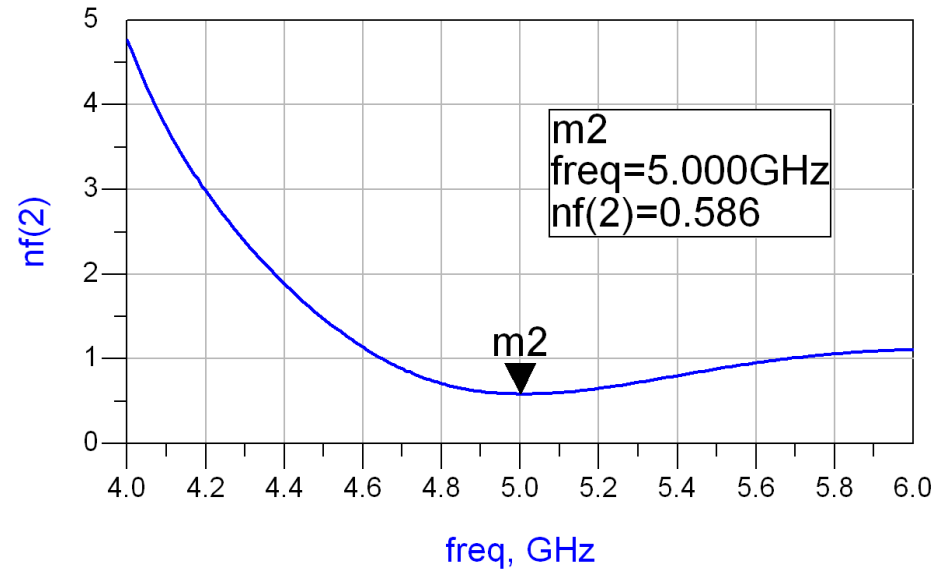
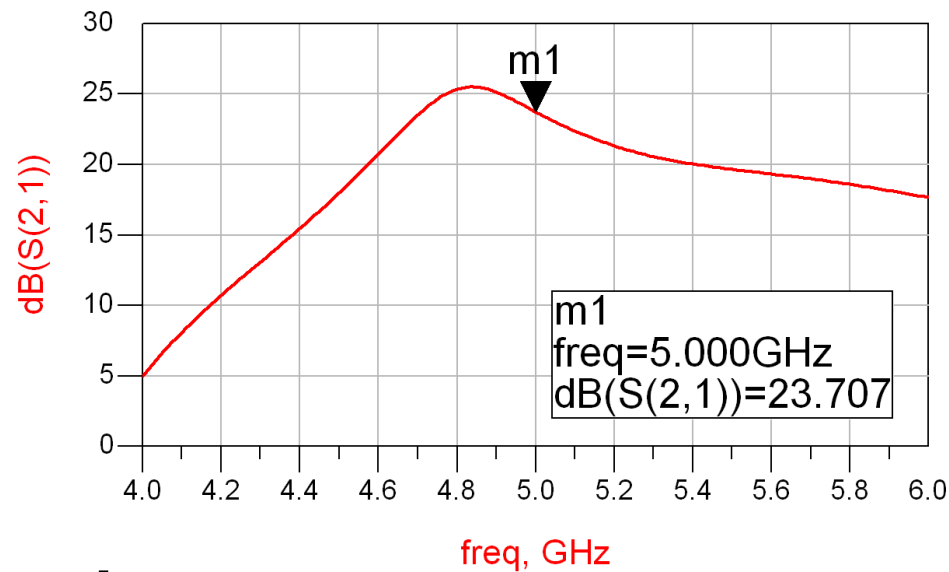
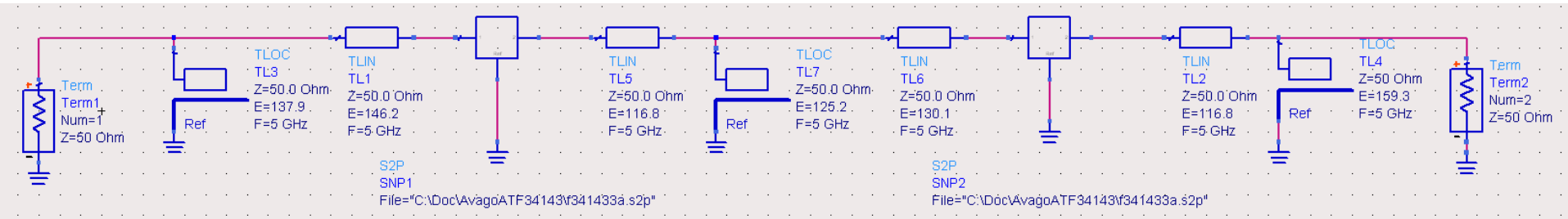
**Tune Control**

Select a parameter to tune by clicking on it

Simulate:

Trace History:

# Merge 1, ADS



# Merge 2, Smith Chart

$$\theta_{L1} = 116.8^\circ \quad \theta_{S2} = 12.6^\circ$$

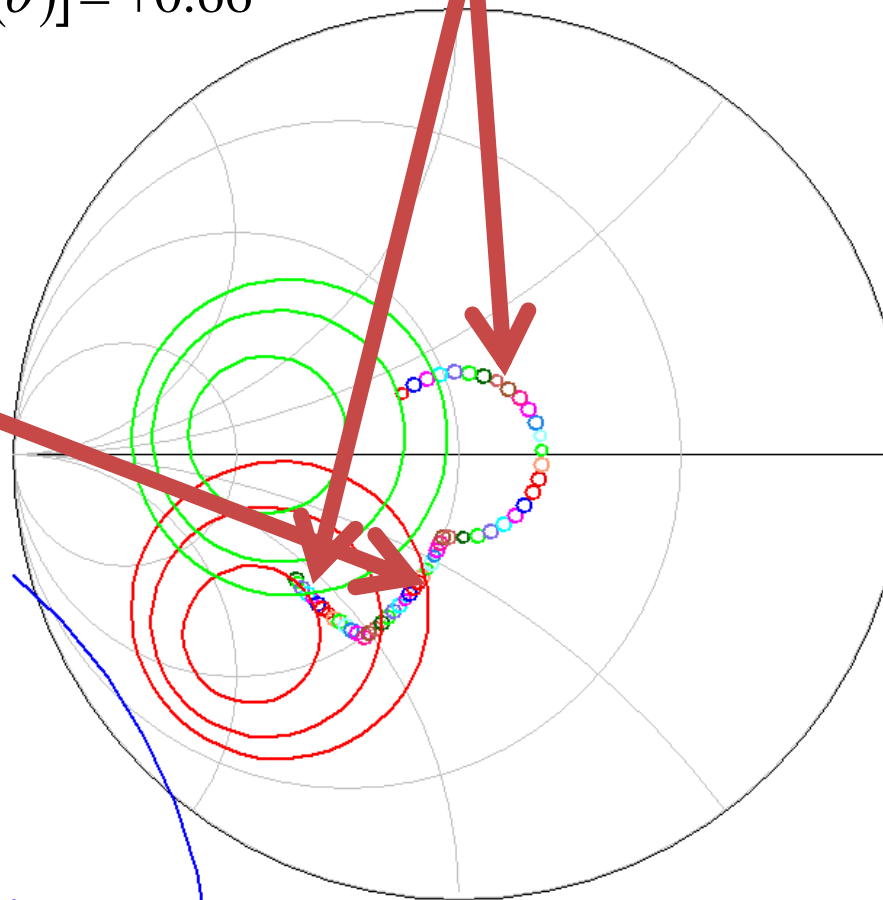
$$\text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = +0.66$$

$$\theta_{sp} = 33.4^\circ$$

“combined”  
stub

ref..CSIN  
ref..CZ  
ref..CCCN  
S(2,2)

series  
lines



**Tune Control**

Select a parameter to tune by clicking on it

Simulate:

Trace History:

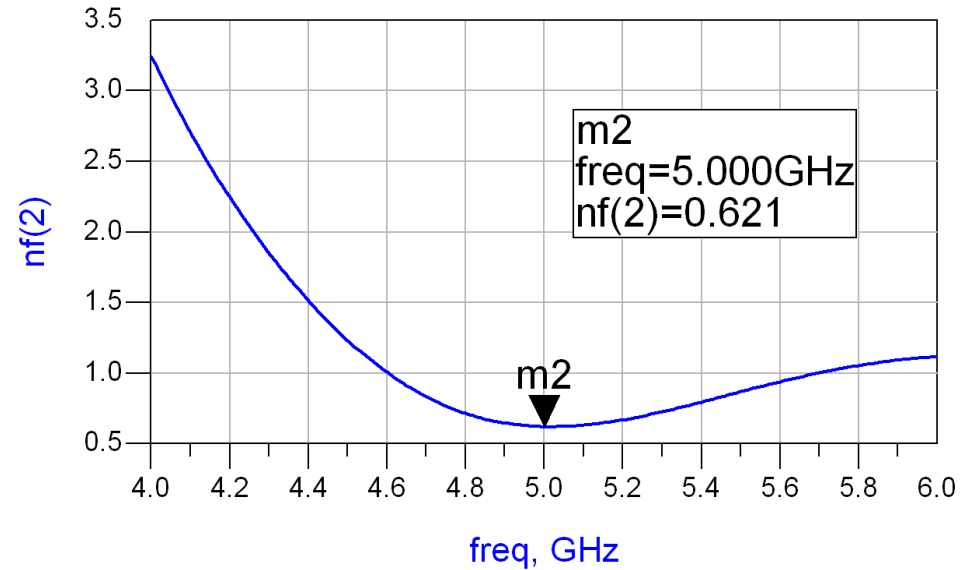
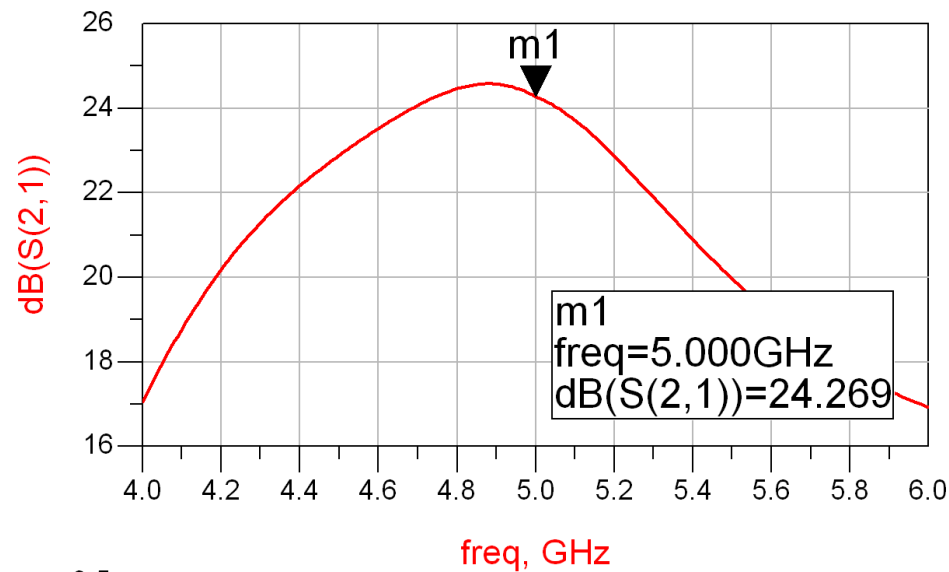
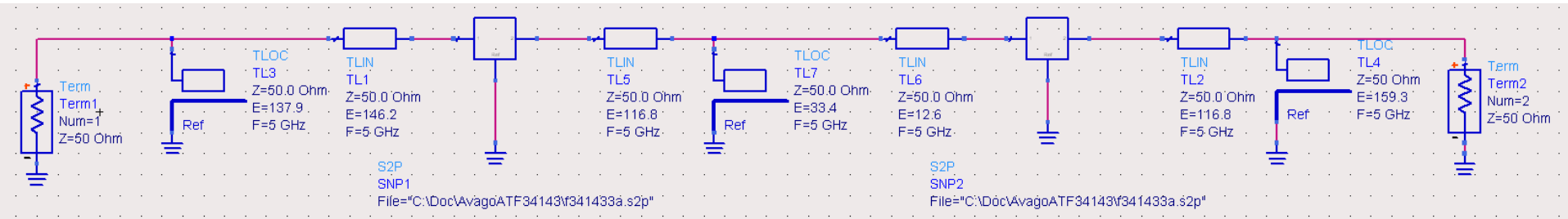
lini\_inter\_smith2.TL1.E

lini\_inter\_smith2.TL2.E

lini\_inter\_smith2.TL3.E



# Merge 2, ADS



# Merge 3, Smith Chart

$$\theta_{L1} = 16.1^\circ \quad \theta_{S2} = 130.1^\circ$$

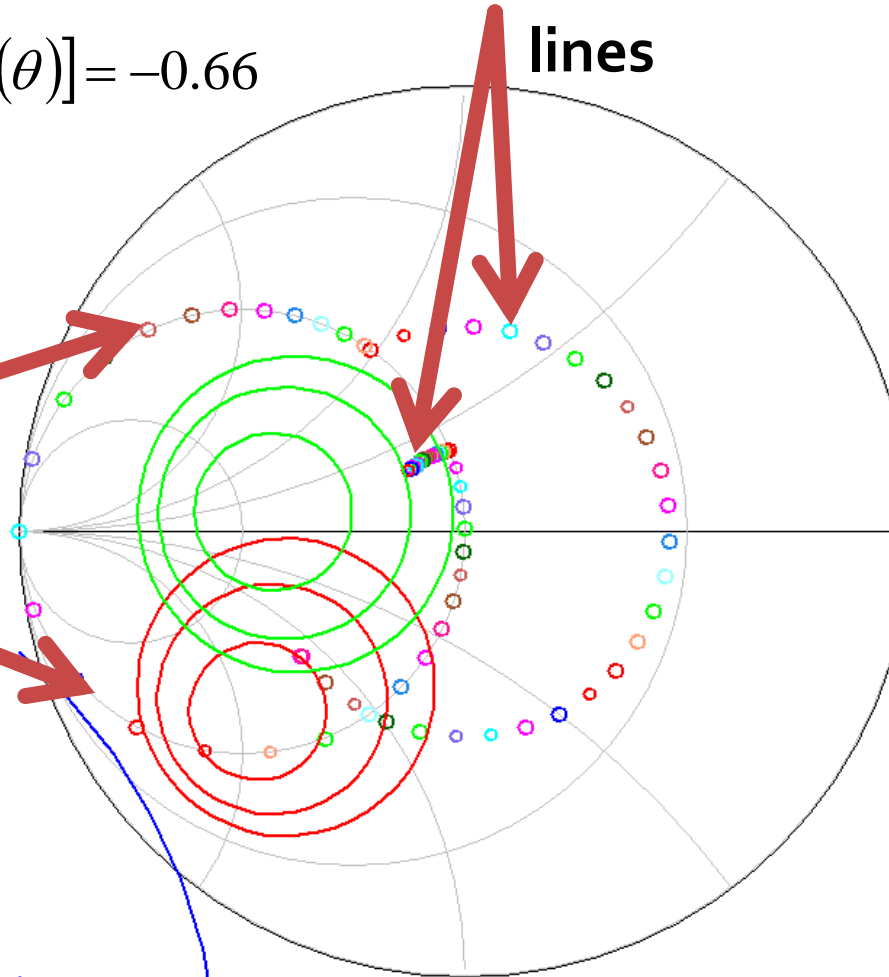
$$\text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = -0.66$$

$$\theta_{sp} = 146.6^\circ$$

“combined”  
stub

ref..CSIN  
ref..CZ  
ef..CCIN  
S(2,2)

series  
lines



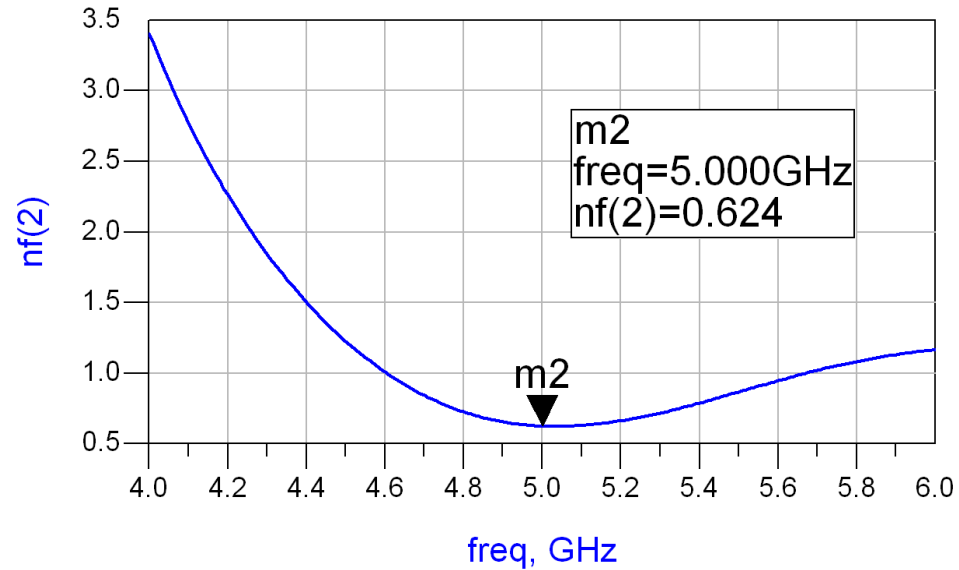
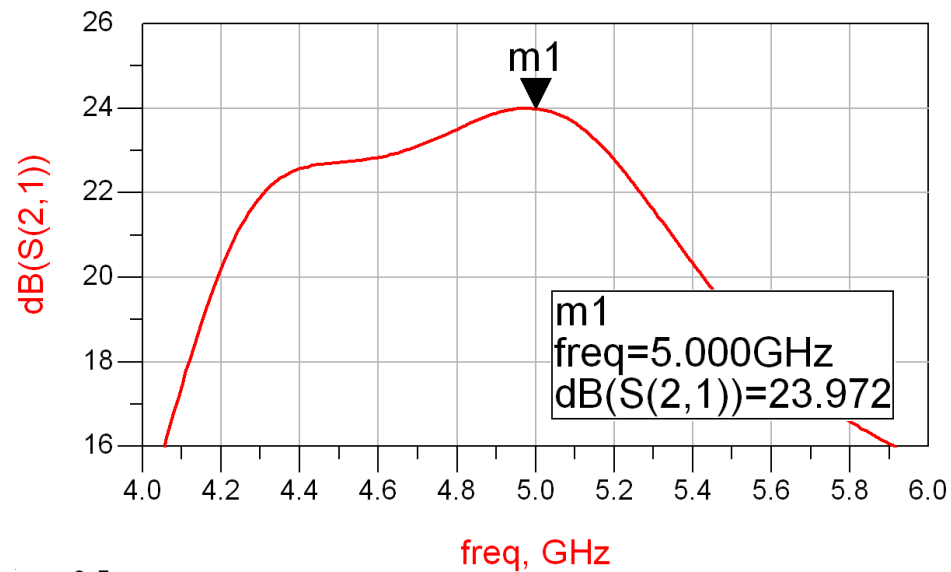
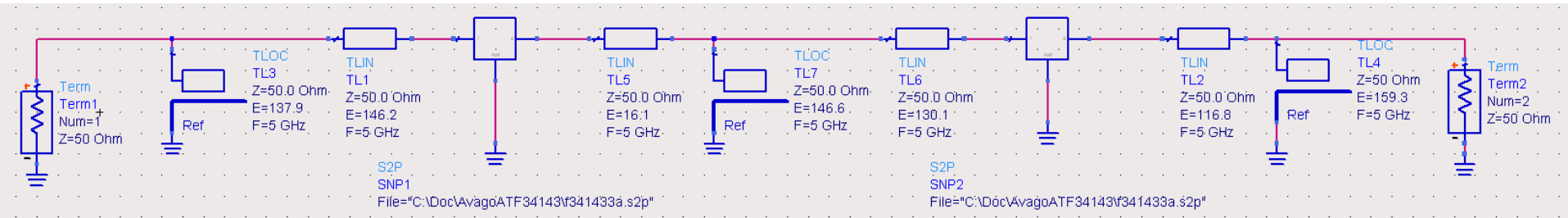
**Tune Control**

Select a parameter to tune by clicking on it

Simulate:

Trace History:

# Merge 3, ADS



# Merge 4, Smith Chart

$$\theta_{L1} = 16.1^\circ \quad \theta_{S2} = 12.6^\circ$$

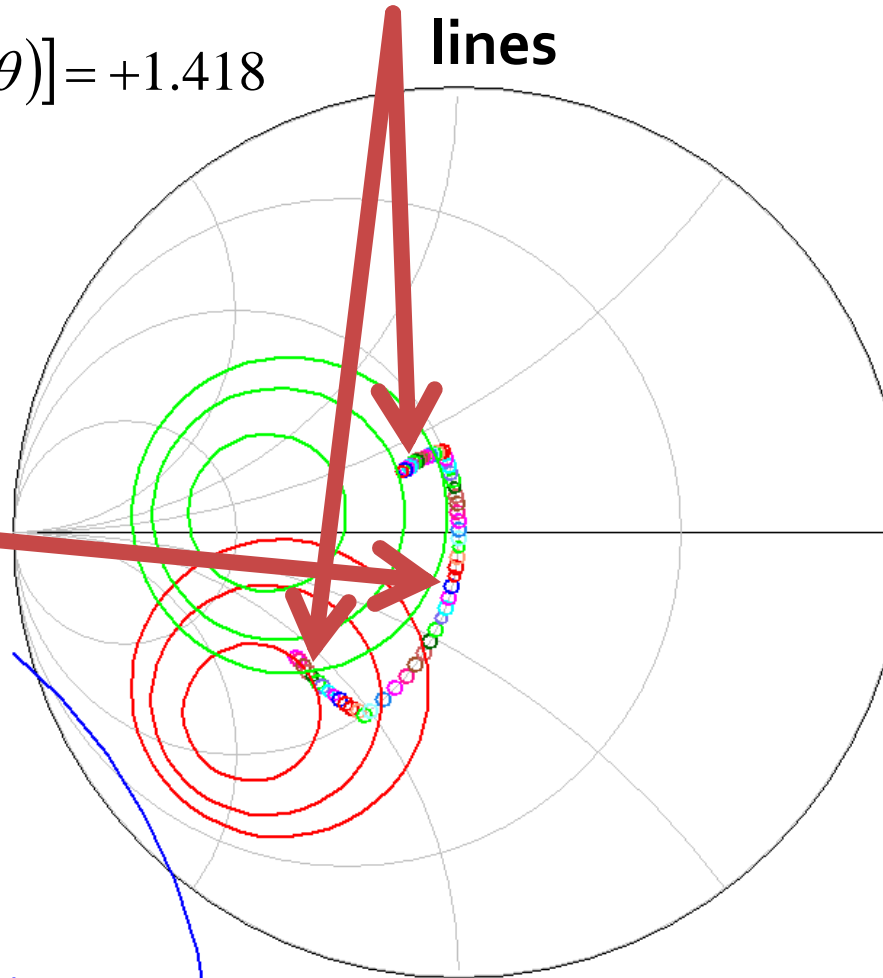
$$\text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = +1.418$$

$$\theta_{sp} = 54.8^\circ$$

“combined”  
stub

ref.:CSIN  
ref.:CZ  
ref.:CCIN  
S(1,2)

series  
lines



**Tune Control**

Select a parameter to tune by clicking on it

Simulate:

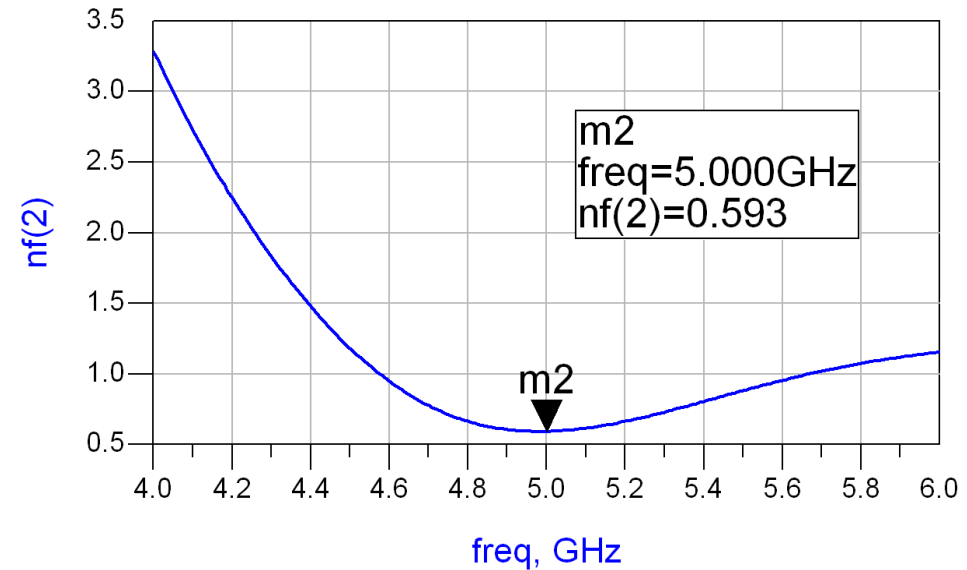
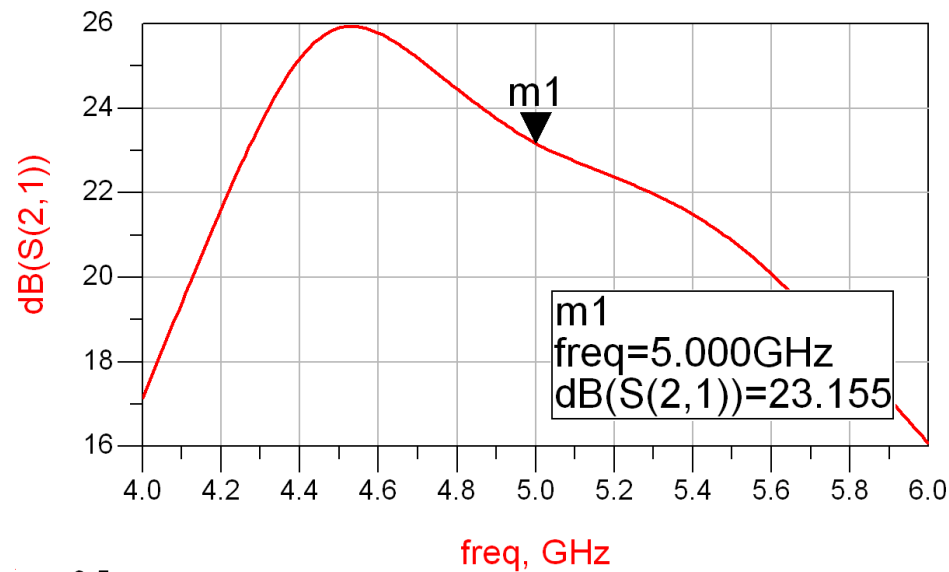
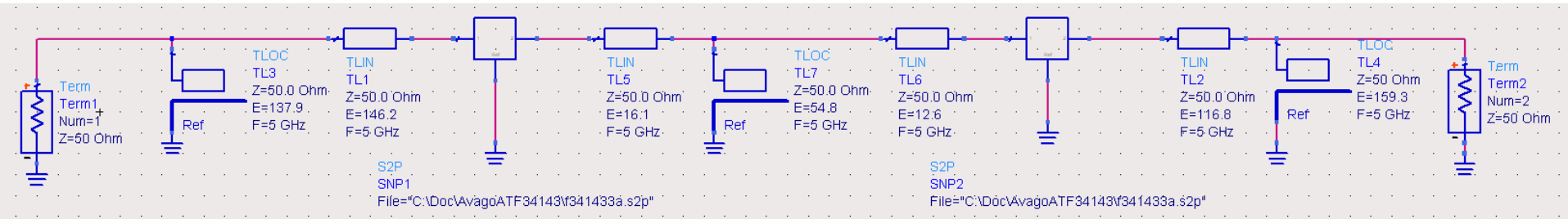
Trace History:

lini\_inter\_smith2.TL1.E

lini\_inter\_smith2.TL2.E

lini\_inter\_smith2.TL3.E

# Merge 4, ADS



# Interstage matching 2

- All the combinations obtained meet the target conditions for gain and noise
- Choose a convenient one depending on:
  - the physical dimensions of the lines  $l = \frac{\theta}{360^\circ} \cdot \lambda$
  - frequency bandwidth/flatness
  - stability
  - performance (noise/gain)
  - input and output reflection
  - etc.

# Supplement Mini Project

# Implementation in microstrip technology

- microstrip lines
  - dielectric layer
  - plane metallization (ground plane)
  - traces which will control:
    - characteristic impedance
    - physical/electrical length

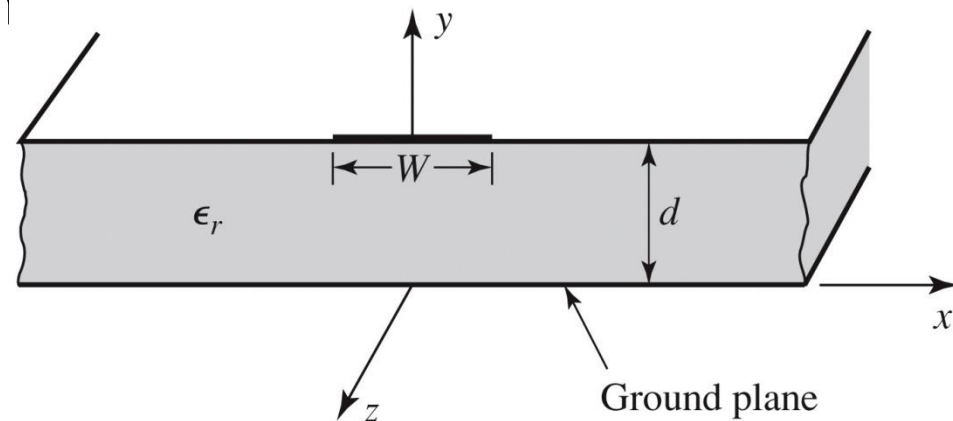


Figure 3.25a  
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# Implementation in microstrip technology

- quasi TEM line

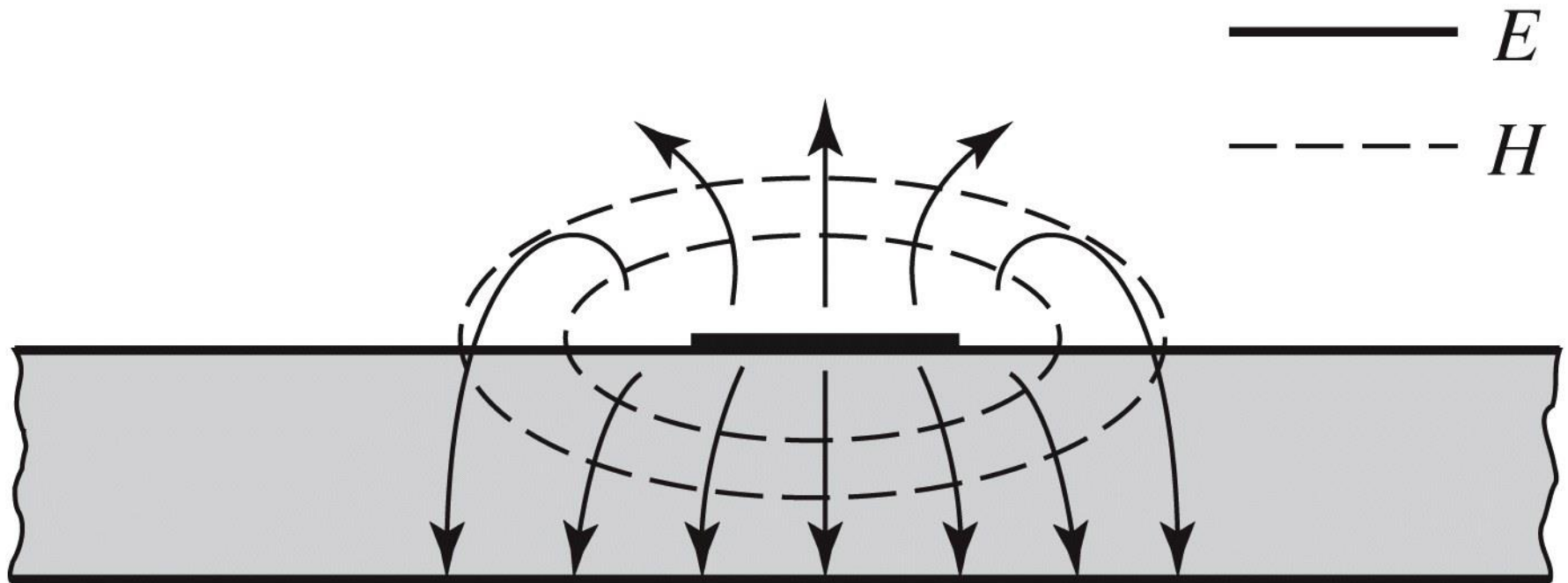
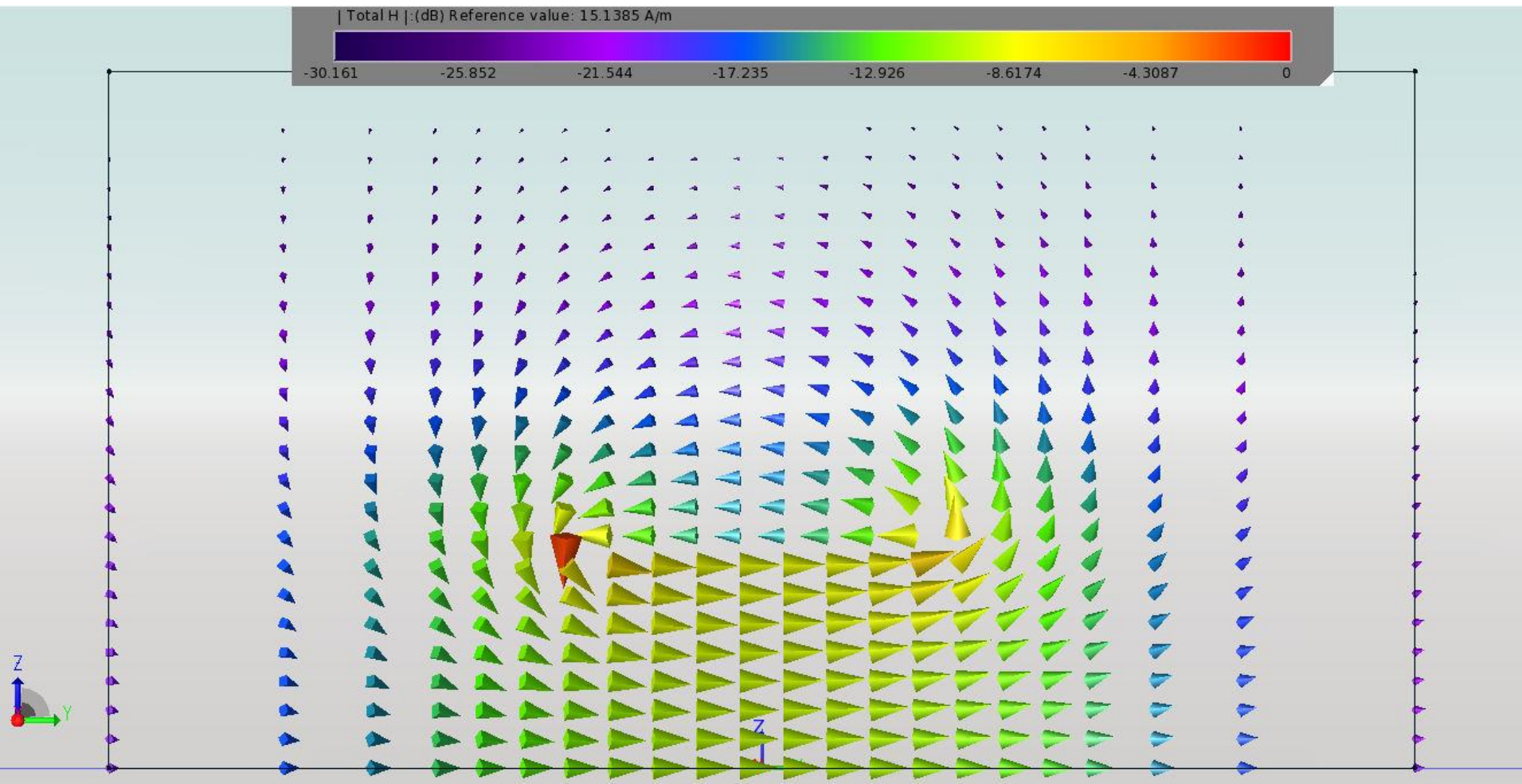


Figure 3.25b

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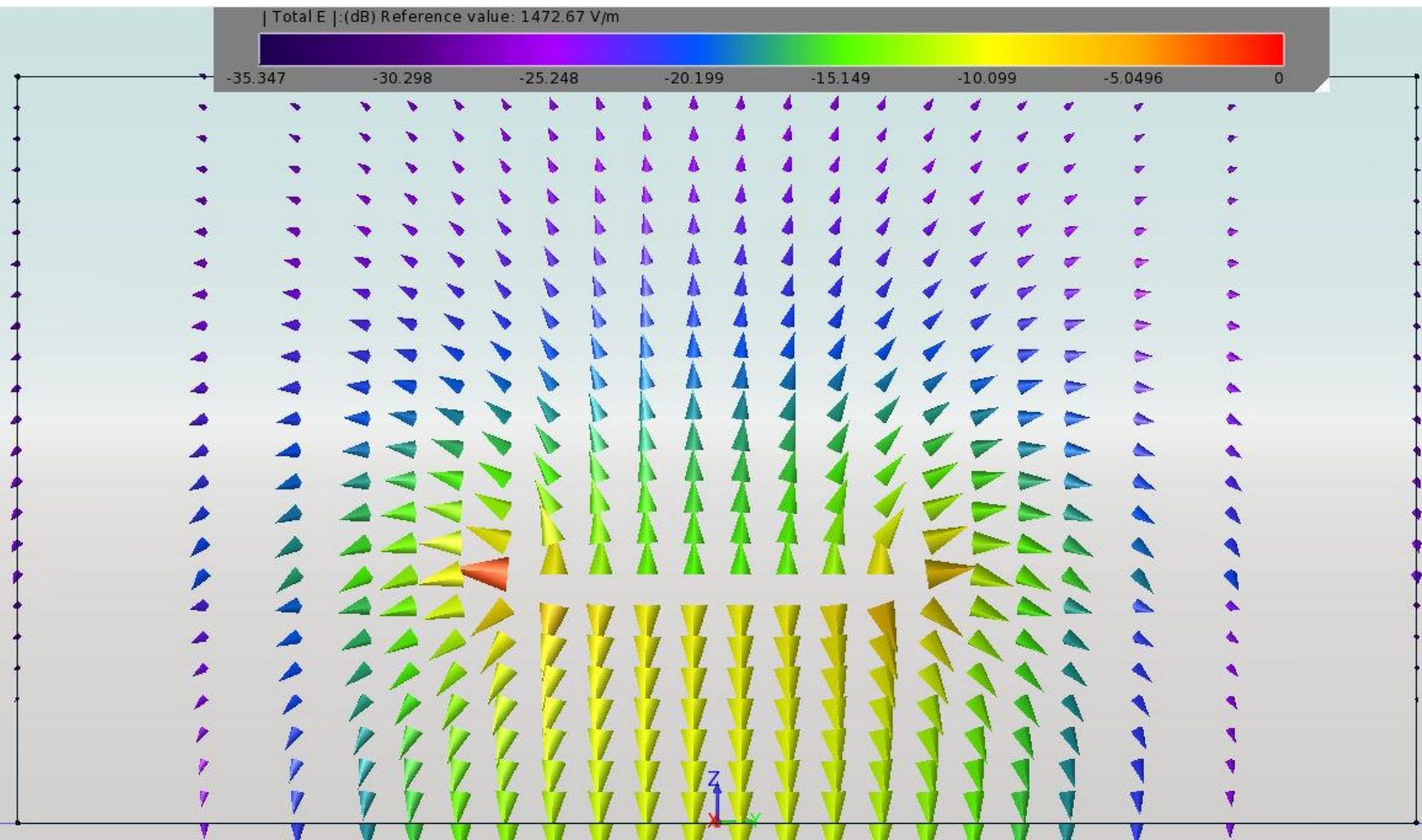
# Implementation in microstrip technology

- quasi TEM line, EmPro



# Implementation in microstrip technology

- quasi TEM line, EmPro

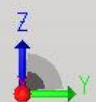
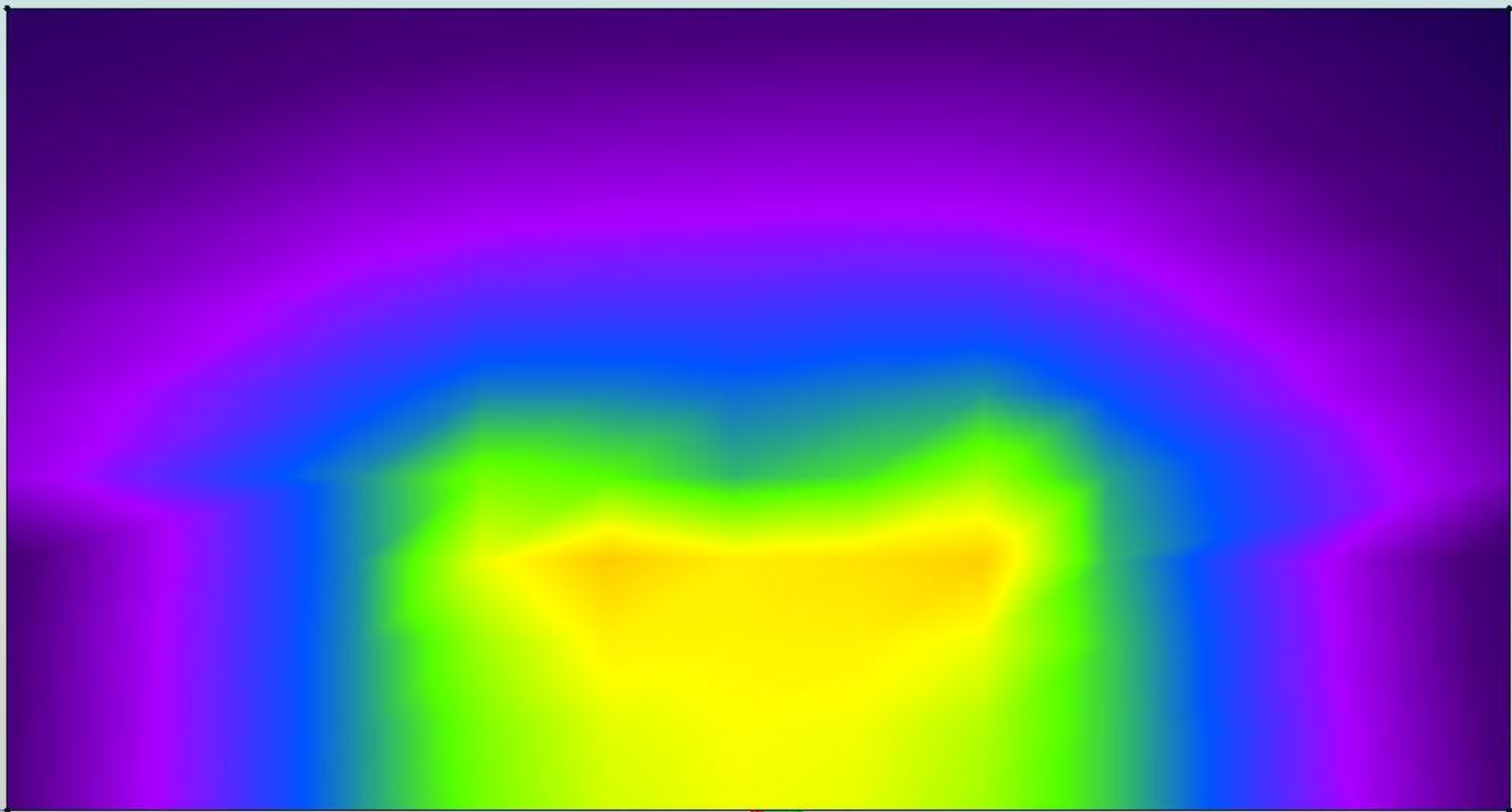


# Implementation in microstrip technology

- quasi TEM line, EmPro

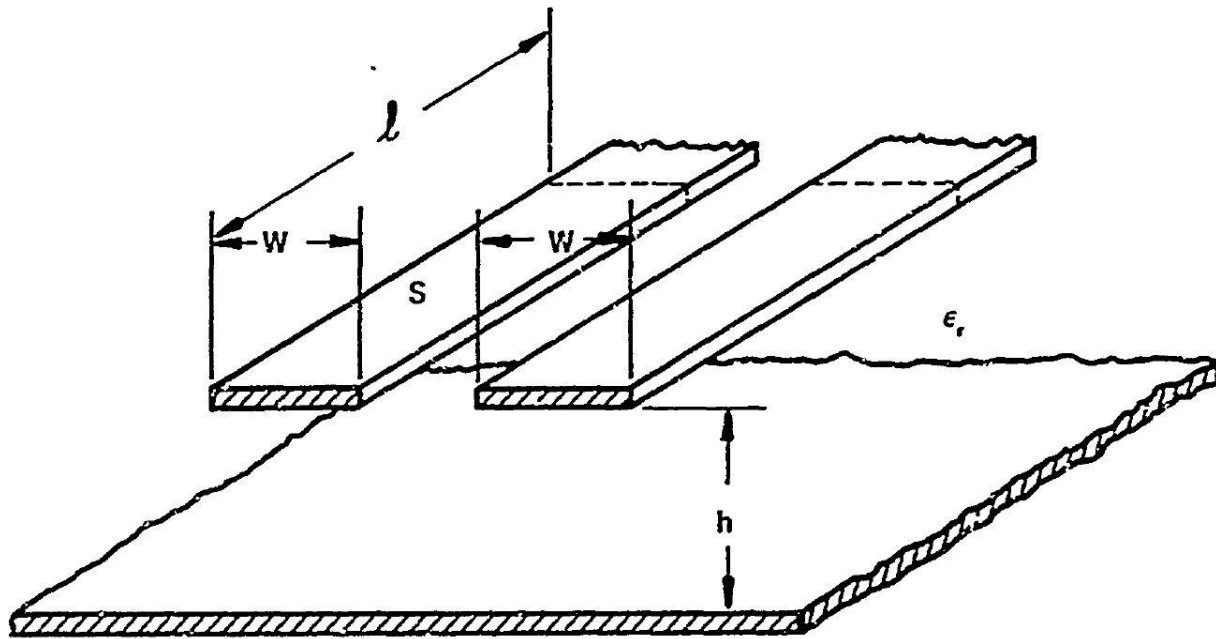


( 85, 42, 48 )



# Implementation in microstrip technology

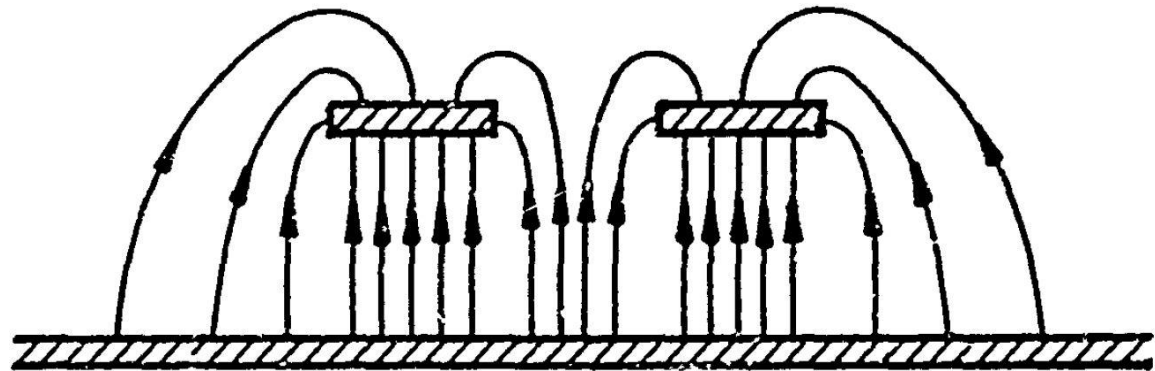
- ~ quasi TEM



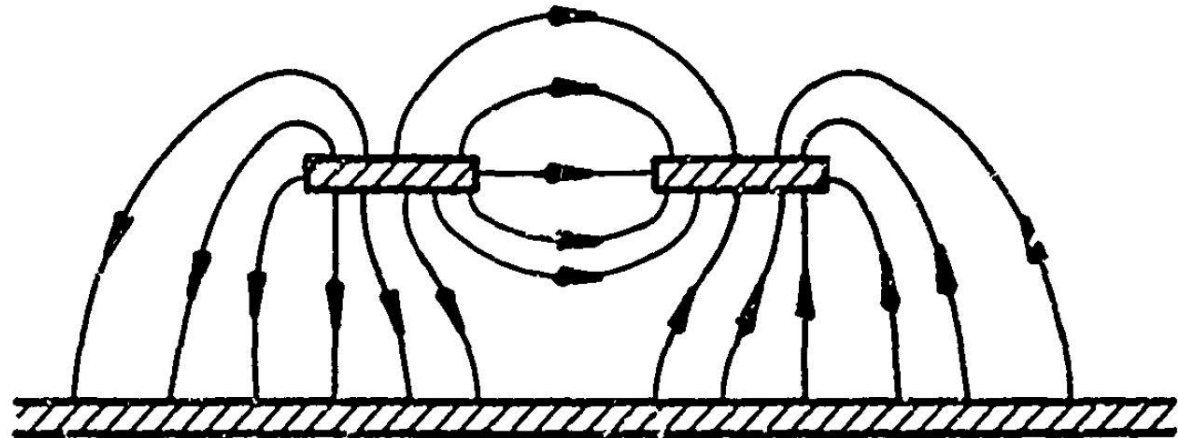
a) COUPLED STRIP GEOMETRY

# Implementation in microstrip technology

- ~ quasi TEM



b) EVEN MODE ELECTRIC FIELD PATTERN (SCHEMATIC)



c) ODD MODE ELECTRIC FIELD PATTERN (SCHEMATIC)

# Implementation in microstrip technology

- Equivalent geometry of a quasi-TEM microstrip line with effective dielectric constant homogeneous medium

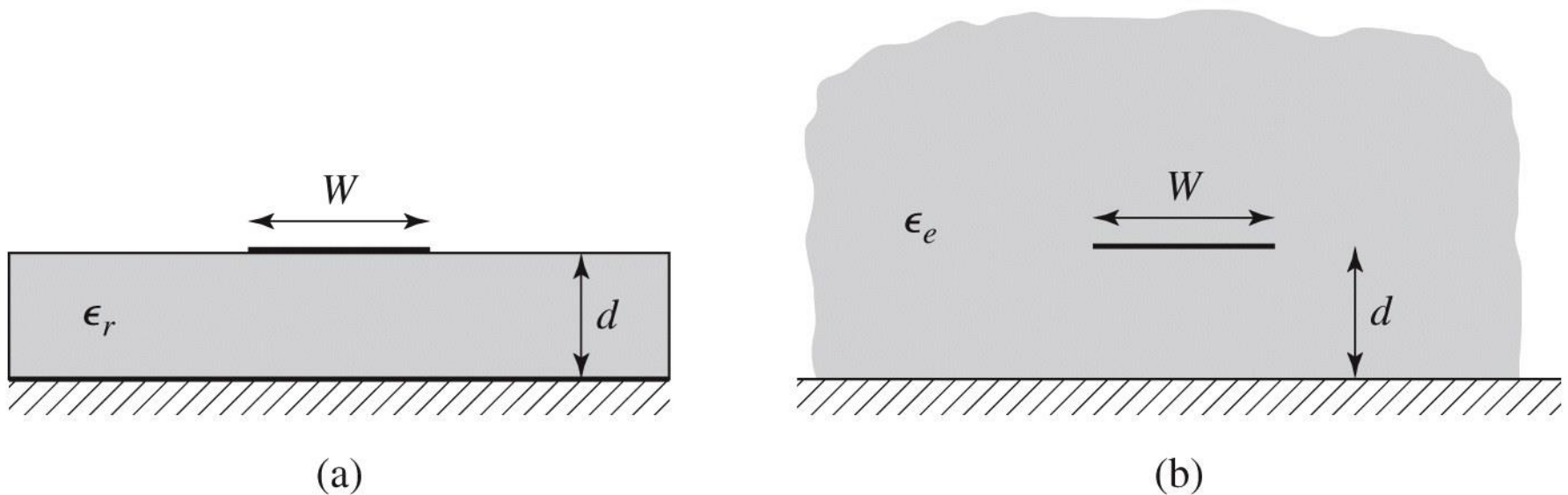


Figure 3.26  
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# Design

## ■ Empirical formulas

$$v_p = \frac{c}{\sqrt{\epsilon_e}},$$

$$\beta = k_0 \sqrt{\epsilon_e},$$

$$\epsilon_e = \frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{2} \frac{1}{\sqrt{1 + 12d/W}}.$$

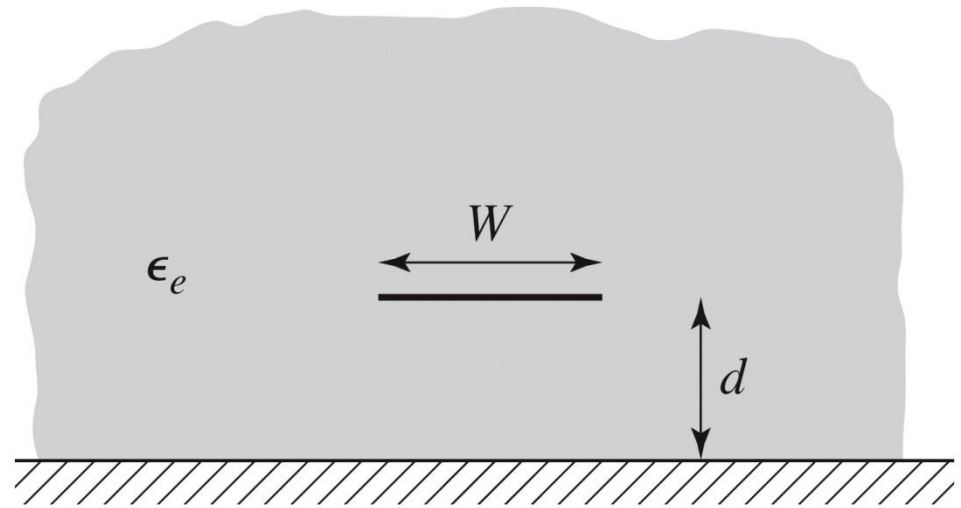


Figure 3.26b  
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$$Z_0 = \begin{cases} \frac{60}{\sqrt{\epsilon_e}} \ln \left( \frac{8d}{W} + \frac{W}{4d} \right) & \text{for } W/d \leq 1 \\ \frac{120\pi}{\sqrt{\epsilon_e} [W/d + 1.393 + 0.667 \ln (W/d + 1.444)]} & \text{for } W/d \geq 1. \end{cases}$$



# Design

- Empirical formulas

$$A = \frac{Z_0}{60} \sqrt{\frac{\epsilon_r + 1}{2}} + \frac{\epsilon_r - 1}{\epsilon_r + 1} \left( 0.23 + \frac{0.11}{\epsilon_r} \right)$$

$$B = \frac{377\pi}{2Z_0\sqrt{\epsilon_r}}$$

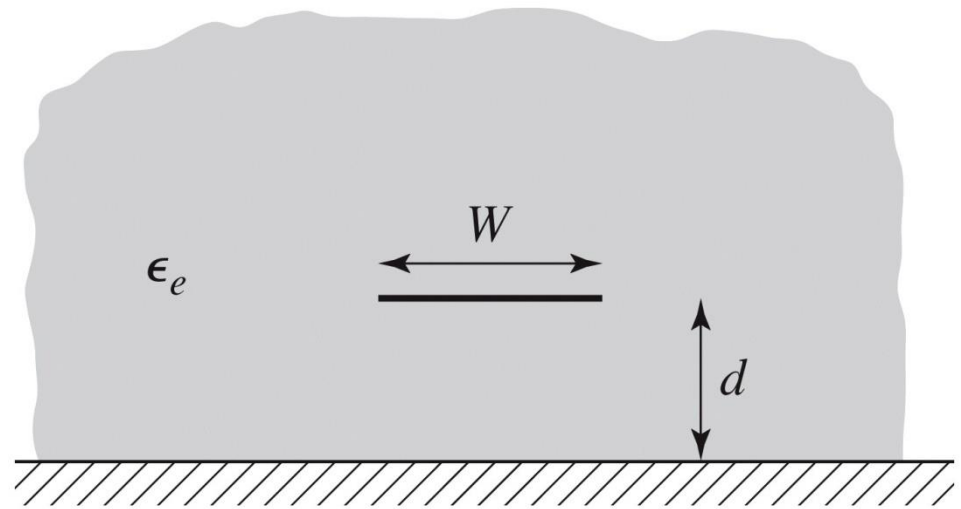
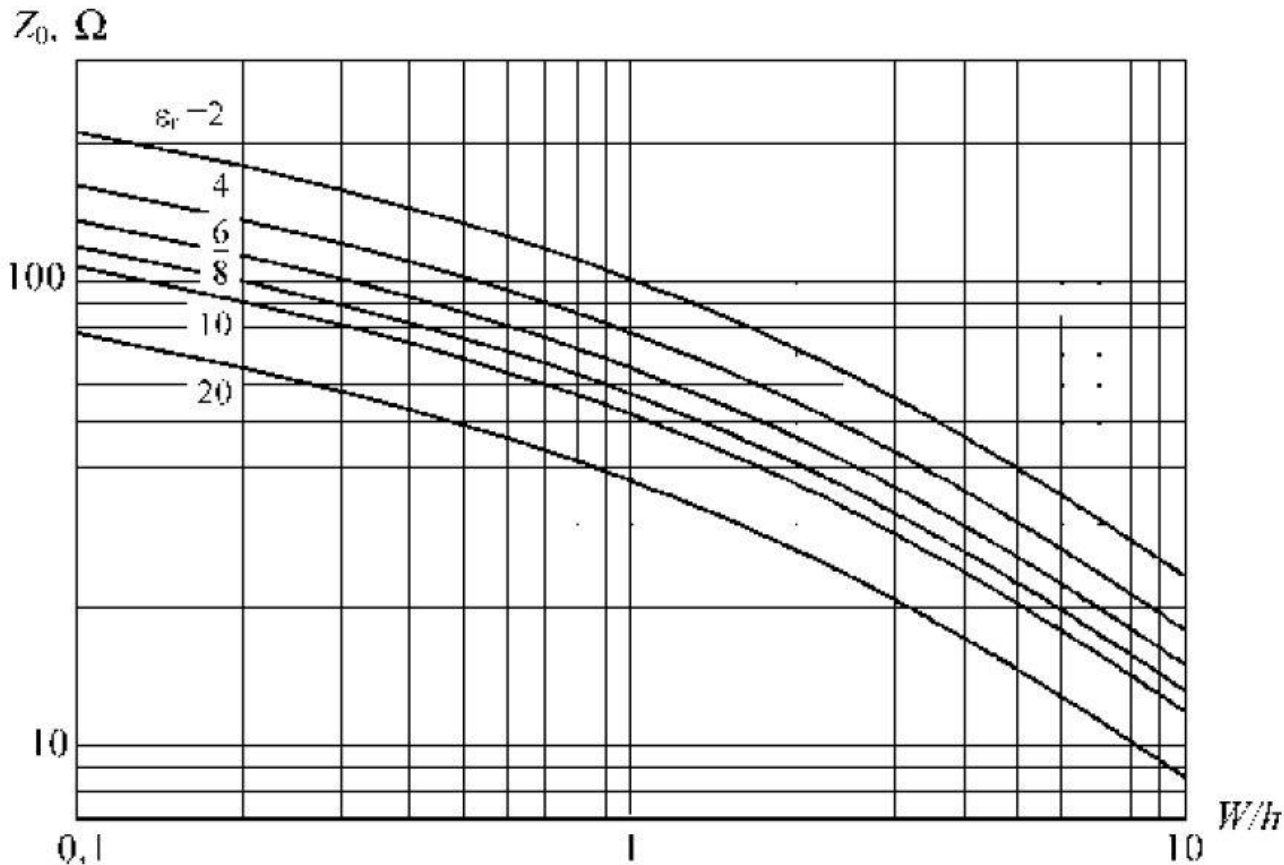


Figure 3.26b  
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$$\frac{W}{d} = \begin{cases} \frac{8e^A}{e^{2A} - 2} & \text{for } W/d < 2 \\ \frac{2}{\pi} \left[ B - 1 - \ln(2B - 1) + \frac{\epsilon_r - 1}{2\epsilon_r} \left\{ \ln(B - 1) + 0.39 - \frac{0.61}{\epsilon_r} \right\} \right] & \text{for } W/d > 2, \end{cases}$$

# Characteristic impedance

- **Large impedances** require **narrow traces**
- **Small impedances** require **wide traces**



$$k_0 = \frac{2\pi f}{c}$$
$$\beta l = \sqrt{\epsilon_e} k_0 l,$$

# Microstrip standardization

- Standardization
  - dimensions in **mil**
  - 1 mil =  $10^{-3}$  inch
  - 1 inch = 2.54 cm
- Trace thickness
  - based on the weight of the deposited copper
  - oz/ft<sup>2</sup>
  - 1oz=28.35g and 1ft=30.48cm

| Weight of the deposited copper |                   | Trace thickness |        |
|--------------------------------|-------------------|-----------------|--------|
| oz/ft <sup>2</sup>             | g/ft <sup>2</sup> | inch            | mm     |
| 0.5                            | 14.175            | 0.0007          | 0.0178 |
| 1.0                            | 28.35             | 0.0014          | 0.0356 |
| 2.0                            | 56.7              | 0.0028          | 0.0712 |

# Microstrip standardization

- Typically the height of the dielectric layers is also standardized in mil

Standard Thickness

**RO4003C:**

0.008" (0.203mm), 0.012 (0.305mm), 0.016" (0.406mm),  
0.020" (0.508mm)

0.032" (0.813mm), 0.060" (1.524mm)

**RO4350B:**

\*0.004" (0.101mm), 0.0066" (0.168mm) 0.010" (0.254mm),  
0.0133 (0.338mm), 0.0166 (0.422mm), 0.020" (0.508mm)

0.030" (0.762mm), 0.060" (1.524mm)

# ADS linecalc

- In schematics: >Tools>LineCalc>Start
- for Microstrip lines >Tools>LineCalc>Send to Linecalc

The screenshot displays the ADS LineCalc software interface. The window title is "LineCalc/untitled". The menu bar includes "File", "Simulation", "Options", and "Help". The interface is divided into several sections:

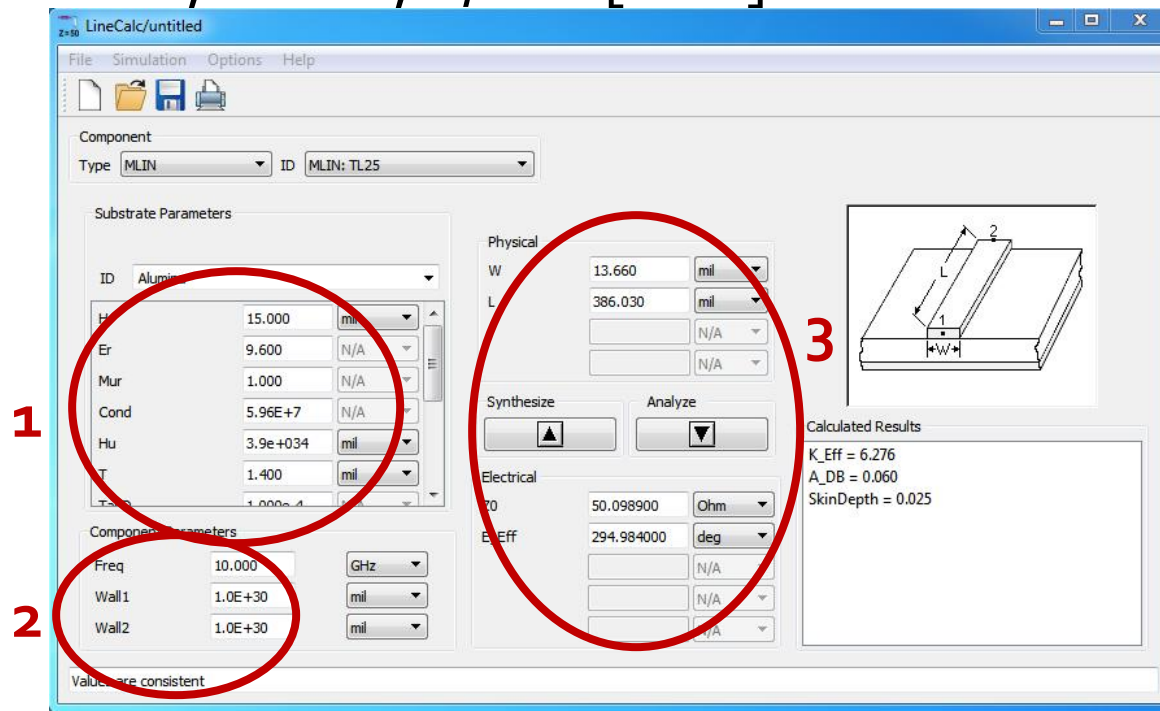
- Component:** Type: MLIN, ID: MLIN: TL25
- Substrate Parameters:** ID: Alumina, H: 15.000 mil, Er: 9.600 N/A, Mur: 1.000 N/A, Cond: 5.96E+7 N/A, Hu: 3.9e+034 mil, T: 1.400 mil, TanD: 1.000e-4 N/A
- Physical:** W: 13.660 mil, L: 386.030 mil
- Electrical:** Z0: 50.098900 Ohm, E\_Eff: 294.984000 deg
- Calculated Results:** K\_Eff = 6.276, A\_DB = 0.060, SkinDepth = 0.025

A diagram on the right shows a 3D perspective of a microstrip line on a substrate, with labels for width (W), length (L), and height (H). The width is labeled with a double-headed arrow and 'W', the length with 'L', and the height with 'H'. The substrate is labeled '1' and the microstrip line is labeled '2'.

Values are consistent

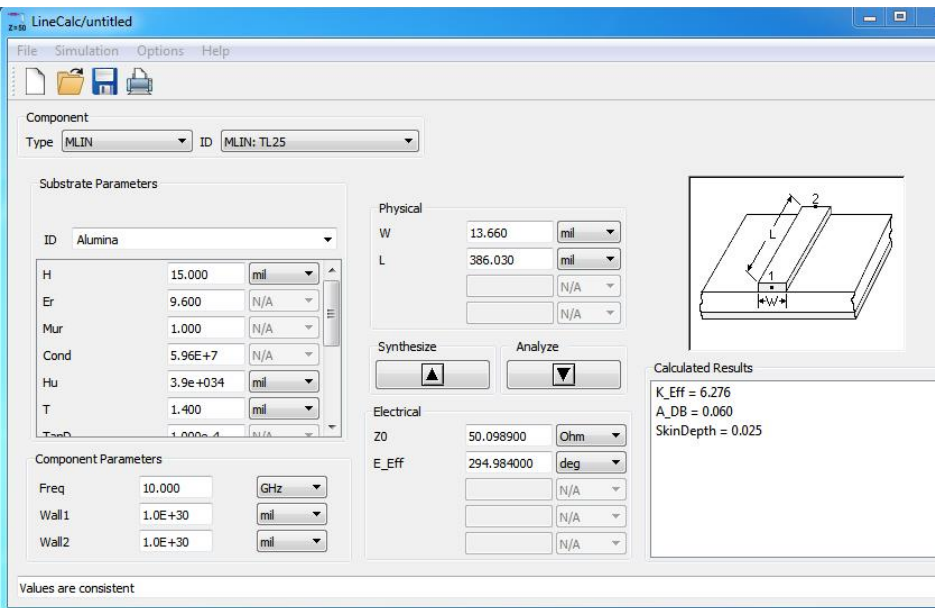
# ADS linecalc

- 1. Define substrate (receive from schematic)
- 2. Insert frequency
- 3. Insert input data
  - Analyze:  $W, L \rightarrow Z_o, E$  or  $Z_e, Z_o, E$  / at  $f$  [GHz]
  - Synthesis:  $Z_o, E \rightarrow W, L$  / at  $f$  [GHz]



# ADS linecalc

- Can be used for:
  - microstrip lines MLIN:  $W, L \Leftrightarrow Z_0, E$
  - microstrip coupled lines MCLIN:  $W, L, S \Leftrightarrow Z_e, Z_0, E$



The screenshot shows the ADS LineCalc/untitled window for a single microstrip line (MLIN). The component type is MLIN and the ID is MLIN: TL25. The substrate parameters are set to Alumina. The physical parameters are W = 13.660 mil and L = 386.030 mil. The calculated results are K\_Eff = 6.276, A\_DB = 0.060, and SkinDepth = 0.025. The diagram shows a single microstrip line on a substrate with width W and length L.

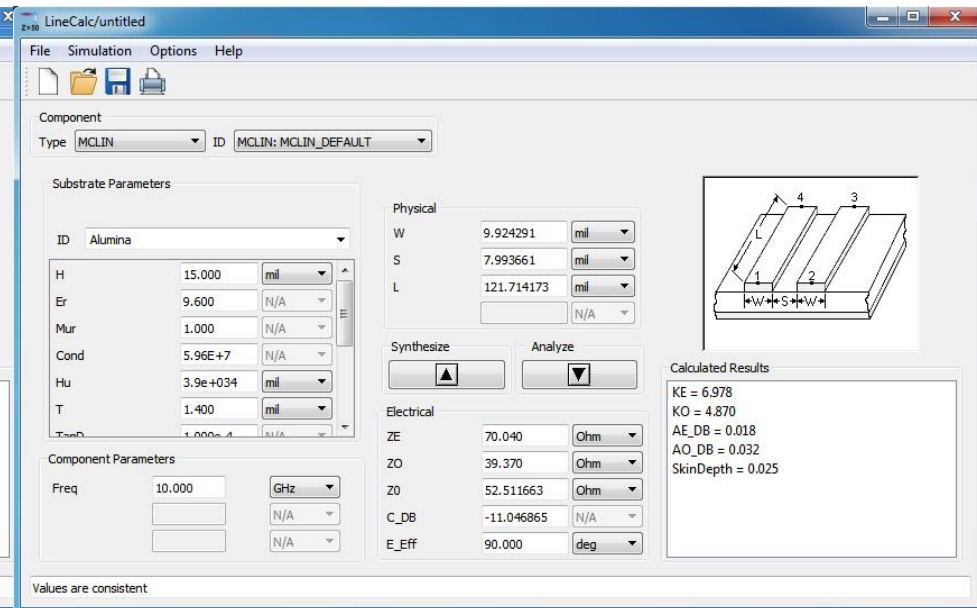
| Parameter | Value    | Unit |
|-----------|----------|------|
| W         | 13.660   | mil  |
| L         | 386.030  | mil  |
| H         | 15.000   | mil  |
| Er        | 9.600    | N/A  |
| Mur       | 1.000    | N/A  |
| Cond      | 5.96E+7  | N/A  |
| Hu        | 3.9e+034 | mil  |
| T         | 1.400    | mil  |
| Ze        | 1.000E+4 | N/A  |

| Parameter | Value      | Unit |
|-----------|------------|------|
| Z0        | 50.098900  | Ohm  |
| E_Eff     | 294.984000 | deg  |

Calculated Results

- K\_Eff = 6.276
- A\_DB = 0.060
- SkinDepth = 0.025

Values are consistent



The screenshot shows the ADS LineCalc/untitled window for a microstrip coupled line (MCLIN). The component type is MCLIN and the ID is MCLIN: MCLIN\_DEFAULT. The substrate parameters are set to Alumina. The physical parameters are W = 9.924291 mil, S = 7.993661 mil, and L = 121.714173 mil. The calculated results are KE = 6.978, KO = 4.870, AE\_DB = 0.018, AO\_DB = 0.032, and SkinDepth = 0.025. The diagram shows two microstrip lines on a substrate with width W, spacing S, and length L.

| Parameter | Value      | Unit |
|-----------|------------|------|
| W         | 9.924291   | mil  |
| S         | 7.993661   | mil  |
| L         | 121.714173 | mil  |
| H         | 15.000     | mil  |
| Er        | 9.600      | N/A  |
| Mur       | 1.000      | N/A  |
| Cond      | 5.96E+7    | N/A  |
| Hu        | 3.9e+034   | mil  |
| T         | 1.400      | mil  |
| Ze        | 1.000E+4   | N/A  |

| Parameter | Value      | Unit |
|-----------|------------|------|
| ZE        | 70.040     | Ohm  |
| Z0        | 39.370     | Ohm  |
| Z0        | 52.511663  | Ohm  |
| C_DB      | -11.046865 | N/A  |
| E_Eff     | 90.000     | deg  |

Calculated Results

- KE = 6.978
- KO = 4.870
- AE\_DB = 0.018
- AO\_DB = 0.032
- SkinDepth = 0.025

Values are consistent

# ADS linecalc

LineCalc/untitled

File Simulation Options Help

Component  
Type: MCLIN ID: MCLIN: MCLIN\_DEFAULT

Substrate Parameters

|      |              |
|------|--------------|
| ID   | Alumina      |
| H    | 15.000 mil   |
| Er   | 9.600 N/A    |
| Mur  | 1.000 N/A    |
| Cond | 5.96E+7 N/A  |
| Hu   | 3.9e+034 mil |
| T    | 1.400 mil    |
| TanD | 1.000e-4 N/A |

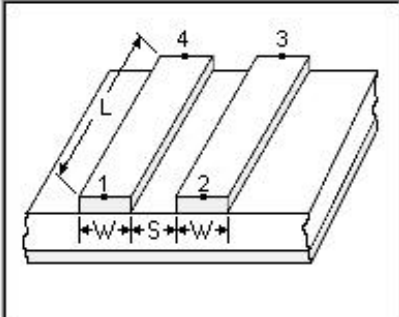
Physical

|   |                |
|---|----------------|
| W | 9.924291 mil   |
| S | 7.993661 mil   |
| L | 121.714173 mil |
|   | N/A            |

Synthesize Analyze

Electrical

|       |                |
|-------|----------------|
| ZE    | 70.040 Ohm     |
| ZO    | 39.370 Ohm     |
| Z0    | 52.511663 Ohm  |
| C_DB  | -11.046865 N/A |
| E_Eff | 90.000 deg     |



Calculated Results

KE = 6.978  
KO = 4.870  
AE\_DB = 0.018  
AO\_DB = 0.032  
SkinDepth = 0.025

Values are consistent



# Transmission lines

- <http://rf-opto.etti.tuiasi.ro>
- Transmission lines / Rogers
  - more precise formulas including
    - $t$ , trace thickness
    - $f$ , frequency
  - formulas for
    - microstrip
    - strip
    - coupled lines

# Implementation in microstrip technology

## MTEE

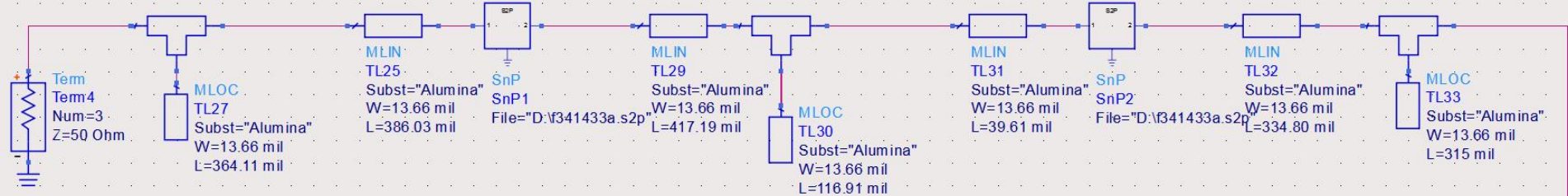
Tee1  
Subst="Alumina"  
W1=13.66 mil  
W2=13.66 mil  
W3=13.66 mil

## MTEE

Tee2  
Subst="Alumina"  
W1=13.66 mil  
W2=13.66 mil  
W3=13.66 mil

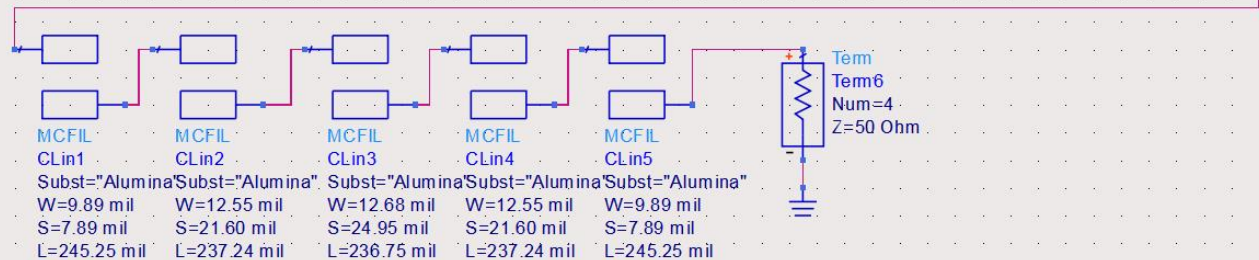
## MTEE

Tee3  
Subst="Alumina"  
W1=13.66 mil  
W2=13.66 mil  
W3=13.66 mil



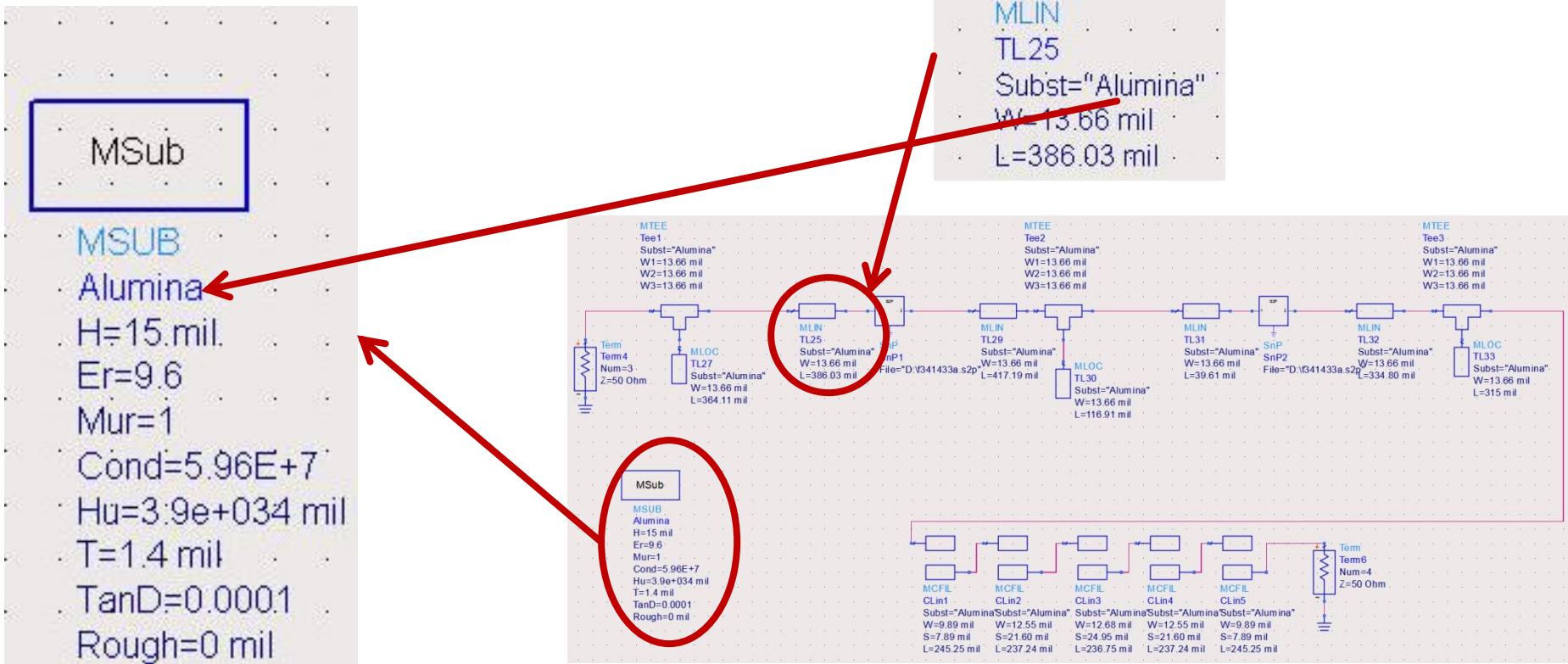
## MSub

MSUB  
Alumina  
H=15 mil  
Er=9.6  
Mur=1  
Cond=5.96E+7  
Hu=3.9e+034 mil  
T=1.4 mil  
TanD=0.0001  
Rough=0 mil



# Implementation in microstrip technology

- On all schematics you must have an substrate model/component
- Microstrip lines and coupled lines are computed in Linecalc for the same substrate

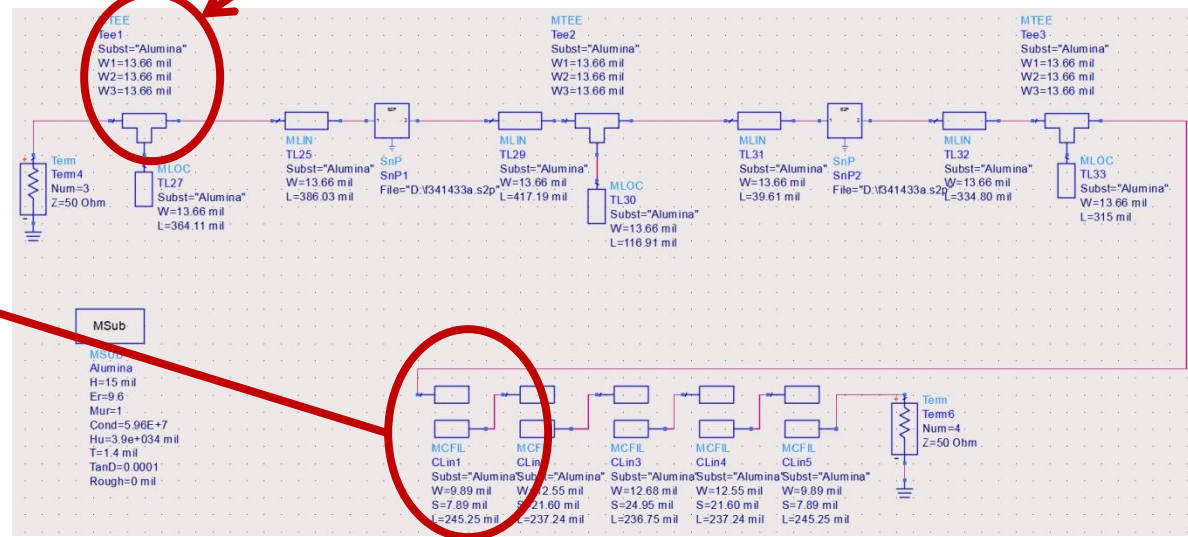
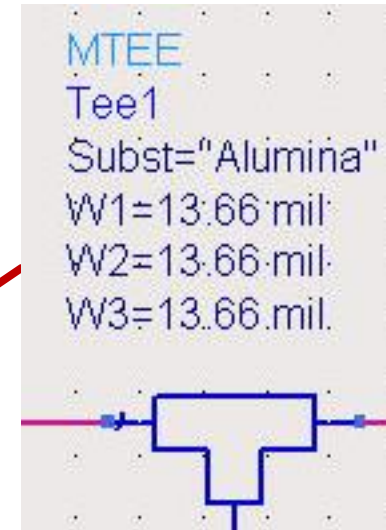


# Implementation in microstrip technology

- We use components from the “Transmission Lines – Microstrip” palette
  - MSUB - substrate
  - MLIN – series line
  - MLOC – open-circuit shunt stub
  - MTEE – modeling of T junction (shunt stub connection to main line)
  - MCFIL – coupled line filter section (more accurate model than MCLIN – takes into account that two adjacent sections are physically close)

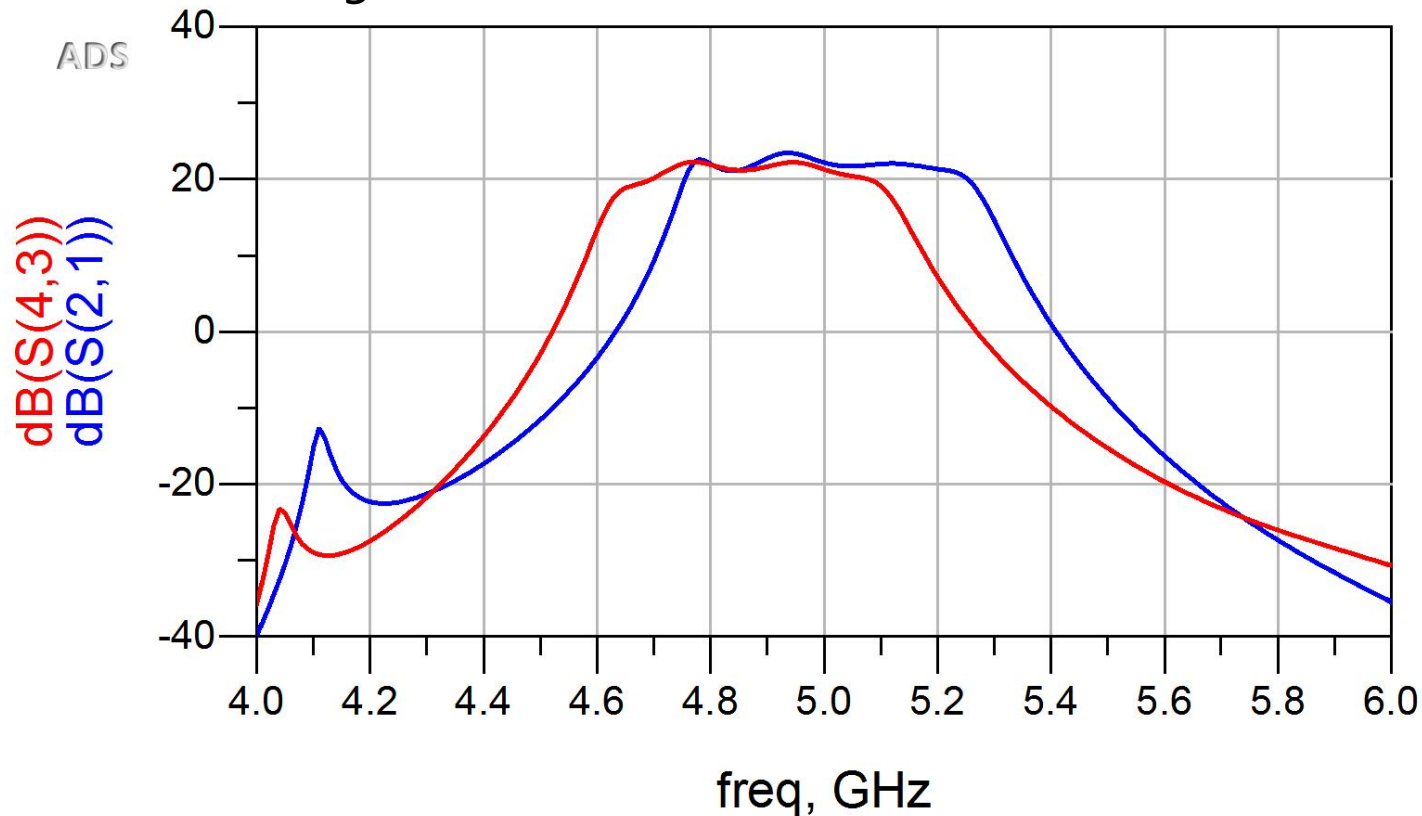
# Implementation in microstrip technology

- Attention is required when inserting parameters for MTEE and MCFIL by checking in the schematic the width of the lines connected to each port.



# Implementation in microstrip technology

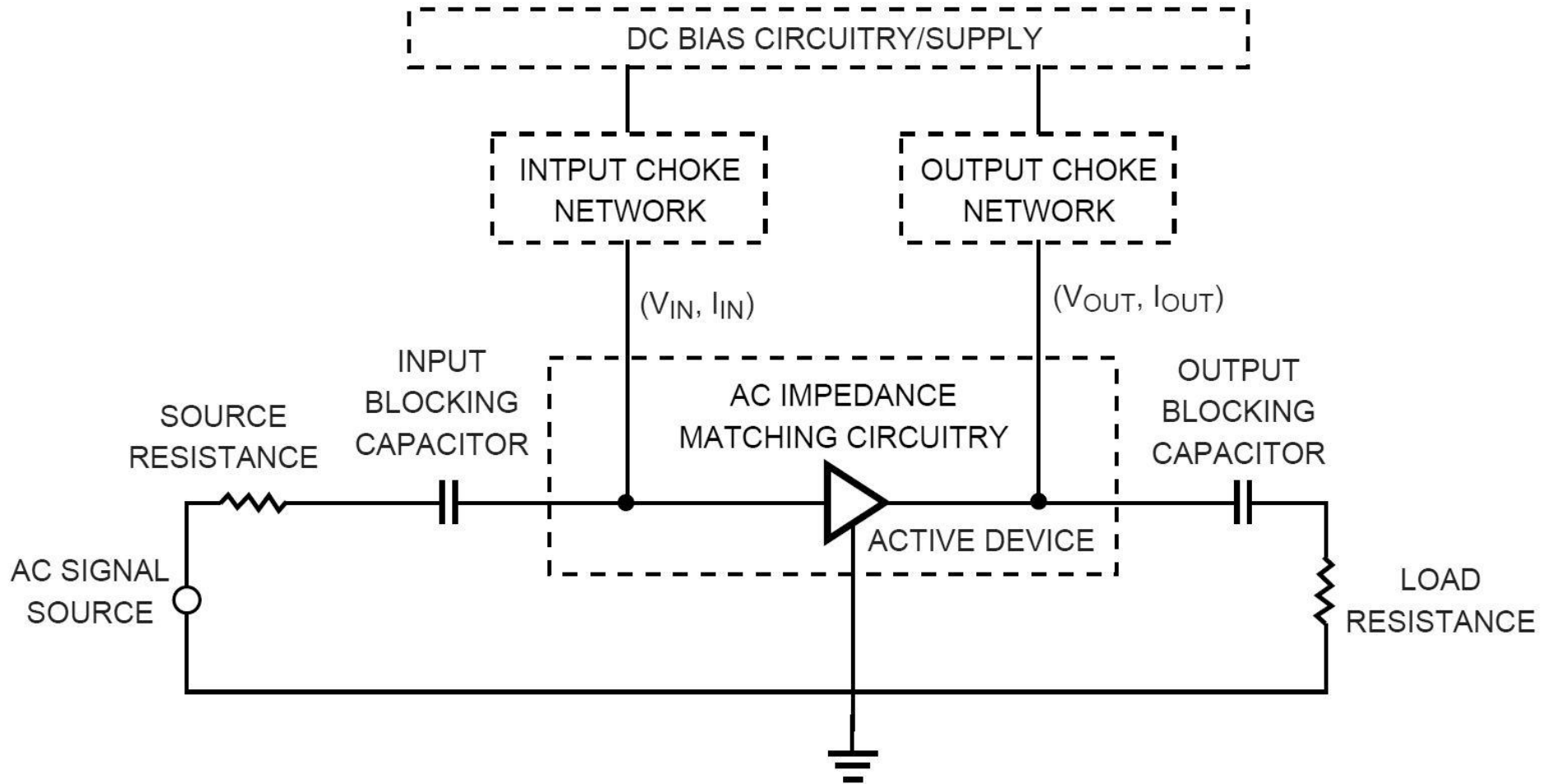
- Usually there is a shift of the transfer function (red) towards lower frequencies compared to the ideal model (blue)
  - due to the MCFIL/MCLIN difference
- Tune the length of filter elements to move the filter bandwidth around  $f_0 = 5\text{GHz}$



# DC Bias

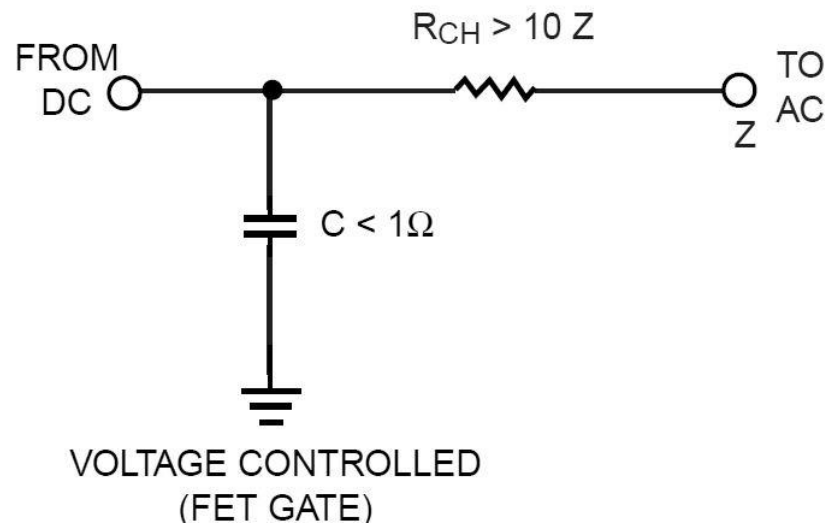
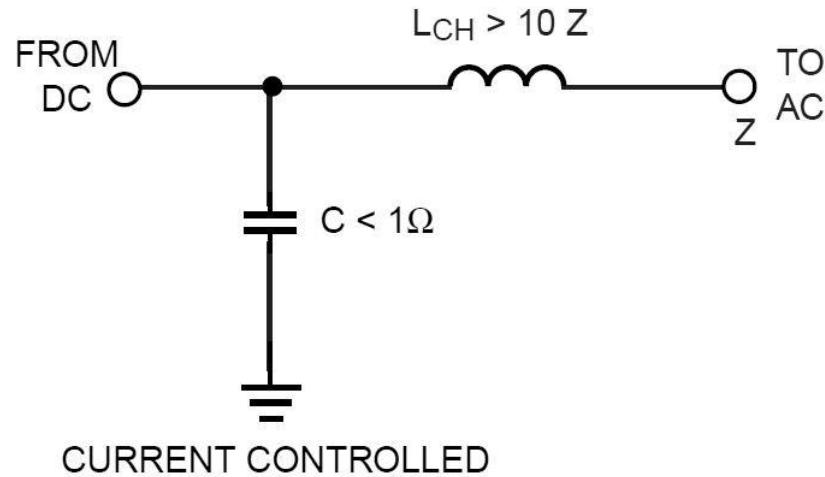
- <http://rf-opto.etti.tuiasi.ro>
- Agilent Application Notes
  - decoupling signal from DC Bias circuitry
  - DC Bias circuits for microwave transistors
- Appcad has tools for designing DC Bias circuits

# DC Bias

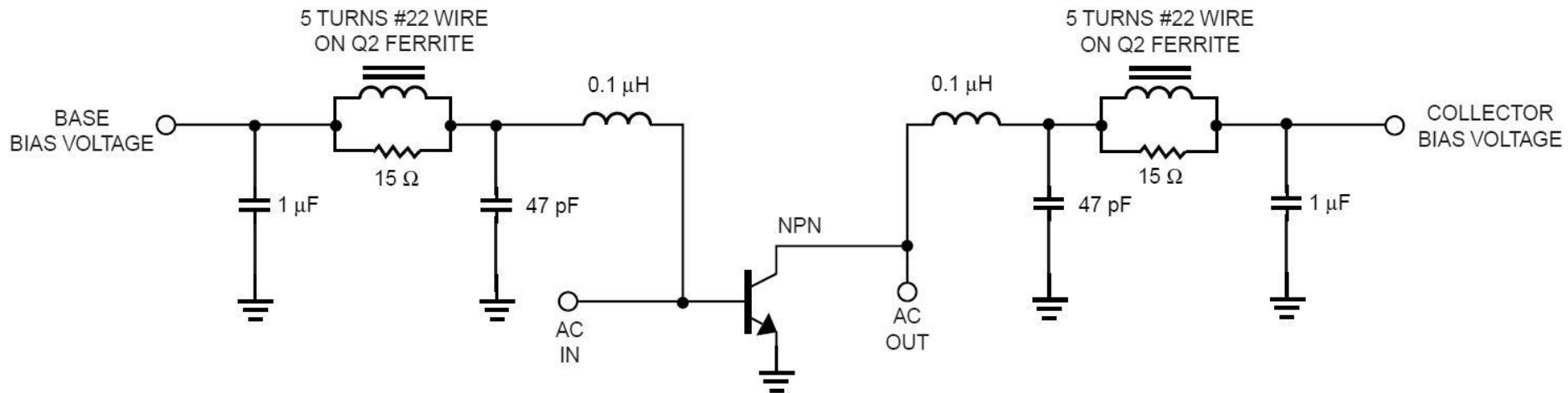
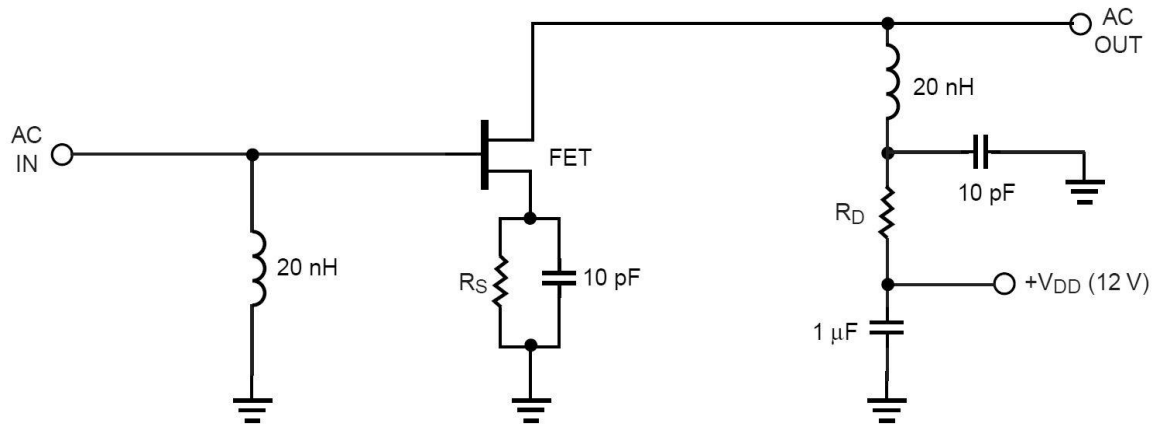




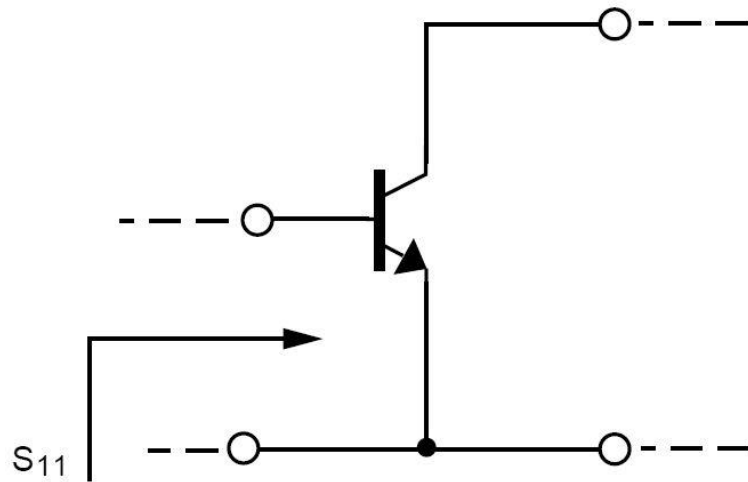
# DC Bias, typical choke



# DC Bias, typical schematics/values

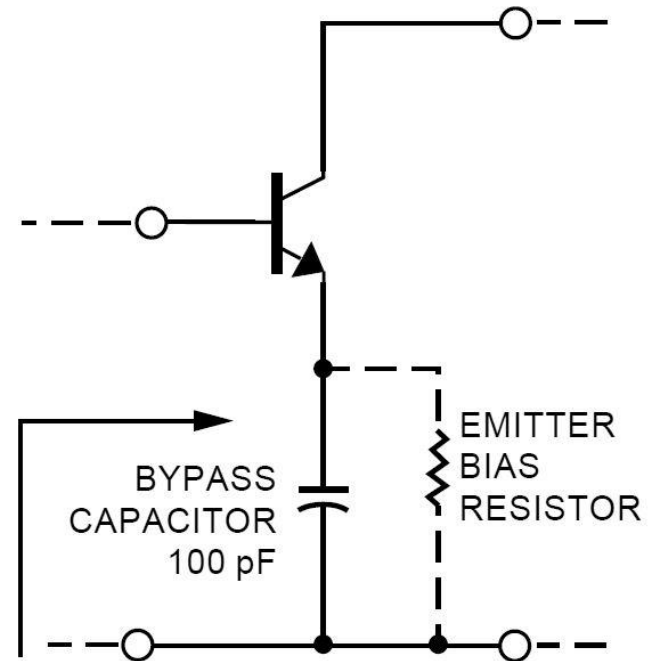


# DC Bias, elements in E/S



$$S_{11} (\text{AT } 4 \text{ GHz}) = 0.52 \angle 154^\circ$$

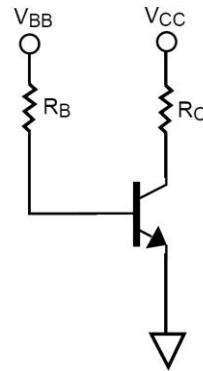
$$S_{11} (\text{AT } 0.1 \text{ GHz}) = 0.901 \angle -14.9^\circ$$



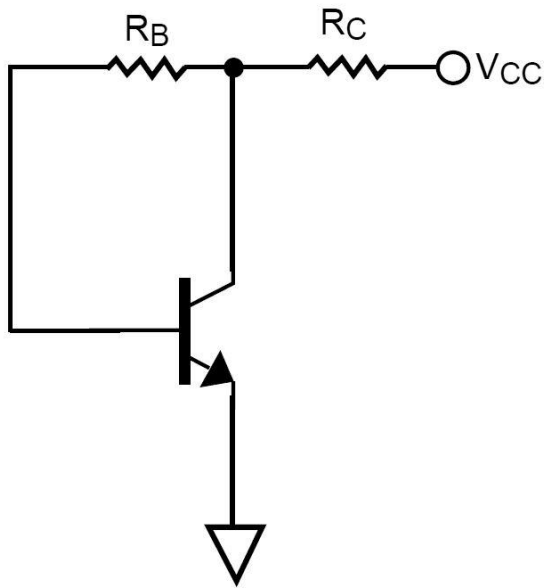
$$S'_{11} (\text{AT } 4 \text{ GHz}) = 0.52 \angle 154^\circ \text{ UNCHANGED AT } 4 \text{ GHz}$$

$$S'_{11} (\text{AT } 0.1 \text{ GHz}) = 1.066 \angle -8.5^\circ \quad |S_{11}| > 1 \text{ AT } 0.1 \text{ GHz}$$

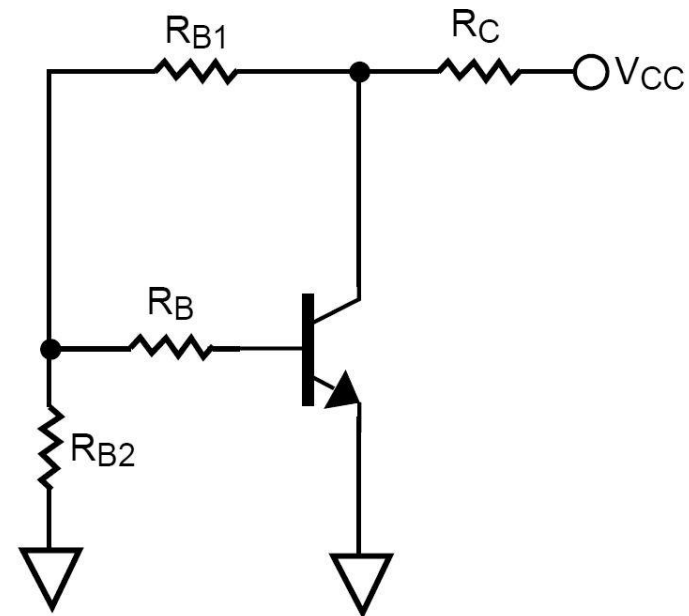
# DC Bias, bipolar transistors



NON-STABILIZED



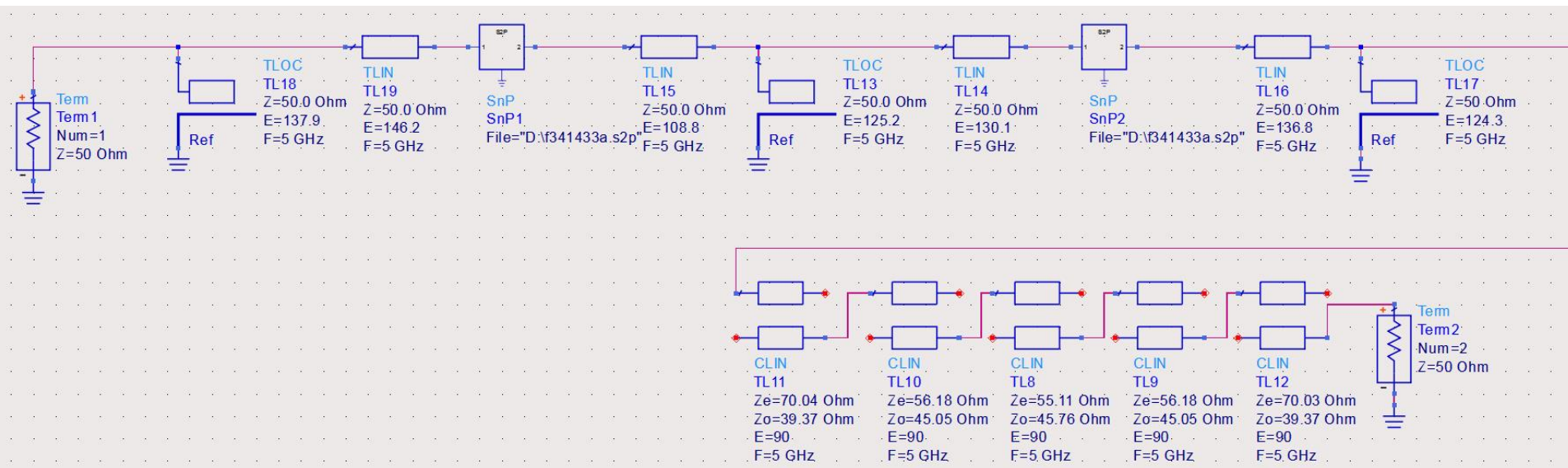
VOLTAGE FEEDBACK



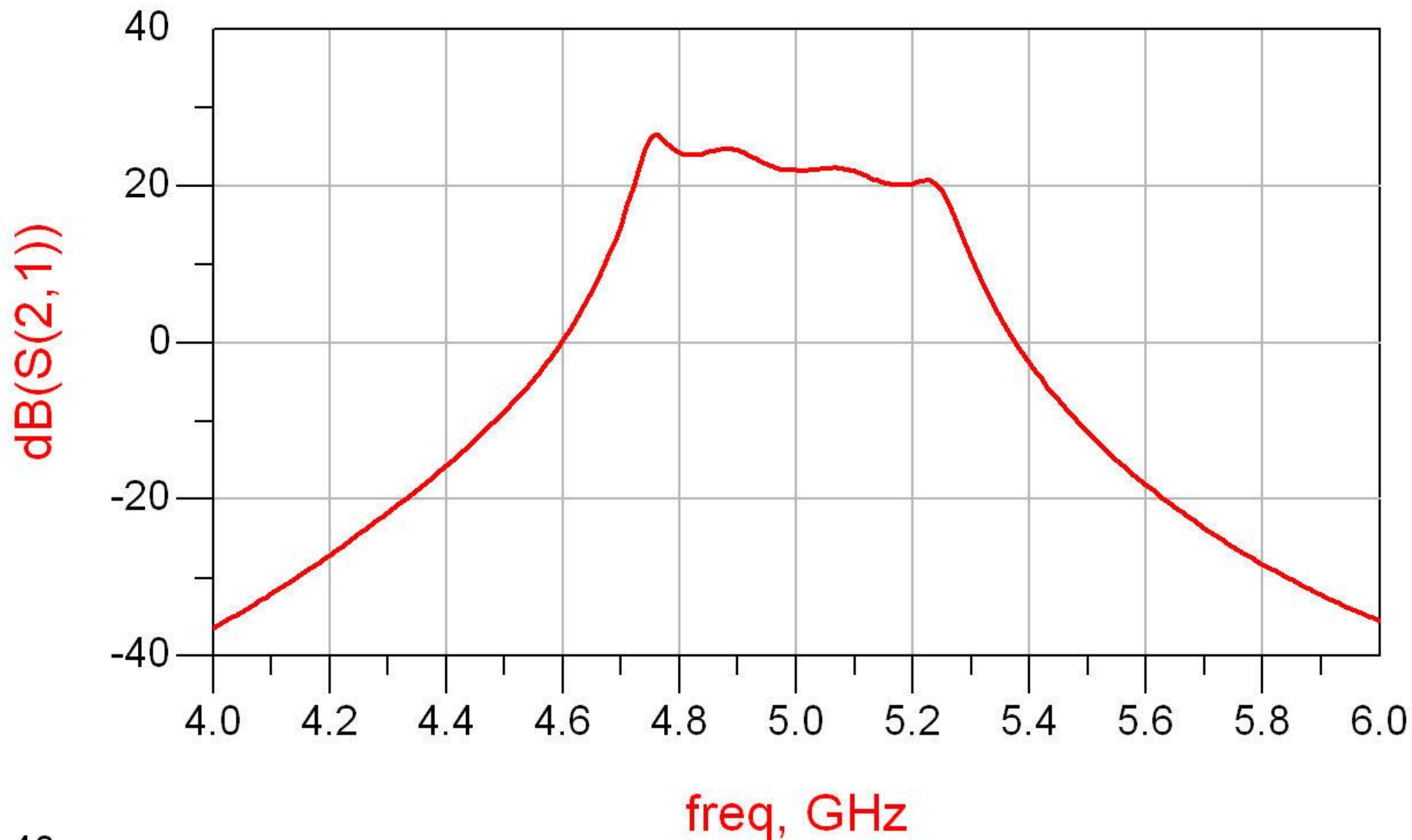
VOLTAGE FEEDBACK AND CONSTANT  
BASE CURRENT SOURCE

# Example project

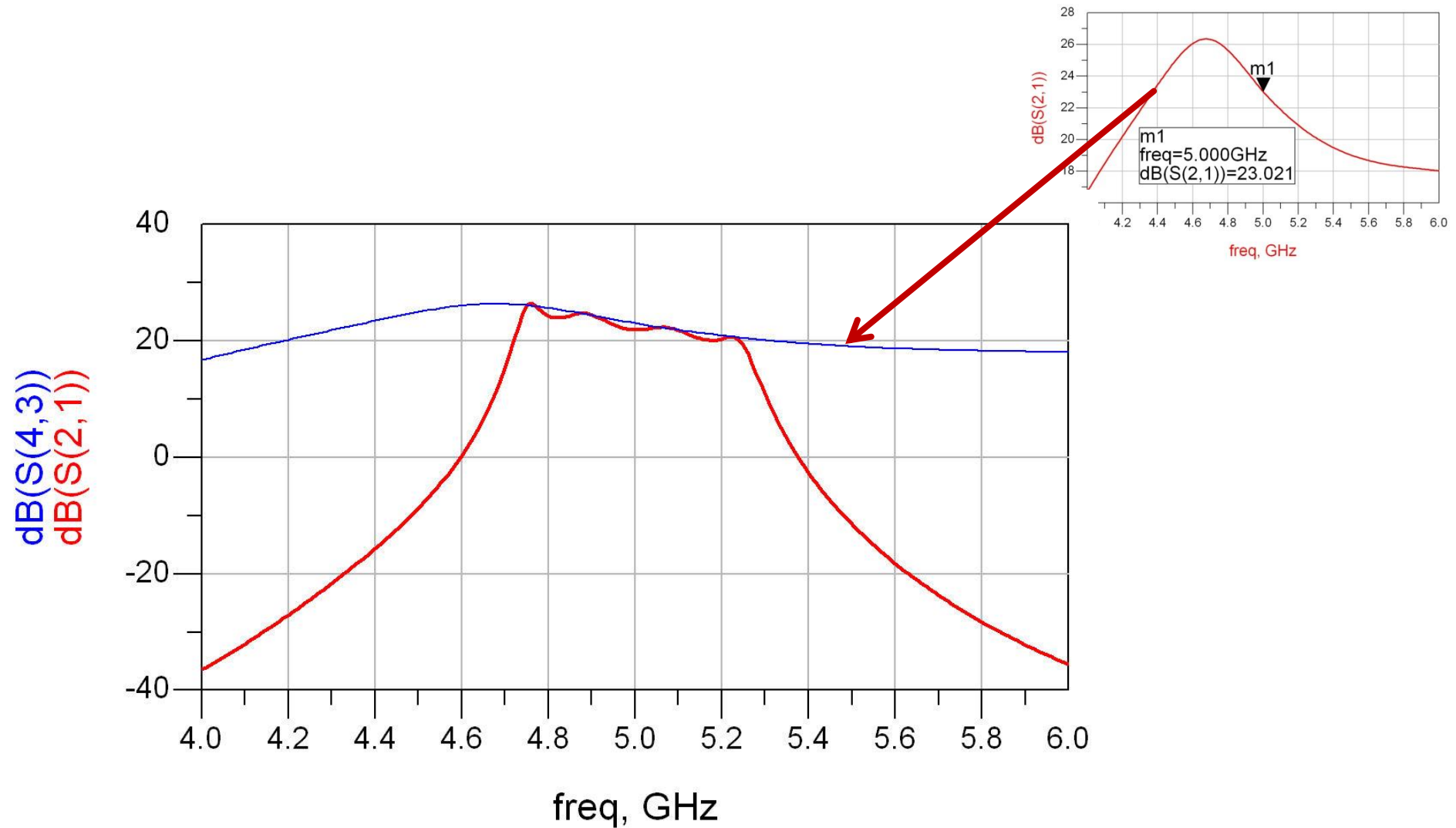
- Unify the two schematics
  - L10 – amplifier
  - L12 – filter



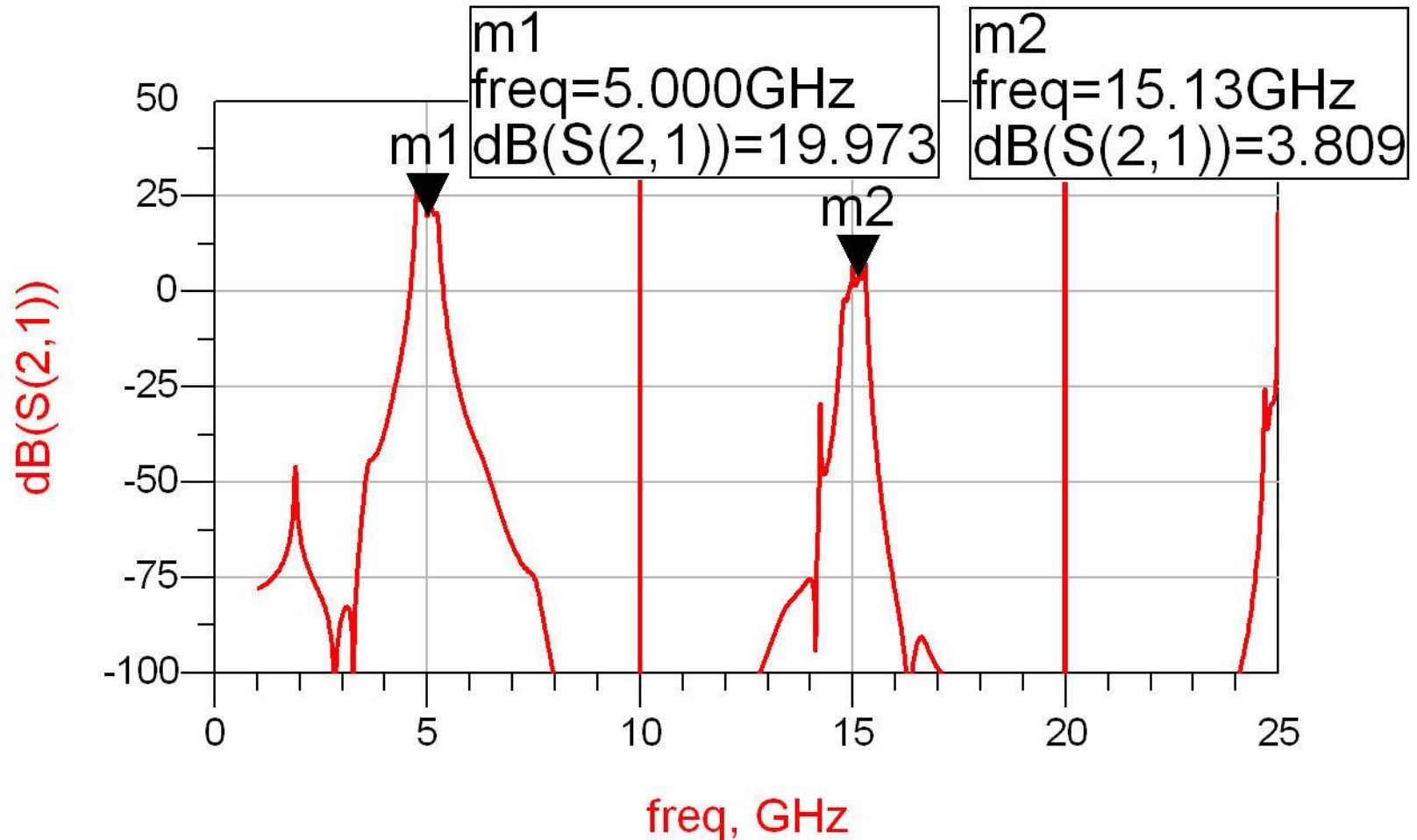
# Result (unbalanced)



# Result (unbalanced)



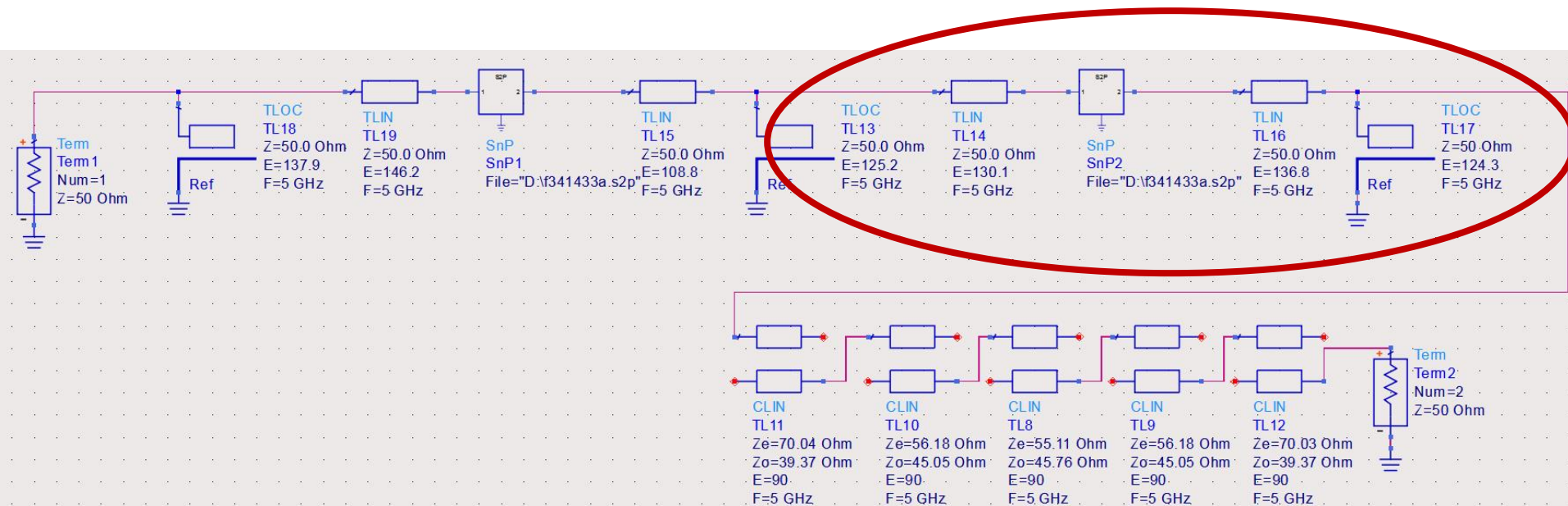
# Result (~periodic in frequency)



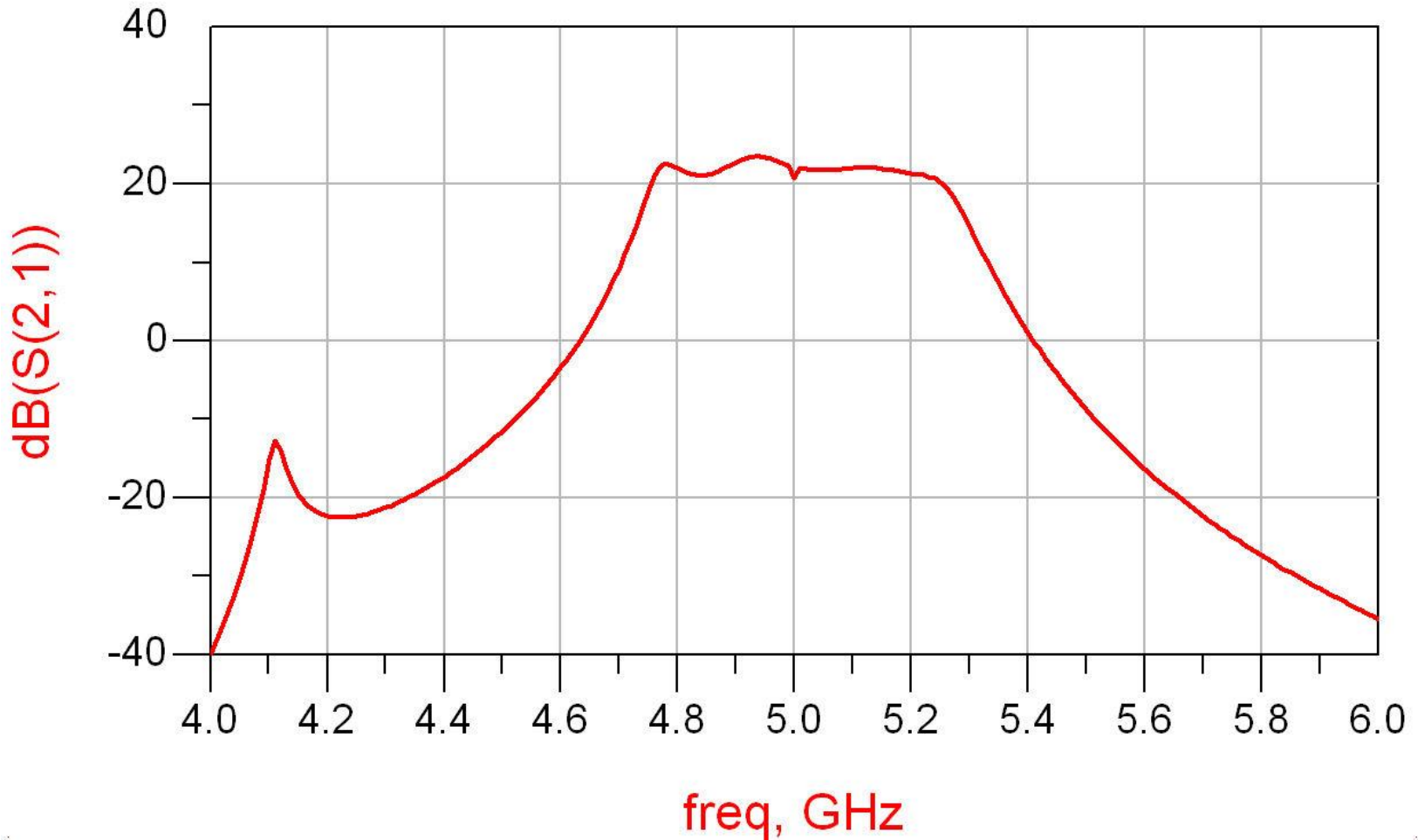


# Tune -> balance

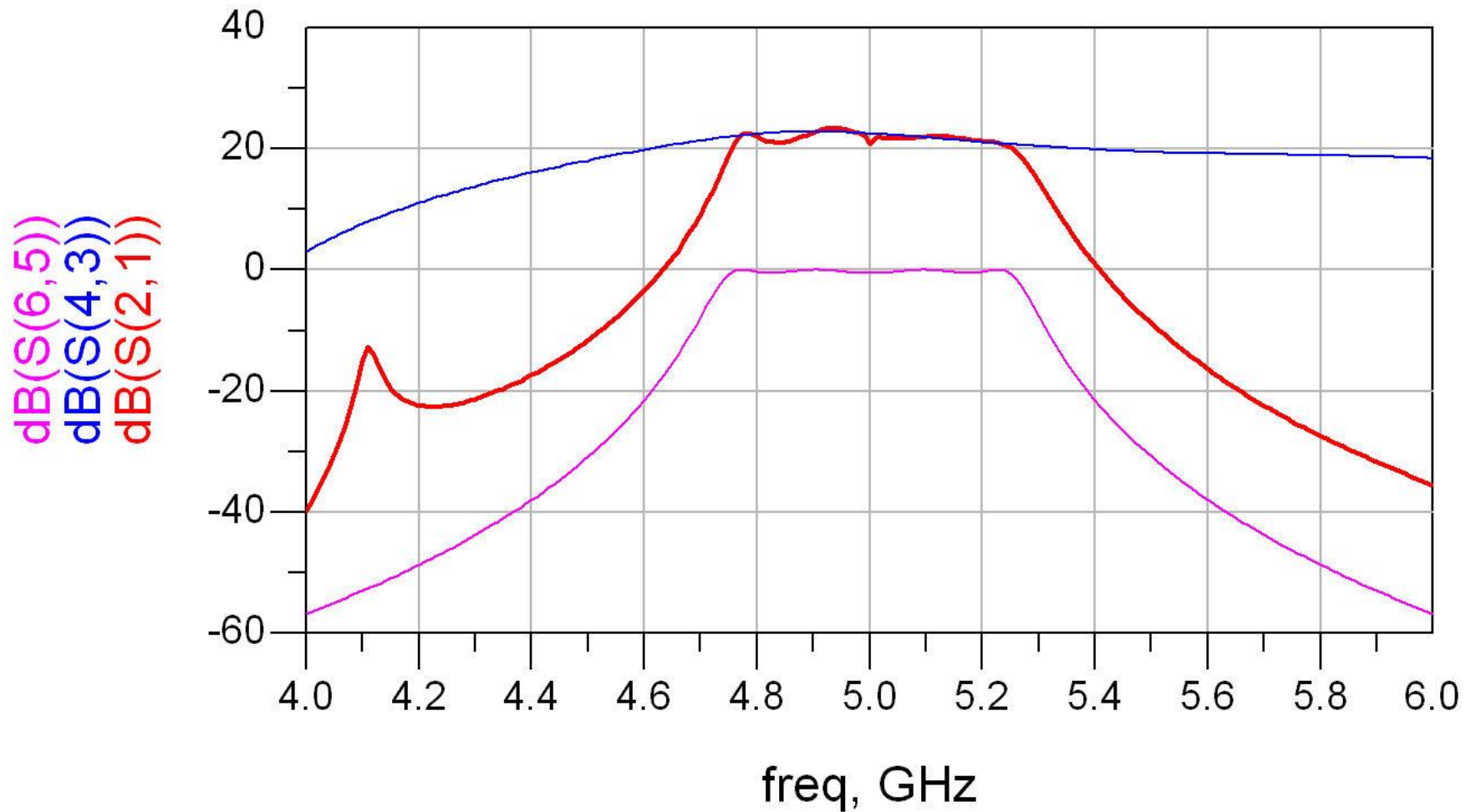
- purpose: balance the gain characteristic of the amplifier (maximum at design frequency)
  - favor tuning lines at the end of the amplifier
    - eliminate/minimize effect of the tune on noise



# Tune -> balance, result

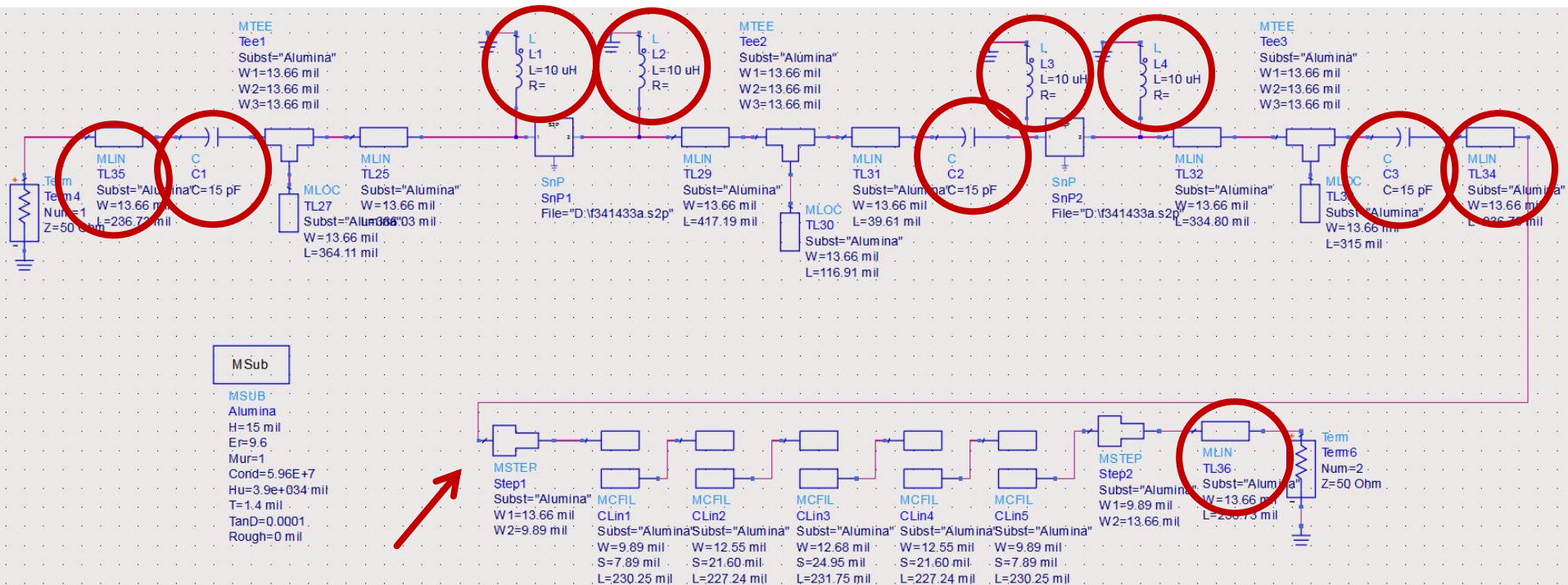


# Amplifier, Filter, Total

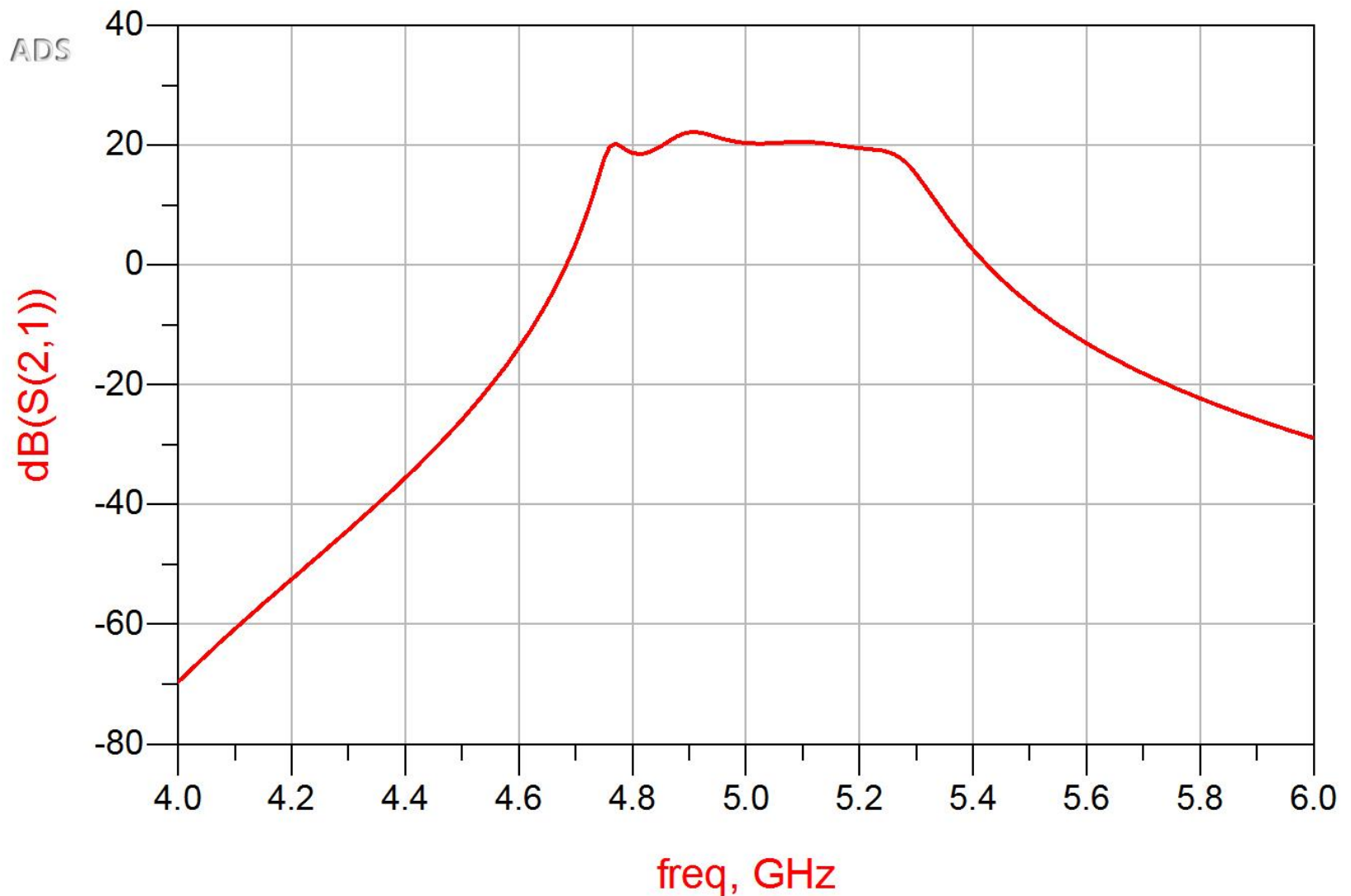


# DC Bias elements in ADS schematic

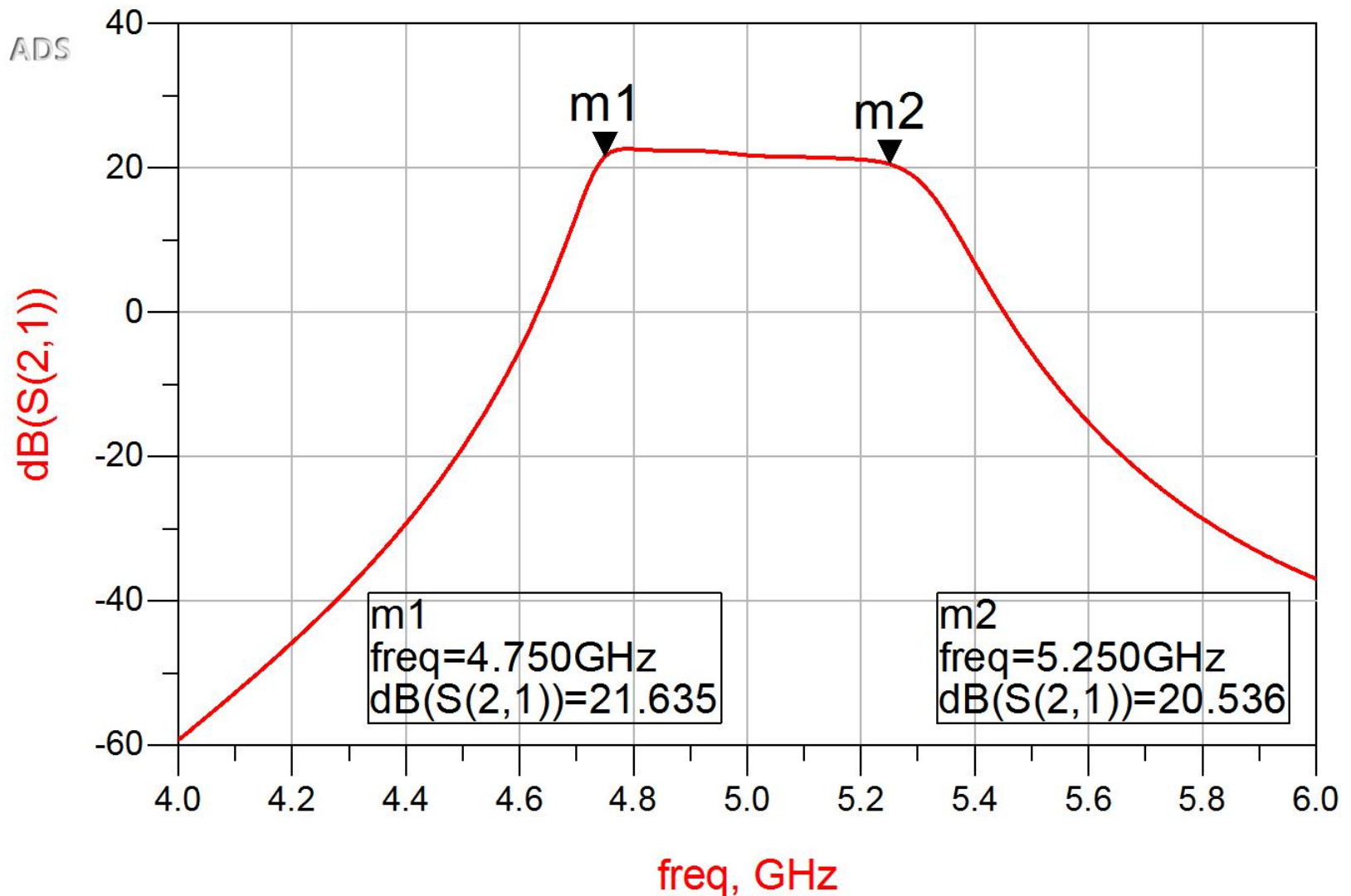
- Insert L (RF chokes) and C (decoupling)
- additional 50Ω connection lines
  - source
  - load
  - between blocks



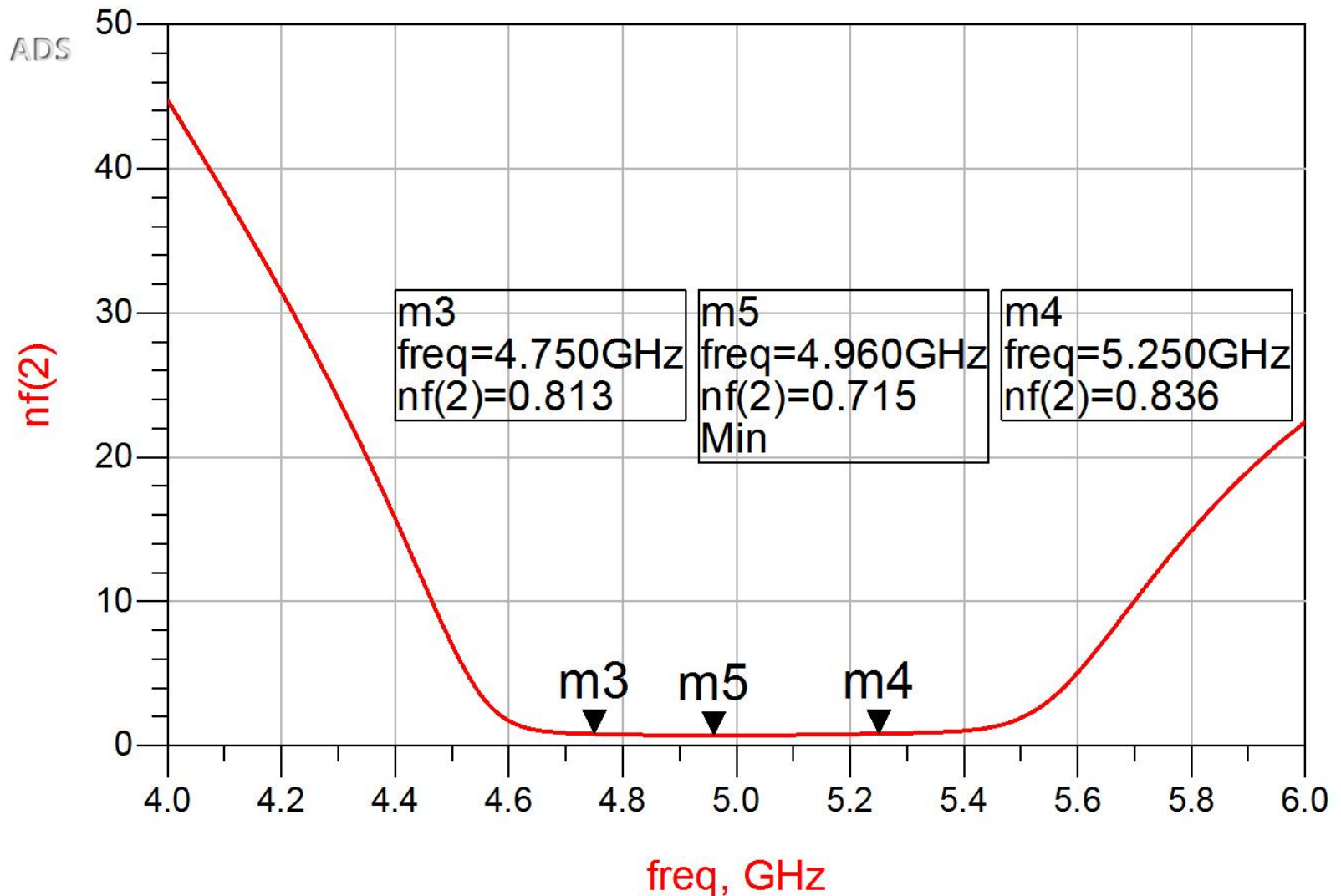
# Gain -> Tune/Optimization



# Final result (Gain)

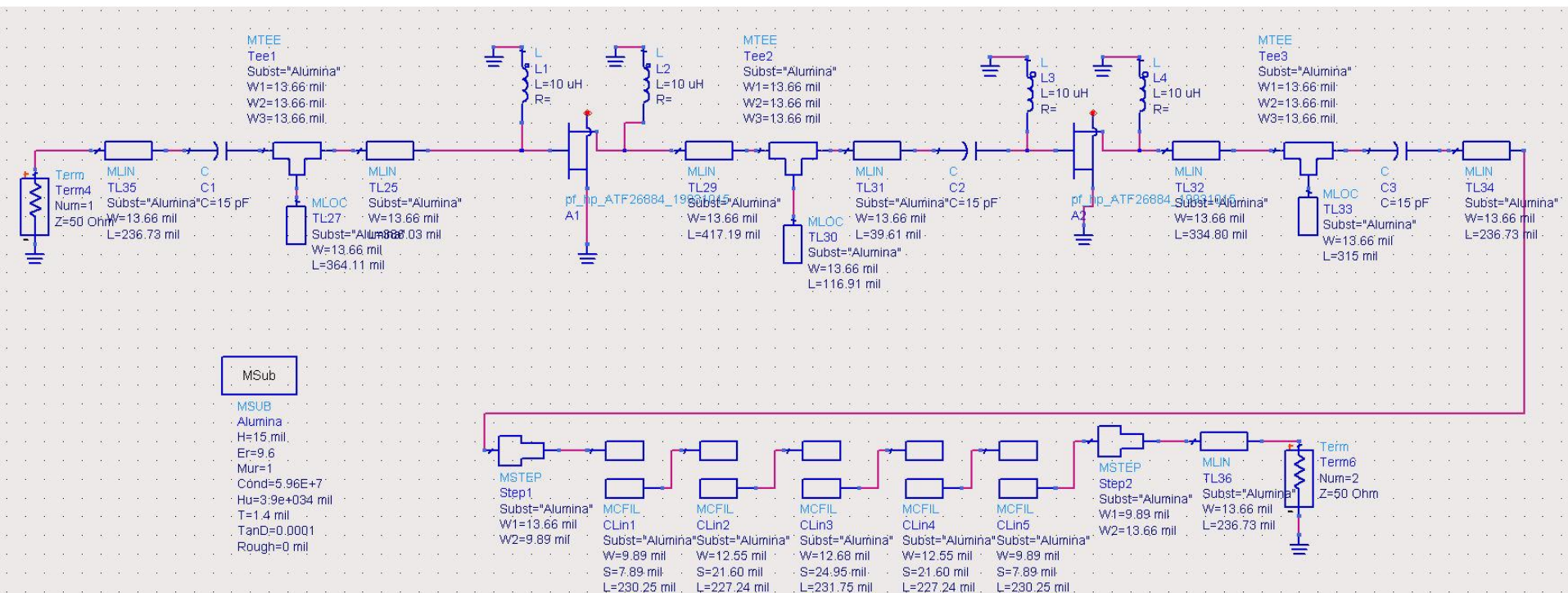


# Final result (Noise)



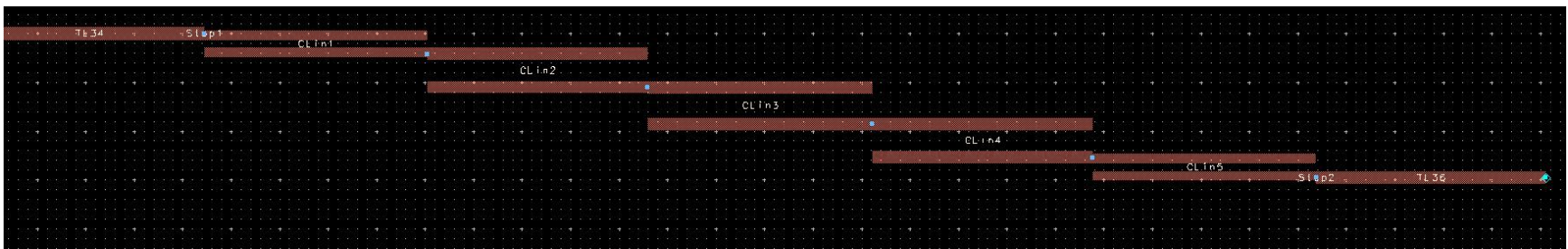
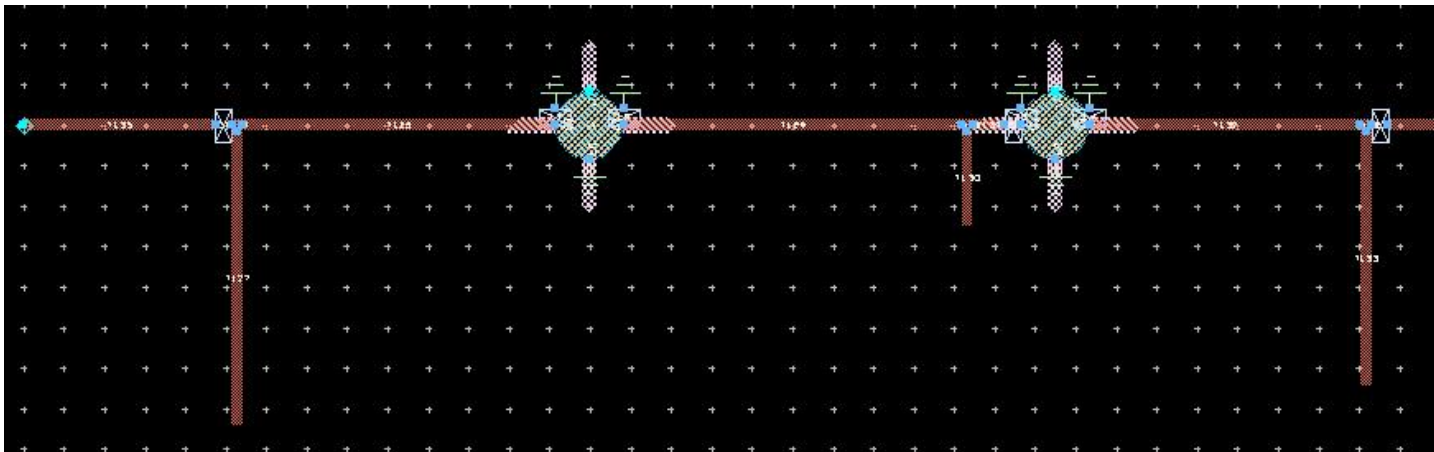
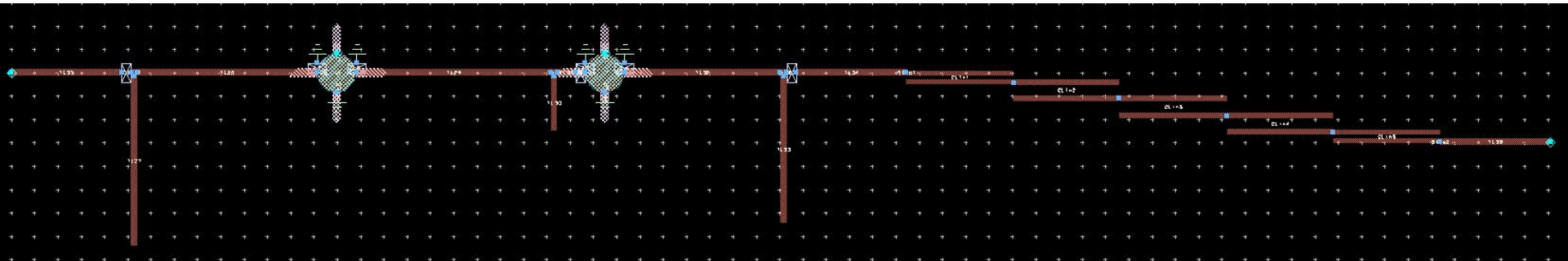
# Layout (Example)

- Temporary replacement of the transistors and lumped elements (LC) with elements for which ADS has case information





# Layout (Example)



# Contact

- Microwave and Optoelectronics Laboratory
- <http://rf-opto.etti.tuiasi.ro>
- [rdamian@etti.tuiasi.ro](mailto:rdamian@etti.tuiasi.ro)